

Class – XII  
**MATHEMATICS (041)**  
**SQP Marking Scheme (2019-20)**

**TIME: 3 Hrs.**

**Maximum Marks: 80**

SECTION A		
1	(c) 9	1
2	(a) $3 \times p$	1
3	(b) $p=3, q=\frac{27}{2}$	1
4	(b) 0.25	1
5	(c) (2,3)	1
6	(b) $\frac{\pi}{3}$	1
7	(c) $\frac{8}{15}$	1
8	(b) $\frac{1}{5} \sin^{-1} \left( \frac{5x}{3} \right) + c$	1
9	(a) 0	1
10	(b) $\vec{r} = (-\hat{i} + 3\hat{j} + 5\hat{k}) + \lambda(2\hat{i} + 3\hat{j})$	1
11	$g \left( \left[ -\frac{5}{4} \right] \right) = g(-2) = 2$	1
12	2	1
13	$y = 2$	1
14	$\frac{-3}{2}$  OR  decreasing at rate of 72 units/sec.	1
15	2 units  OR  $\frac{5}{7}(-2\hat{i} - 3\hat{j} + 6\hat{k})$	1
16	Apply $R_1 \rightarrow R_1 + R_2$ $\begin{vmatrix} l+m+n & m+n+l & n+l+m \\ n & l & m \\ 1 & 2 & 2 \end{vmatrix}$ $= 2(l+m+n) \begin{vmatrix} 1 & 1 & 1 \\ n & l & m \\ 1 & 1 & 1 \end{vmatrix}$ ; yes $(l+m+n)$ is a factor	1
17	$\int_{-2}^2 (x^3 + 1) dx = \int_{-2}^2 (x^3) dx + \int_{-2}^2 1 dx = I_1 + I_2$ $= 0 + [x]_{-2}^2$ (As $I_1$ is odd function) $= 2+2$ $= 4$	1

18	Let $x + \sin x = t$ So $(1 + \cos x) dx = dt$ $I = 3 \int \frac{dt}{t} = 3 \log t  + c = 3 \log (x + \sin x)  + c$ or directly by writing formula $\int \frac{f'(x)}{f(x)} dx = \log f(x)  + c$ <p style="text-align: center;"><b>OR</b></p> $\int \cos 4x dx = \frac{\sin 4x}{4} + c$	1
19	let $(1 + x^2) = t$ so $2x dx = dt$ $\Rightarrow I = \frac{1}{2} \int e^t dt = \frac{1}{2} e^t + c = \frac{1}{2} e^{(1+x^2)} + c$	1
20	$\frac{dy}{dx} = e^x e^y$ $\Rightarrow \frac{dy}{e^y} = e^x dx$ integrating both sides $\Rightarrow -e^{-y} + c = e^x$ $\Rightarrow e^x + e^{-y} = c$	1
<b>SECTION B</b>		
21	$= \sin^{-1} \left( \frac{\sin x}{\sqrt{2}} + \frac{\cos x}{\sqrt{2}} \right)$ if $-\frac{\pi}{4} < x < \frac{\pi}{4}$ $= \sin^{-1} \left( \sin x \cos \frac{\pi}{4} + \cos x \sin \frac{\pi}{4} \right)$ if $-\frac{\pi}{4} + \frac{\pi}{4} < x + \frac{\pi}{4} < \frac{\pi}{4} + \frac{\pi}{4}$ $= \sin^{-1} \left( \sin \left( x + \frac{\pi}{4} \right) \right)$ if $0 < \left( x + \frac{\pi}{4} \right) < \frac{\pi}{2}$ i.e. principal values $= \left( x + \frac{\pi}{4} \right)$	1
	<p style="text-align: center;"><b>OR</b></p> Let 2 divides $(a - b)$ and 2 divides $(b - c)$ : where $a, b, c \in Z$ So 2 divides $[(a - b) + (b - c)]$ 2 divides $(a - c)$ : Yes relation R is transitive $[0] = \{0, \pm 2, \pm 4, \pm 6, \dots\}$	1
22	$y = ae^{2x} + be^{-x} \dots \dots \dots (1)$ $\frac{dy}{dx} = 2ae^{2x} - be^{-x} \dots \dots \dots (2)$ $\frac{d^2y}{dx^2} = 4ae^{2x} + be^{-x} \dots \dots \dots (3)$ putting values on LHS $= \frac{d^2y}{dx^2} - \frac{dy}{dx} - 2y$ $= (4ae^{2x} + be^{-x}) - (2ae^{2x} - be^{-x}) - 2(ae^{2x} + be^{-x})$ $= 4ae^{2x} + be^{-x} - 2ae^{2x} + be^{-x} - 2ae^{2x} - 2be^{-x}$ $= 0$	1
		1

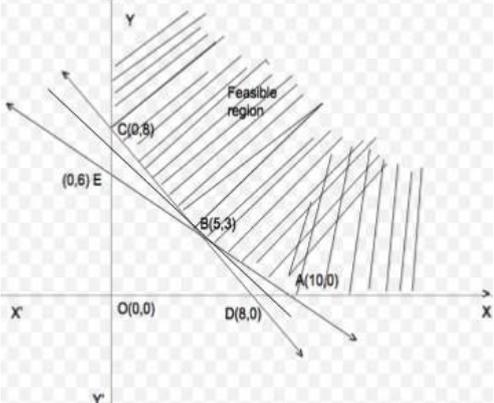


	$= P(A)P(B) \text{ or } P(\bar{A})P(\bar{B})$ $= \left(\frac{4}{5}\right)\left(\frac{9}{10}\right) + \left(\frac{1}{5}\right)\left(\frac{1}{10}\right)$ $= \frac{36+1}{50} = \frac{37}{50}$ $= \frac{74}{100} = 74\%$	1
	<b>SECTION C</b>	
27	<p>Let <math>y = f(x) = \frac{2x+3}{x-3}</math> .....(1)</p> <p>Let <math>x_1, x_2 \in A = \mathbb{R} - \{3\}</math></p> <p>Let <math>f(x_1) = f(x_2)</math></p> $\Rightarrow \frac{2x_1+3}{x_1-3} = \frac{2x_2+3}{x_2-3}$ $\Rightarrow (2x_1+3)(x_2-3) = (2x_2+3)(x_1-3)$ $\Rightarrow (2x_1x_2 - 6x_1 + 3x_2 - 9) = (2x_1x_2 - 6x_2 + 3x_1 - 9)$ $\Rightarrow -6x_1 + 3x_2 = -6x_2 + 3x_1$ $\Rightarrow 9x_1 = 9x_2$ $\Rightarrow x_1 = x_2$ <p>Now <math>f(x_1) = f(x_2) \Rightarrow x_1 = x_2</math></p> <p>so <math>f(x)</math> is one-one</p> <p>For onto</p> $y = \frac{2x+3}{x-3}$ $\Rightarrow xy - 3y = 2x + 3$ $\Rightarrow xy - 2x = 3y + 3$ $\Rightarrow x(y-2) = 3(y+1)$ $\Rightarrow x = \frac{3(y+1)}{(y-2)} \text{ .....(2)}$ <p>equation (2) is defined for all real values of <math>y</math> except 2 i.e <math>y \in \mathbb{R} - \{2\}</math> which is same as given set <math>B = \mathbb{R} - \{2\}</math> (co-domain=range)</p> <p>Also <math>y = f(x)</math></p> $f(x) = f\left(\frac{3(y+1)}{(y-2)}\right)$ $= \frac{2\left[\frac{3(y+1)}{(y-2)}\right] + 3}{\frac{3(y+1)}{(y-2)} - 3} \left(\text{since } f(x) = \frac{2x+3}{x-3}\right)$ $\frac{2(3y+3) + 3(y-2)}{3y+3-3y+6} = \frac{9y}{9} = y$ <p>Thus for every <math>y \in B</math>, there exists <math>x \in A</math> such that <math>f(x) = y</math></p> <p>Thus function is onto.</p> <p>Since <math>f(x)</math> is one-one and onto so <math>f(x)</math> is invertible.</p> <p>Inverse is given by <math>x = f^{-1}(y) = \frac{3(y+1)}{(y-2)}</math></p>	<p><math>\frac{1}{2}</math></p> <p>1</p> <p><math>\frac{1}{2}</math></p> <p>1</p>
28	$\sqrt{1-x^2} + \sqrt{1-y^2} = a(x-y)$ <p>Let <math>x = \sin A</math> , <math>y = \sin B</math></p> $\sqrt{1-\sin^2 A} + \sqrt{1-\sin^2 B} = a(\sin A - \sin B)$ $\cos A + \cos B = a(\sin A - \sin B)$ $\Rightarrow 2 \cos\left(\frac{A+B}{2}\right) \cos\left(\frac{A-B}{2}\right) = 2a \cos\left(\frac{A+B}{2}\right) \sin\left(\frac{A-B}{2}\right)$ $\Rightarrow \cos\left(\frac{A-B}{2}\right) = a \sin\left(\frac{A-B}{2}\right)$	<p><math>\frac{1}{2}</math></p> <p>1</p>

	$\Rightarrow \cot\left(\frac{A-B}{2}\right) = a$ $\Rightarrow \frac{A-B}{2} = \cot^{-1} a$ $\Rightarrow A-B = 2 \cot^{-1} a$ $\Rightarrow \sin^{-1} x - \sin^{-1} y = 2 \cot^{-1} a$ <p>differentiating w.r.t. x</p> $\Rightarrow \frac{1}{\sqrt{1-x^2}} - \frac{1}{\sqrt{1-y^2}} \frac{dy}{dx} = 0$ $\Rightarrow \frac{dy}{dx} = \frac{\sqrt{1-y^2}}{\sqrt{1-x^2}}$ <p style="text-align: center;"><b>OR</b></p>	<p style="text-align: center;">1</p> <p style="text-align: center;">1</p> <p style="text-align: center;"><math>\frac{1}{2}</math></p>
	$x = a(\cos 2\theta + 2\theta \sin 2\theta)$ $\Rightarrow \frac{dx}{d\theta} = a(-2 \sin 2\theta + 2 \sin 2\theta + 4\theta \cos 2\theta)$ $\Rightarrow \frac{dx}{d\theta} = a(4\theta \cos 2\theta) \dots \dots \dots (1)$ $y = a(\sin 2\theta - 2\theta \cos 2\theta)$ $\Rightarrow \frac{dy}{d\theta} = a(2 \cos 2\theta + 4\theta \sin 2\theta - 2 \cos 2\theta)$ $\Rightarrow \frac{dy}{d\theta} = a(4\theta \sin 2\theta) \dots \dots \dots (2)$ <p>using (1) and (2)</p> $\Rightarrow \frac{dy}{dx} = \frac{a(4\theta \sin 2\theta)}{a(4\theta \cos 2\theta)}$ $\Rightarrow \frac{dy}{dx} = \frac{\sin 2\theta}{\cos 2\theta} = \tan 2\theta$ <p>Differentiating again with respect to x, we get</p> $\Rightarrow \frac{d^2y}{dx^2} = 2 \sec^2 2\theta \cdot \frac{d\theta}{dx}$ $\Rightarrow \frac{d^2y}{dx^2} = 2 \sec^2 2\theta \cdot \frac{1}{a(4\theta \cos 2\theta)}$ $\left. \frac{d^2y}{dx^2} \right _{\theta=\frac{\pi}{8}} = 2 \sec^2 \frac{\pi}{4} \cdot \frac{1}{4a \left(4 \frac{\pi}{8} \cos \frac{\pi}{4}\right)}$ $= \frac{8\sqrt{2}}{\pi a}$	<p style="text-align: center;">1</p> <p style="text-align: center;">1</p> <p style="text-align: center;"><math>\frac{1}{2}</math></p> <p style="text-align: center;"><math>\frac{1}{2}</math></p> <p style="text-align: center;">1</p>
29	$x \frac{dy}{dx} - y = \sqrt{x^2 + y^2}$ $\Rightarrow x \frac{dy}{dx} = y + \sqrt{x^2 + y^2}$ $\Rightarrow \frac{dy}{dx} = \frac{y + \sqrt{x^2 + y^2}}{x} \dots \dots \dots (1)$ <p style="text-align: center;">let <math>y = vx</math></p> <p>differentiating with w.r.t. x</p> $\Rightarrow \frac{dy}{dx} = v + x \frac{dv}{dx}$ <p>put in (1)</p>	<p style="text-align: center;">1</p>

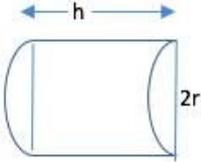
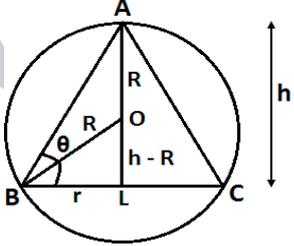




	 <p>corner points of feasible region are A(10,0), B(5,3) and C(0,8) Value of Z at these corner points</p> <table border="1" data-bbox="406 660 1109 795"> <thead> <tr> <th>Point</th> <th>Z = 150x + 200y (in ₹)</th> </tr> </thead> <tbody> <tr> <td>A(10,0)</td> <td>=1500+0=1500</td> </tr> <tr> <td>B(5,3)</td> <td>=750+600=1350 (minimum)</td> </tr> <tr> <td>C(0,8)</td> <td>=0+1600=1600</td> </tr> </tbody> </table> <p>So minimum value of Z is ₹1350 when tailor A works for 5 days and tailor B works for 3 days. To check draw <math>150x + 200y &lt; 1350</math> i.e <math>3x + 4y &lt; 27</math> As there is no region common with feasible region so minimum value is ₹1350</p>	Point	Z = 150x + 200y (in ₹)	A(10,0)	=1500+0=1500	B(5,3)	=750+600=1350 (minimum)	C(0,8)	=0+1600=1600	<p>1</p> <p>1</p>
Point	Z = 150x + 200y (in ₹)									
A(10,0)	=1500+0=1500									
B(5,3)	=750+600=1350 (minimum)									
C(0,8)	=0+1600=1600									
<b>SECTION D</b>										
<p>33</p>	$\text{LHS} = \begin{vmatrix} (y+z)^2 & x^2 & x^2 \\ y^2 & (z+x)^2 & y^2 \\ z^2 & z^2 & (x+y)^2 \end{vmatrix}$ <p style="text-align: center;">Apply <math>C_2 \rightarrow C_2 - C_1, C_3 \rightarrow C_3 - C_1</math></p> $= \begin{vmatrix} (y+z)^2 & x^2 - (y+z)^2 & x^2 - (y+z)^2 \\ y^2 & (z+x)^2 - y^2 & y^2 \\ z^2 & z^2 & (x+y)^2 - z^2 \end{vmatrix}$ $= \begin{vmatrix} (y+z)^2 & (x+y+z)(x-y-z) & (x+y+z)(x-y-z) \\ y^2 & (z+x+y)(z+x-y) & 0 \\ z^2 & 0 & (x+y+z)(x+y-z) \end{vmatrix}$ <p>Taking <math>(x+y+z)</math> common from <math>C_2</math> as well as <math>C_3</math></p> $= (x+y+z)^2 \begin{vmatrix} (y+z)^2 & (x-y-z) & (x-y-z) \\ y^2 & (z+x-y) & 0 \\ z^2 & 0 & (x+y-z) \end{vmatrix}$ <p>Apply <math>R_1 \rightarrow R_1 - R_2 - R_3</math></p> $= (x+y+z)^2 \begin{vmatrix} 2yz & -2z & -2y \\ y^2 & (z+x-y) & 0 \\ z^2 & 0 & (x+y-z) \end{vmatrix}$	<p>1</p> <p>1</p> <p>1</p>								

<p>Apply <math>C_2 \rightarrow y C_2</math> and <math>C_3 \rightarrow z C_3</math></p> $= \frac{(x+y+z)^2}{yz} \begin{vmatrix} 2yz & -2yz & -2yz \\ y^2 & (yz + yx - y^2) & 0 \\ z^2 & 0 & (zx + zy - z^2) \end{vmatrix}$ <p>Apply <math>C_2 \rightarrow C_2 + C_1</math> and <math>C_3 \rightarrow C_3 + C_1</math></p> $= \frac{(x+y+z)^2}{yz} \begin{vmatrix} 2yz & 0 & 0 \\ y^2 & (yz + yx) & y^2 \\ z^2 & z^2 & (zx + zy) \end{vmatrix}$ <p>expanding along <math>R_1</math></p> $= \left(\frac{(x+y+z)^2}{yz}\right) 2yz[(yz + yx)(zx + zy) - y^2 z^2]$ $= 2(x + y + z)^2 [xyz^2 + x^2 yz + xy^2 z + y^2 z^2 - y^2 z^2]$ $= 2xyz(x + y + z)^2 (x + y + z)$ $= 2xyz(x + y + z)^3$ <p style="text-align: center;"><b>OR</b></p>	<p>1</p> <p>1</p> <p>1</p>
<p>** <math>A = \begin{bmatrix} 2 &amp; 3 &amp; 4 \\ 1 &amp; -1 &amp; 0 \\ 0 &amp; 1 &amp; 2 \end{bmatrix}</math></p> $ A  = 2(-2) - 3(2 - 0) + 4(1 - 0) = -6 \neq 0$ <p style="text-align: center;"><math>\therefore A^{-1}</math> exists</p> <p>Cofactors</p> $A_{11} = -2 \quad A_{12} = -2 \quad A_{13} = 1$ $A_{21} = -2 \quad A_{22} = 4 \quad A_{23} = -2$ $A_{31} = 4 \quad A_{32} = 4 \quad A_{33} = -5$ $Adj A = \begin{bmatrix} -2 & -2 & 1 \\ -2 & 4 & -2 \\ 4 & 4 & -5 \end{bmatrix}'$ $Adj A = \begin{bmatrix} -2 & -2 & 4 \\ -2 & 4 & 4 \\ 1 & -2 & -5 \end{bmatrix}$ $A^{-1} = \frac{Adj A}{ A } = \frac{1}{-6} \begin{bmatrix} -2 & -2 & 4 \\ -2 & 4 & 4 \\ 1 & -2 & -5 \end{bmatrix}$ <p>System of equations can be written as <math>AX = B</math></p> <p>Where <math>A = \begin{bmatrix} 2 &amp; 3 &amp; 4 \\ 1 &amp; -1 &amp; 0 \\ 0 &amp; 1 &amp; 2 \end{bmatrix}</math>, <math>X = \begin{bmatrix} x \\ y \\ z \end{bmatrix}</math>, <math>B = \begin{bmatrix} 17 \\ 3 \\ 7 \end{bmatrix}</math></p> <p>Now <math>AX = B</math></p> $\Rightarrow X = A^{-1}B$ $\Rightarrow X = \frac{1}{-6} \begin{bmatrix} -2 & -2 & 4 \\ -2 & 4 & 4 \\ 1 & -2 & -5 \end{bmatrix} \begin{bmatrix} 17 \\ 3 \\ 7 \end{bmatrix}$	<p>1</p> <p>2</p> <p>1</p> <p><math>\frac{1}{2}</math></p>

	$\Rightarrow X = \frac{1}{-6} \begin{bmatrix} -34 - 6 + 28 \\ -34 + 12 + 28 \\ 17 - 6 - 35 \end{bmatrix}$ $\Rightarrow X = \frac{1}{-6} \begin{bmatrix} -12 \\ 6 \\ -24 \end{bmatrix}$ $\Rightarrow X = \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 2 \\ -1 \\ 4 \end{bmatrix}$ $\Rightarrow x = 2, \quad y = -1, \quad z = 4$	$1\frac{1}{2}$
34	<p> <math>x^2 + y^2 = 1</math>.....(1)  <math>x + y = 1</math>.....(2)                      solving (1) and(2)  <math>x^2 + (1 - x)^2 = 1</math>  <math>x^2 + x^2 - 2x + 1 = 1</math>  <math>2x^2 - 2x = 0</math>  <math>2x(x - 1) = 0</math>  <math>x = 0</math> or <math>x = 1</math> </p> <p>                     Required area = shaded area ACBDA                      = area(OACBO) – area(OADBO)  <math>= \int_0^1 (y_{circle} - y_{line}) dx</math>  <math>\int_0^1 \sqrt{1 - x^2} dx - \int_0^1 (1 - x) dx</math>  <math>= \left[ \frac{x\sqrt{1-x^2}}{2} + \frac{1}{2} \sin^{-1} x \right]_0^1 - \left[ x - \frac{x^2}{2} \right]_0^1</math>  <math>\left[ \left( 0 + \frac{1}{2} \cdot \frac{\pi}{2} \right) - 0 \right] - \left[ \left( 1 - \frac{1}{2} \right) \right]</math>  <math>\left( \frac{\pi}{4} - \frac{1}{2} \right)</math> square units                 </p>	<p>1</p> <p>1</p> <p>1</p> <p><math>1\frac{1}{2}</math></p> <p><math>1\frac{1}{2}</math></p>
35	<p>Let <math>r</math> be the radius and <math>h</math> be the height of half cylinder</p> <p>Volume <math>= \frac{1}{2} \pi r^2 h = V(\text{constant})</math>.....(1)</p>	$\frac{1}{2} (fig)$

	<div style="text-align: center;">  </div> <p>Total surface area of half cylinder is</p> $S = 2\left(\frac{1}{2}\pi r^2\right) + \pi r h + 2rh \dots\dots\dots(2)$ <p>From (1) put the value of <math>h</math> in (2)</p> $S = (\pi r^2) + \pi r \left(\frac{2V}{\pi r^2}\right) + 2r \left(\frac{2V}{\pi r^2}\right)$ $S = (\pi r^2) + \left(\frac{1}{r}\right) \left[\frac{4V}{\pi} + 2V\right]$ $\frac{ds}{dr} = (2\pi r) + \left(\frac{-1}{r^2}\right) \left[\frac{4V}{\pi} + 2V\right] \dots\dots\dots(3)$ <p>For maxima/minima <math>\frac{ds}{dr} = 0</math></p> $\Rightarrow (2\pi r) + \left(\frac{-1}{r^2}\right) \left[\frac{4V}{\pi} + 2V\right] = 0$ $\Rightarrow (2\pi r) = \left(\frac{1}{r^2}\right) \left[\frac{4V}{\pi} + 2V\pi\right]$ $\Rightarrow \pi r^3 = V \left[\frac{2 + \pi}{\pi}\right]$ $\Rightarrow V = \frac{\pi^2 r^3}{\pi + 2} \dots\dots\dots(4)$ <p>From (1) and (4)</p> $\Rightarrow \frac{1}{2} \pi r^2 h = \frac{\pi^2 r^3}{\pi + 2}$ $\Rightarrow \frac{h}{2r} = \frac{\pi}{\pi + 2}$ $\Rightarrow \text{height: diameter} = \pi : \pi + 2$ <p>Differentiating (3) with respect to <math>r</math></p> $\frac{d^2s}{dr^2} = (2\pi) + \left(\frac{2}{r^3}\right) \left[\frac{4V}{\pi} + 2V\right] = \text{positive (as all quantities are +ve)}$ <p>so <math>S</math> is minimum when</p> $\text{height: diameter} = \pi : \pi + 2$ <p>OR</p>	<p style="text-align: center;"><math>1 \frac{1}{2}</math></p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p>
	<p>Let <math>2r</math> be the base and <math>h</math> be the height of triangle, which is inscribed in a circle of radius <math>R</math></p> <p>Area of triangle = <math>\frac{1}{2}(\text{base})(\text{height})</math></p> $A = \frac{1}{2}(2r)(h) = rh \dots\dots\dots(1)$ <div style="text-align: center;">  </div> <p>Area being positive quantity, <math>A</math> will be maximum or minimum if <math>A^2</math> is</p>	<p style="text-align: center;">1</p> <p style="text-align: center;"><math>\frac{1}{2}(\text{fig})</math></p>

	<p>maximum or minimum.</p> $Z = A^2 = r^2 h^2 \dots \dots \dots (2)$ <p>Now In triangle OLB <math>BL^2 = OB^2 - OL^2</math>            In <math>\triangle OBD</math>  <math>Z = A^2 = r^2 h^2 \quad r^2 = R^2 - (h - R)^2 \Rightarrow r^2 = 2hR - h^2</math>  <math display="block">\text{put in (2)}</math> <math display="block">Z = h^2(2hR - h^2)</math> <math display="block">\Rightarrow Z = (2h^3R - h^4)</math> <math display="block">\Rightarrow \frac{dZ}{dh} = 6h^2R - 4h^3 \dots \dots \dots (3)</math> <p>For maxima/minima <math>\frac{dZ}{dh} = 0</math>  <math>\Rightarrow 6h^2R - 4h^3 = 0</math>  <math>\Rightarrow 6R = 4h(h \neq 0)</math></p> <math display="block">\Rightarrow h = \frac{3R}{2}</math> <p>differentiating (3) w.r.t. h  <math display="block">\Rightarrow \frac{d^2Z}{dh^2} = 12hR - 12h^2</math> <math display="block">\Rightarrow \left. \frac{d^2Z}{dh^2} \right _{h=\frac{3R}{2}} = 12\left(\frac{3R}{2}\right)R - 12\left(\frac{3R}{2}\right)^2</math> <math display="block">= 18R^2 - 27R^2 = -ve</math> <p>so <math>Z=A^2</math> is maximum when <math>h = \frac{3R}{2}</math>  <math>\Rightarrow A</math> is maximum when <math>h = \frac{3R}{2}</math>            when <math>h = \frac{3R}{2}, r^2 = 2hR - h^2 = 2R \cdot \frac{3R}{2} - \left(\frac{3R}{2}\right)^2</math>  <math display="block">r^2 = \frac{3R^2}{4}</math> <math display="block">r = \frac{\sqrt{3}R}{2}</math> <math display="block">\tan \theta = \frac{h}{r} = \frac{\frac{3R}{2}}{\frac{\sqrt{3}R}{2}} = \sqrt{3} \Rightarrow \theta = \frac{\pi}{3}</math> <p>Triangle ABC is equilateral triangle</p> </p></p></p>	<p style="text-align: center;"><math>\frac{1}{2}</math></p> <p style="text-align: center;">1</p>
36	<p>Let <math>P(x, y, z)</math> be any point on the plane in which <math>A(2, 1, 2)</math> and <math>B(4, -2, 1)</math> lie.  <math>\therefore \vec{AP}</math> and <math>\vec{AB}</math> lie on required plane.            Also required plane is perpendicular to given plane <math>\vec{r} \cdot (\hat{i} - 2\hat{k}) = 5</math>  <math>\therefore</math> normal to given plane <math>\vec{n}_1 = (\hat{i} - 2\hat{k})</math> lie on required plane.  <math>\Rightarrow \vec{AP}, \vec{AB}</math> and <math>\vec{n}_1</math> are coplanar.            Where <math>\vec{AP} = (x - 2)\hat{i} + (y - 1)\hat{j} + (z - 2)\hat{k}</math>  <math>\vec{AB} = 2\hat{i} - 3\hat{j} - \hat{k}</math>  <math>\Rightarrow</math> Scaler triple product <math>[\vec{AP} \quad \vec{AB} \quad \vec{n}_1] = 0</math></p>	<p style="text-align: center;">1</p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p>

$\Rightarrow \begin{vmatrix} x-2 & y-1 & z-2 \\ 2 & -3 & -1 \\ 1 & 0 & -2 \end{vmatrix} = 0$	
$\Rightarrow (x-2)(6-0) - (y-1)(-4+1) + (z-2)(0+3) = 0$	1
$\Rightarrow 6x - 12 + 3y - 3 + 3z - 6 = 0$	
$\Rightarrow 2x + y + z = 7 \dots\dots\dots(1)$	
Line passing through points $L(3,4,1)$ and $M(5,1,6)$ is	1
$\Rightarrow \frac{x-3}{2} = \frac{y-4}{-3} = \frac{z-1}{5} = \lambda \dots\dots\dots(2)$	
$\Rightarrow \text{General point on the line is } Q(2\lambda + 3, -3\lambda + 4, 5\lambda + 1)$	
As line (2) crosses plane (1) so point Q should satisfy equation(1)	
$\therefore 2(2\lambda + 3) + (-3\lambda + 4) + (5\lambda + 1) = 7$	
$4\lambda + 6 - 3\lambda + 4 + 5\lambda + 1 = 7$	
$6\lambda = -4$	1
$\lambda = -\frac{2}{3}$	
$Q\left(-\frac{4}{3} + 3, 2 + 4, -\frac{10}{3} + 1\right) = Q\left(\frac{5}{3}, 6, -\frac{7}{3}\right)$	

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