# Graduate Aptitude Test in Engineering 2021 

 Organising Institute - IIT BombayInstrumentation Engineering (IN)

## General Aptitude (GA)

Q. 1 - Q. 5 Multiple Choice Question (MCQ), carry ONE mark each (for each wrong answer: - 1/3).

| Q.1 | Getting to the top is___ than staying on top. |
| ---: | :--- |
| (A) | more easy |
| (B) | much easy |
| (C) | easiest |
| (D) | easier |


| $\begin{aligned} & \text { GATI } \\ & 2 \end{aligned}$ | Graduate Aptitude Test in Engineering 2021 Organising Institute - IIT Bombay |
| :---: | :---: |
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| Q. 2 | TRIANGLE <br> The mirror image of the above text about the $\mathbf{x}$-axis is |
| (A) | LВIVИФГЕ |
| (B) |  |
| (C) | LВIVNCГE |
| (D) | 」ВIVИСГヨ |


| Q.3 | In a company, 35\% of the employees drink coffee, $\mathbf{4 0 \%}$ of the employees <br> drink tea and $10 \%$ of the employees drink both tea and coffee. What \% of <br> employees drink neither tea nor coffee? |
| ---: | :--- |
| (A) | 15 |
| (B) | 25 |
| (C) | 35 |
| (D) | 40 |

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| Q.4 | $\oplus$ and $\odot$ are two operators on numbers $\boldsymbol{p}$ and $\boldsymbol{q}$ such that <br> $p \oplus q=\frac{p^{2}+q^{2}}{p q}$ and $\boldsymbol{p} \odot \boldsymbol{q}=\frac{p^{2}}{\boldsymbol{q}} ;$ <br>  <br> If $\boldsymbol{x} \oplus \boldsymbol{y}=\mathbf{2} \odot \mathbf{2}$, then $x=$ |
| :--- | :--- |
| (A) | $\frac{y}{2}$ |
| (B) | $y$ |
| (C) | $\frac{3 y}{2}$ |
| (D) | $2 y$ |


| Q.5 | Four persons $\mathbf{P}, \mathbf{Q}, \mathbf{R}$ and $S$ are to be seated in a row, all facing the same <br> direction, but not necessarily in the same order. P and $\mathbf{R}$ cannot sit adjacent <br> to each other. S should be seated to the right of $\mathbf{Q}$. The number of distinct <br> seating arrangements possible is: |
| :--- | :--- |
| (A) | 2 |
| (B) | 4 |
| (C) | 6 |
| (D) | 8 |

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Q. 6 - Q. 10 Multiple Choice Question (MCQ), carry TWO marks each (for each wrong answer: - 2/3).

| Q.6 | Statement: Either P marries Q or X marries Y <br> Among the options below, the logical NEGATION of the above statement is: |
| ---: | :--- |
| (A) | P does not marry Q and X marries Y. |
| (B) | Neither P marries Q nor X marries Y. |
| (C) | X does not marry Y and P marries Q. |
| (D) | P marries Q and X marries Y. |


| Q. 7 | Consider two rectangular sheets, Sheet $\mathbf{M}$ and Sheet $\mathbf{N}$ of dimensions $\mathbf{6} \mathbf{c m} \mathbf{x} \mathbf{4}$ <br> cm each. <br> Folding operation 1: The sheet is folded into half by joining the short edges of <br> the current shape. <br> Folding operation 2: The sheet is folded into half by joining the long edges of <br> the current shape. <br> Folding operation $\mathbf{1}$ is carried out on Sheet $\mathbf{M}$ three times. <br> Folding operation 2 is carried out on Sheet $\mathbf{N}$ three times. <br> The ratio of perimeters of the final folded shape of Sheet $\mathbf{N}$ to the final folded <br> shape of Sheet $\mathbf{M}$ is <br> (A) <br> $13: 7$ <br> (B) <br> (C) <br> (D:5 |
| :--- | :--- |
| (D) | $5: 13$ |


| Q. 8 |  |
| :--- | :--- |
| (A) | 36 |
| (B) | 45 |
| (C) | 72 |
| (Dive line segments of alue of $\theta$, in degrees, is | 108 |


| Q. 9 | A function, $\lambda$, is defined by |
| :--- | :--- |
| $\lambda(p, q)= \begin{cases}(p-q)^{2}, & \text { if } p \geq q, \\ p+q, & \text { if } p<q .\end{cases}$ |  |
| The value of the expression $\frac{\lambda(-(-3+2),(-2+3))}{(-(-2+1))}$ is: |  |
| (A) | -1 |
| (B) | 0 |
| (C) | $\frac{16}{3}$ |
| (D) | 16 |

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| Q.10 | Humans have the ability to construct worlds entirely in their minds, which <br> don't exist in the physical world. So far as we know, no other species possesses <br> this ability. This skill is so important that we have different words to refer to <br> its different flavors, such as imagination, invention and innovation. <br> Based on the above passage, which one of the following is TRUE? |
| ---: | :--- |
| (A) | No species possess the ability to construct worlds in their minds. |
| (B) | The terms imagination, invention and innovation refer to unrelated skills. |
| (C) | We do not know of any species other than humans who possess the ability to <br> construct mental worlds. |
| (D) | Imagination, invention and innovation are unrelated to the ability to construct <br> mental worlds. |

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Q. 1 - Q. 8 Multiple Choice Question (MCQ), carry ONE mark each (for each wrong answer: - 1/3).

| Q.1 | Consider the row vectors $\boldsymbol{v}=(\mathbf{1 , 0})$ and $\boldsymbol{w}=(\mathbf{2 , 0})$. The rank of the matrix <br> $\boldsymbol{M}=\mathbf{2} \boldsymbol{v}^{\boldsymbol{T}} \boldsymbol{v}+\mathbf{3} \boldsymbol{w}^{\boldsymbol{T}} \boldsymbol{w}$, where the superscript $\boldsymbol{T}$ denotes the transpose, is |
| :--- | :--- |
| (A) | 1 |
| (B) | 2 |
| (C) | 3 |
| (D) | 4 |


| Q.2 | Consider the sequence $x_{\boldsymbol{n}}=\mathbf{0 . 5} \boldsymbol{x}_{\boldsymbol{n - 1}}+1, n=1,2, \ldots \ldots$ with $\boldsymbol{x}_{\mathbf{0}}=\mathbf{0}$. Then <br> $\lim _{\boldsymbol{n}}$ is |
| ---: | :--- |
| (A) | 0 |
| (B) | 1 |
| (C) | 2 |
| (D) | $\infty$ |


| Q.3 | An infinitely long line, with uniform positive charge density, lies along the z- <br> axis. In cylindrical coordinates $(\boldsymbol{r}, \emptyset, \mathbf{z})$, at any point $\overrightarrow{\boldsymbol{P}}$ not on the z-axis, the <br> direction of the electric field is |
| :--- | :--- |
| (A) | $\hat{r}$ |
| (B) | $\widehat{\varnothing}$ |
| (C) | $\hat{z}$ |
| (D) | $\frac{(\hat{r}+\hat{z})}{\sqrt{2}}$ |

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| Q. 4 | The input-output relationship of an LTI system is given below. |
| :--- | :--- | :--- |
| For an input $x[n]$ shown below |  |
| (A) | 2 |
| (B) | 4 |
| (C) | 5 |
| (D) | 6 |

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| Q. 5 | In an ac main, the rms voltage $V_{a c}$, rms current $I_{a c}$ and power $W_{a c}$ are measured as: $\mathrm{V}_{\mathrm{ac}}=\mathbf{1 0 0} \mathrm{V} \pm \mathbf{1 \%}, \mathrm{I}_{\mathrm{ac}}=1 \mathrm{~A} \pm \mathbf{1 \%}$ and $\mathrm{W}_{\mathrm{ac}}=\mathbf{5 0} \mathrm{W} \pm \mathbf{2 \%}$ (errors are with respect to readings). The percentage error in calculating the power factor using these readings is |
| :---: | :---: |
| (A) | 1\% |
| (B) | $2 \%$ |
| (C) | 3\% |
| (D) | 4\% |


| Q.6 | Let $\boldsymbol{u}(\boldsymbol{t})$ denote the unit step function. The bilateral Laplace transform of <br> the function $\boldsymbol{f}(\boldsymbol{t})=\boldsymbol{e}^{\boldsymbol{t}} \boldsymbol{u}(-\boldsymbol{t})$ is <br> (A)$\frac{1}{s-1}$ with real part of $\mathrm{s}<1$ |
| :--- | :--- |
| (B) | $\frac{1}{s-1}$ with real part of $\mathrm{s}>1$ |
| (C) | $\frac{-1}{s-1}$ with real part of $\mathrm{s}<1$ |
| (D) | $\frac{-1}{s-1}$ with real part of $\mathrm{s}>1$ |


| Q. 7 | Input-output characteristic of a temperature sensor is exponential for a |
| ---: | :--- |
| (A) | Thermistor |
| (B) | Thermocouple |
| (C) | Resistive Temperature Device (RTD) |
| (D) | Mercury thermometer |

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| Q. $\mathbf{8}$ | The signal $\sin (\sqrt{\mathbf{2 \pi t}})$ is |
| ---: | :--- |
| (A) | periodic with period $T=\sqrt{2 \pi}$ |
| (B) | not periodic |
| (C) | periodic with period $T=2 \pi$ |
| (D) | periodic with period $T=4 \pi^{2}$ |

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Q. 9 - Q. 11 Multiple Select Question (MSQ), carry ONE mark each (no negative marks).

| Q.9 | The step response of a circuit is seen to have an oscillatory behaviour at the <br> output with oscillations dying down after some time. The correct inference(s) <br> regarding the transfer function from input to output is/are |
| ---: | :--- |
| (A) | that it is of at least second order. |
| (B) | that it has at least one pole-pair that is underdamped. |
| (C) | that it does not have a real pole. |
| (D) | that it is a first order system. |


| Q.10 | For a 4-bit Flash type Analog to Digital Convertor (ADC) with full scale <br> input voltage range "V", which of the following statement(s) is/are true? |
| :---: | :--- |
| (A) | The ADC requires 15 comparators. |
| (B) | The ADC requires one 4 to 2 priority encoder and 4 comparators. |
| (C) | A change in the input voltage by $\frac{V}{16}$ will always flip MSB of the output. |
| (D) | A change in the input voltage by $\frac{V}{16}$ will always flip the LSB of the output. |

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| Q. 11 | A 16-bit microprocessor has twenty address lines ( $\mathrm{A}_{0}$ to $\mathrm{A}_{19}$ ) and 16 data lines. The higher eight significant lines of the data bus of the processor are tied to the $\mathbf{8}$-data lines of a 16 Kbyte memory that can store one byte in each of its 16 K address locations. The memory chip should map onto contiguous memory locations and occupy only 16 Kbyte of memory space. Which of the following statement(s) is/are correct with respect to the above design? |
| :---: | :---: |
| (A) | If the 16 Kbyte of memory chip is mapped with a starting address of 80000 H , then the ending address will be 83FFFH. |
| (B) | The active high chip-select needed to map the 16 Kbyte memory with a starting address at F 0000 H is given by the logic expression $\left(\mathrm{A}_{19} \cdot \mathrm{~A}_{18} \cdot \mathrm{~A}_{17} \cdot \mathrm{~A}_{16}\right)$. |
| (C) | The 16 Kbyte memory cannot be mapped with contiguous address locations with a starting address as 0 F 000 H using only $\mathrm{A}_{19}$ to $\mathrm{A}_{14}$ for generating chip select. |
| (D) | The above chip cannot be interfaced as the width of the data bus of the processor and the memory chip differs. |

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Q. 12 - Q. 25 Numerical Answer Type (NAT), carry ONE mark each (no negative marks).
Q. 12 A single-phase transformer has a magnetizing inductance of $\mathbf{2 5 0} \mathbf{~ m H}$ and a core loss resistance of $\mathbf{3 0 0} \Omega$, referred to primary side. When excited with a $230 \mathrm{~V}, 50 \mathrm{~Hz}$ sinusoidal supply at the primary, the power factor of the input current drawn, with secondary on open circuit, is $\qquad$ (rounded off to two decimal places).
Q. 13 Taking $N$ as positive for clockwise encirclement, otherwise negative, the number of encirclements $N$ of $(-1,0)$ in the Nyquist plot of $G(s)=\frac{3}{s-1}$ is
$\qquad$ .
Q. 14 The diode used in the circuit has a fixed voltage drop of 0.6 V when forward biased. A signal $v_{s}$ is given to the ideal OpAmp as shown. When $v_{s}$ is at its positive peak, the output ( $v_{O A}$ ) of the OpAmp in volts is $\qquad$ .


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Q. 16 A $300 \mathrm{~V}, 5 \mathrm{~A}$, LPF wattmeter has a full scale of 300 W . The wattmeter can be used for loads supplied by 300 V ac mains with a maximum power factor of $\qquad$ (rounded off to one decimal place).
Q. 17 A 10-bit ADC has a full-scale of 10.230 V , when the digital output is ( 111111 1111)2. The quantization error of the ADC in millivolt is $\qquad$ .
Q. $18 \quad$ A strain gage having nominal resistance of $1000 \Omega$ has a gage factor of 2.5 . If the strain applied to the gage is $100 \mu \mathrm{~m} / \mathrm{m}$, its resistance in ohm will change to $\qquad$ (rounded off to two decimal places).
Q. 19 Given: Density of mercury is $13,600 \mathrm{~kg} / \mathrm{m}^{3}$ and acceleration due to gravity is $9.81 \mathrm{~m} / \mathrm{s}^{2}$. Atmospheric pressure is 101 kPa . In a mercury U-tube manometer, the difference between the heights of the liquid in the $\mathbf{U}$-tube is $1 \mathbf{~ c m}$. The differential pressure being measured in pascal is $\qquad$ (rounded off to the nearest integer).
Q. 20

A piezoresistive pressure sensor has a sensitivity of $1(\mathrm{mV} / \mathrm{V}) / \mathrm{kPa}$. The sensor is excited with a de supply of 10 V and the output is read using a $31 / 2$ digit 200 mV full-scale digital multimeter. The resolution of the measurement set-up, in pascal is $\qquad$ .

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## Q. 21 An amplitude modulation (AM) scheme uses tone modulation, with modulation index of 0.6 . The power efficiency of the AM scheme is <br> $\qquad$ \% (rounded off to one decimal place).

Q. 22 When the movable arm of a Michelson interferometer in vacuum $(n=1)$ is moved by $325 \mu \mathrm{~m}$, the number of fringe crossings is 1000 . The wavelength of the laser used in nanometers is $\qquad$ .
Q. 23 Consider the function $f(x)=-x^{2}+10 x+100$. The minimum value of the function in the interval $[5,10]$ is
Q. 24 Let $f(z)=\frac{1}{z^{2}+6 z+9}$ defined in the complex plane. The integral $\oint_{c} f(z) d z$ over the contour of a circle $\boldsymbol{c}$ with center at the origin and unit radius is
$\qquad$ .
Q. 25

The determinant of the matrix $M$ shown below is $\qquad$ .

$$
\mathrm{M}=\left[\begin{array}{llll}
1 & 2 & 0 & 0 \\
3 & 4 & 0 & 0 \\
0 & 0 & 4 & 3 \\
0 & 0 & 2 & 1
\end{array}\right]
$$

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Q. 26 - Q. 36 Multiple Choice Question (MCQ), carry TWO mark each (for each wrong answer: - 2/3).

| Q.26 | $\boldsymbol{f}(\mathbf{z})=(\mathbf{z}-\mathbf{1})^{\mathbf{- 1}}-\mathbf{1}+(\mathbf{z}-\mathbf{1})-(\mathbf{z}-\mathbf{1})^{\mathbf{2}}+\cdots$ is the series <br> expansion of |
| :--- | :--- |
| (A) | $\frac{-1}{z(z-1)}$ for $\|z-1\|<1$ |
| (B) $\frac{1}{z(z-1)}$ for $\|z-1\|<1$ |  |
| (C) $\frac{1}{(z-1)^{2}}$ for $\|z-1\|<1$ |  |
| (D) $\frac{-1}{(z-1)}$ for $\|z-1\|<1$ |  |


| Q.27 | A single-phase transformer has maximum efficiency of $\mathbf{9 8} \%$. The core losses <br> are 80 W and the equivalent winding resistance as seen from the primary <br> side is $\mathbf{0 . 5} \mathbf{\Omega}$. The rated current on the primary side is $\mathbf{2 5} \mathrm{A}$. The percentage <br> of the rated input current at which the maximum efficiency occurs is |
| ---: | :--- |
| (A) | $35.7 \%$ |
| (B) | $50.6 \%$ |
| (C) | $80.5 \%$ |
| (D) | $100 \%$ |


| Q.28 | A slip-ring induction motor is expected to be started by adding extra <br> resistance in the rotor circuit. The benefit that is derived by adding extra <br> resistance in the rotor circuit in comparison to the rotor being shorted is |
| ---: | :--- |
| (A) | The starting torque would be higher. |
| (B) | The power factor at start will be lower. |
| (C) | The starting current is higher. |
| (D) | The losses at starting would be lower. |

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| Q.29 | Consider a unity feedback configuration with a plant and a PID controller <br> as shown in the figure. $\boldsymbol{G}(\boldsymbol{s})=\frac{1}{(\boldsymbol{s}+1)(\boldsymbol{s + 3})}$ and $\boldsymbol{C}(\boldsymbol{s})=\boldsymbol{K} \frac{(\boldsymbol{s}+3-\boldsymbol{j})(\boldsymbol{s}+3+\boldsymbol{j})}{\boldsymbol{s}}$ <br> with $K$ being scalar. The closed lop is |
| :--- | :--- | :--- |
| (A) only stable for $K>0$ |  |
| (B) | only stable for $K$ between -1 and +1 |
| (C) | only stable for $K<0$ |
| (D) | stable for all values of $K$ |

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| Q. 30 | The output $\mathrm{V}_{0}$ of the ideal OpAmp used in the circuit shown below is 5 V . <br> Then the value of resistor $\mathrm{R}_{\mathrm{L}}$ in kilo ohm $(\mathrm{k} \Omega)$ is |
| :--- | :--- |
| (A) 2.5 |  |
| (B) 5 |  |
| (C) 25 |  |
| (D) 50 |  |


| Q.31 | A Boolean function $\mathbf{F}$ of three variables $\mathbf{X}, \mathbf{Y}$, and $\mathbf{Z}$ is given as <br> $\mathbf{F}(\mathbf{X}, \mathbf{Y}, \mathbf{Z})=\left(\mathbf{X}^{\prime}+\mathbf{Y}+\mathbf{Z}\right) \cdot\left(\mathbf{X}+\mathbf{Y}^{\prime}+\mathbf{Z}^{\prime}\right) \cdot\left(\mathbf{X}^{\prime}+\mathbf{Y}+\mathbf{Z}^{\prime}\right) \cdot\left(\mathbf{X}^{\prime} \mathbf{Y}^{\prime} \mathbf{Z}^{\prime}+\mathbf{X}^{\prime} \mathbf{Y} \mathbf{Z}^{\prime}+\mathbf{X} \mathbf{Y}\right.$ <br> $\left.\mathbf{Z}^{\prime}\right)$ <br> Which one of the following is true? |
| ---: | :--- |
| (A) | $\mathrm{F}(\mathrm{X}, \mathrm{Y}, \mathrm{Z})=\left(\mathrm{X}+\mathrm{Y}+\mathrm{Z}^{\prime}\right) \cdot\left(\mathrm{X}^{\prime}+\mathrm{Y}^{\prime}+\mathrm{Z}^{\prime}\right)$ |
| (B) | $\mathrm{F}(\mathrm{X}, \mathrm{Y}, \mathrm{Z})=\left(\mathrm{X}^{\prime}+\mathrm{Y}\right) \cdot\left(\mathrm{X}+\mathrm{Y}^{\prime}+\mathrm{Z}^{\prime}\right)$ |
| (C) | $\mathrm{F}(\mathrm{X}, \mathrm{Y}, \mathrm{Z})=\mathrm{X}^{\prime} \mathrm{Z}^{\prime}+\mathrm{Y} \mathrm{Z}^{\prime}$ |
| (D) | $\mathrm{F}(\mathrm{X}, \mathrm{Y}, \mathrm{Z})=\mathrm{X}^{\prime} \mathrm{Y}^{\prime} \mathrm{Z}+\mathrm{X} Y \mathrm{Z}$ |

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| Q. 32 | A 10 $1 / 2$ digit Counter-timer is set in the 'frequency mode' of operation (with <br> $\boldsymbol{T}_{s}=1 \mathrm{~s}$ ). For a specific input, the reading obtained is 1000. Without <br> disconnecting this input, the Counter-timer is changed to operate in the <br> 'Period mode' and the range selected is microseconds ( $\mu \mathrm{s}$, with $\boldsymbol{f}_{s}=\mathbf{1} \mathrm{MHz}$ ). <br> The counter will then display |
| :--- | :--- |
| (A) | 0 |
| (B) | 10 |
| (C) | 100 |
| (D) 1000 |  |


| Q. 33 | A J-type thermocouple has an output voltage $V_{\theta}=\left(\mathbf{1 3 6 5 0}+\mathbf{5 0} \theta_{x}\right) \boldsymbol{\mu} \mathrm{V}$, where $\theta_{x}$ is the junction temperature in Celsius $\left({ }^{\circ} \mathrm{C}\right)$. The thermocouple is used with reference junction compensation, as shown in the figure. The Instrumentation amplifier used has a gain $\mathbf{G}=\mathbf{2 0}$. If $\boldsymbol{\theta}_{\text {Ref }}$ is $1^{\circ} \mathrm{C}$, for an input $\theta_{x}$ of $100^{\circ} \mathrm{C}$, the output $V_{o}$ of the instrumentation amplifier in millivolt is |
| :---: | :---: |
| (A) | 98 mV |
| (B) | 99 mV |
| (C) | 100 mV |
| (D) | 101 mV |

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| Q. 34 | A laser pulse is sent from ground level to the bottom of a concrete water tank at normal incidence. The tank is filled with water up to 2 m below the ground level. The reflected pulse from the bottom of the tank travels back and hits the detector. The round-trip time elapsed between sending the laser pulse, the pulse hitting the bottom of the tank, reflecting back and sensed by the detector is $\mathbf{1 0 0} \mathbf{n s}$. The depth of the tank from ground level marked as $x$ in metre is $\qquad$ . <br> (Refractive index of water $n_{\text {water }}=1.3$ and velocity of light in air $\mathrm{c}_{\text {air }}=\mathbf{3} \times \mathbf{1 0}^{\mathbf{8}} \mathbf{m} / \mathrm{s}$ ) |
| :---: | :---: |
| (A) | 9 |
| (B) | 10 |
| (C) | 11 |
| (D) | 12 |

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| Q. 35 | A $4 \times 1$ multiplexer with two selector lines is used to realize a Boolean function $F$ having four Boolean variables $X, Y, Z$ and $W$ as shown below. $S_{0}$ and $S_{1}$ denote the least significant bit (LSB) and most significant bit (MSB) of the selector lines of the multiplexer respectively. $I_{0}, I_{1}, I_{2}, I_{3}$ are the input lines of the multiplexer. <br> The canonical sum of product representation of $F$ is |
| :---: | :---: |
| (A) | $\mathrm{F}(\mathrm{X}, \mathrm{Y}, \mathrm{Z}, \mathrm{W})=\Sigma \mathrm{m}(0,1,3,14,15)$ |
| (B) | $\mathrm{F}(\mathrm{X}, \mathrm{Y}, \mathrm{Z}, \mathrm{W})=\Sigma \mathrm{m}(0,1,3,11,14)$ |
| (C) | $\mathrm{F}(\mathrm{X}, \mathrm{Y}, \mathrm{Z}, \mathrm{W})=\Sigma \mathrm{m}(2,5,9,11,14)$ |
| (D) | $\mathrm{F}(\mathrm{X}, \mathrm{Y}, \mathrm{Z}, \mathrm{W})=\Sigma \mathrm{m}(1,3,7,9,15)$ |

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| Q. 36 | Given below is the diagram of a synchronous sequential circuit with one J-K flip-flop and one T flip-flop with their outputs denoted as $\mathbf{A}$ and $\mathbf{B}$ respectively, with $J_{A}=\left(A^{\prime}+B^{\prime}\right), K_{A}=(A+B)$, and $T_{B}=A$. <br> Starting from the initial state $(A B=00)$, the sequence of states $(A B)$ visited by the circuit is |
| :---: | :---: |
| (A) | $00 \rightarrow 01 \rightarrow 10 \rightarrow 11 \rightarrow 00 \ldots$ |
| (B) | $00 \rightarrow 10 \rightarrow 01 \rightarrow 11 \rightarrow 00 \ldots$ |
| (C) | $00 \rightarrow 10 \rightarrow 11 \rightarrow 01 \rightarrow 00 \ldots$ |
| (D) | $00 \rightarrow 01 \rightarrow 11 \rightarrow 00 \ldots$ |

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Q. 37 - Q. 55 Numerical Answer Type (NAT), carry TWO mark each (no negative marks).
Q. 37 Consider that $X$ and $Y$ are independent continuous valued random variables with uniform PDF given by $X \sim U(2,3)$ and $Y \sim U(1,4)$. Then $P(Y \leq X)$ is equal to $\qquad$ (rounded off to two decimal places).
Q. 38 Given $A=\left(\begin{array}{ll}2 & 5 \\ 0 & 3\end{array}\right)$. The value of the determinant $\left|A^{4}-5 A^{3}+6 A^{2}+2 I\right|=$


When the bar has moved by 1 m , its speed in metre per second is $\qquad$ (rounded off to one decimal place).
Q. 40 A toroid made of CRGO has an inner diameter of $\mathbf{1 0} \mathbf{~ c m}$ and an outer diameter of 14 cm . The thickness of the toroid is 2 cm .200 turns of copper wire is wound on the core. $\mu_{0}=4 \pi \times 10^{-7} \mathrm{H} / \mathrm{m}$ and $\mu_{\mathrm{R}}$ of CRGO is 3000 . When a current of 5 mA flows through the winding, the flux density in the core in millitesla is $\qquad$ .

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Q. 41 An air cored coil having a winding resistance of $10 \Omega$ is connected in series with a variable capacitor $C_{x}$. The series circuit is excited by a 10 V sinusoidal voltage source of angular frequency $1000 \mathrm{rad} / \mathrm{s}$. As the value of the capacitor is varied, a maximum voltage of 30 V was observed across it. Neglecting skineffect, the value of the inductance of the coil in millihenry is $\qquad$ .
Q. 42 A household fan consumes 60 W and draws a current of 0.3125 A (rms) when connected to a 230 V (rms) ac, 50 Hz single phase mains. The reactive power drawn by the fan in VAr is $\qquad$ (rounded off to the nearest integer).
Q. 43 Given $\boldsymbol{y}(t)=\boldsymbol{e}^{-3 t} u(t) * u(t+3)$, where * denotes convolution operation. The value of $y(t)$ as $t \rightarrow \infty$ is $\qquad$ (rounded off to two decimal places).


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Q. 45 A sinusoid $(\sqrt{2} \sin t) \mu(t)$, where $\mu(t)$ is the step input, is applied to a system with transfer-function $G(s)=\frac{1}{s+1}$. The amplitude of the steady state output is $\qquad$ .
Q. 46 Consider a system with transfer-function $G(s)=\frac{2}{s+1}$. A unit step function $\mu(t)$ is applied to the system, which results in an output $y(t)$. If $e(t)=y(t)-\mu(t)$, then $\lim _{t \rightarrow \infty} e(t)$ is $\qquad$ .


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| Q. 50 | A 31/2 digit, rectifier type digital meter is set to read in its 2000 V range. A <br> symmetrical square wave of frequency 50 Hz and amplitude $\pm 100 \mathrm{~V}$ is <br> measured using the meter. The meter will read$..$ |
| :--- | :--- |

Q. 51 A bar primary current transformer of rating $1000 / 1 \mathrm{~A}, \mathbf{5 V A}$, UPF has 995 secondary turns. It exhibits zero ratio error and phase error of $\mathbf{3 0}$ minutes at 1000 A with rated burden. The watt loss component of the primary excitation current in ampere is $\qquad$ (rounded off to one decimal place).

| Q. 52 | In the bridge circuit shown, the voltmeter V showed zero when the value of the resistors are: $R_{1}=100 \Omega, R_{2}=110 \Omega$, and $R_{3}=90 \Omega$. If $\left(R_{1} / R_{2}\right)=\left(R_{A} / R_{B}\right)$, the value of $R_{4}$ in ohm is $\qquad$ . |
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Q. 54 A signal having a bandwidth of 5 MHz is transmitted using the Pulse code modulation (PCM) scheme as follows. The signal is sampled at a rate of $\mathbf{5 0 \%}$ above the Nyquist rate and quantized into 256 levels. The binary pulse rate of the PCM signal in Mbits per second is $\qquad$ .

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END OF THE QUESTION PAPER

