Graduate Aptitude Test in Engineering 2021 Organising Institute - IIT Bombay

Production \& Industrial Engineering (PI)

## General Aptitude (GA)

Q. 1 - Q. 5 Multiple Choice Question (MCQ), carry ONE mark each (for each wrong answer: - 1/3).

| Q. 1 | The current population of a city is $\mathbf{1 1 , 0 2 , 5 0 0 . \text { If it has been increasing at the }}$ <br> rate of $\mathbf{5 \%}$ per annum, what was its population $\mathbf{2}$ years ago? |
| :--- | :--- |
| (A) | $9,92,500$ |
| (B) | $9,95,006$ |
| (C) | $10,00,000$ |
| (D) | $12,51,506$ |


| Q. 2 | $\boldsymbol{p}$ and $\boldsymbol{q}$ are positive integers and $\frac{p}{q}+\frac{q}{p}=3$, |
| :--- | :--- |
|  | then, $\frac{p^{2}}{q^{2}}+\frac{q^{2}}{p^{2}}=$ |
| (A) | 3 |
| (B) | 7 |
| (C) | 9 |
| (D) | 11 |

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| Q. 3 |  |
| :--- | :--- |
| The least number of squares that must be added so that the line P-Q |  |
| becomes the line of symmetry is |  |
| (A) | 4 |
| (B) | 3 |
| (C) | 6 |
| (D) | 7 |

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| Q.4 | Nostalgia is to anticipation as___ is to ___ maintains a similar logical relation in the <br> Which one of the following options mater <br> above sentence? |
| :--- | :--- |
| (A) | Present, past |
| (B) | Future, past |
| (C) | Past, future |
| (D) | Future, present |

$\left.\begin{array}{|l|l|}\hline \text { Q.5 } & \begin{array}{l}\text { Consider the following sentences: } \\ \text { (i) } \\ \text { (ii) }\end{array} \\ \text { I woke up from sleep. } \\ \text { (iii) } & \text { I woked up from sleep. } \\ \text { (iv) } & \text { I was woken up from sleep. } \\ \text { Which of the above sentences are grammatically CORRECT? }\end{array}\right]$

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Q. 6 - Q. 10 Multiple Choice Question (MCQ), carry TWO marks each (for each wrong answer: - 2/3).

| Q.6 | Given below are two statements and two conclusions. <br> Statement 1: All purple are green. <br> Statement 2: All black are green. <br> Conclusion I: Some black are purple. <br> Conclusion II: No black is purple. <br> Based on the above statements and conclusions, which one of the following <br> options is logically CORRECT? |
| ---: | :--- |
| (A) | Only conclusion I is correct. |
| (B) | Only conclusion II is correct. |
| (C) | Either conclusion I or II is correct. |
| (D) | Both conclusion I and II are correct. |


| Q.7 | Computers are ubiquitous. They are used to improve efficiency in almost all <br> fields from agriculture to space exploration. Artificial intelligence (AI) is <br> currently a hot topic. AI enables computers to learn, given enough training <br> data. For humans, sitting in front of a computer for long hours can lead to <br> health issues. <br> Which of the following can be deduced from the above passage? <br> (i) |
| :--- | :--- |
| (ii)Nowadays, computers are present in almost all places. <br> Computers cannot be used for solving problems in engineering. <br> (iii) <br> For humans, there are both positive and negative effects of using <br> computers. <br> (iv) <br> (ifticial intelligence can be done without data. |  |
| (A) | (ii) and (iii) |
| (B) | (ii) and (iv) |
| (C) | (i), (iii) and (iv) |
| (D) | (i) and (iii) |

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| Q. 8 | Consider a square sheet of side 1 unit. In the first step, it is cut along the main <br> diagonal to get two triangles. In the next step, one of the cut triangles is <br> revolved about its short edge to form a solid cone. The volume of the resulting <br> cone, in cubic units, is |
| :--- | :--- |
| (A) | $\frac{\pi}{3}$ |
| (B) | $\frac{2 \pi}{3}$ |
| (C) | $\frac{3 \pi}{2}$ |
| (D) | $3 \pi$ |

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| Q. 10 |
| :--- | :--- |
| Corners are cut from an equilateral triangle to produce a regular convex |
| hexagon as shown in the figure above. |
| The ratio of the area of the regular convex hexagon to the area of the original |
| equilateral triangle is | (A) $2: 3$

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## Production \& Industrial Engineering (PI)

Q. 1 - Q. 17 Multiple Choice Question (MCQ), carry ONE mark each (for each wrong answer: - 1/3).

| Q.1 | A product has an exponential time-to-failure distribution with a constant <br> failure rate of 0.00006 per hour. The reliability of the product after 4000 <br> hours of operation is |
| :--- | :--- |
| (A) | 0.5866 |
| (B) | 0.6866 |
| (C) | 0.7866 |
| (D) | 0.8866 |


| Q.2 | In a typical product development process under concurrent engineering <br> approach, all elements of product life cycle from conception to disposal are <br> considered at |
| :--- | :--- |
| (A) | Product design stage |
| (B) | Process design stage |
| (C) | Manufacturing stage |
| (D) | Disposal stage |


| Q.3 | When acceptance number of a single sampling plan under attribute category <br> is zero with sample size less than or equal to 10, the Operating Characteristic <br> (OC) curve is |
| ---: | :--- |
| (A) | A horizontal line |
| (B) | A vertical line |
| (C) | A convex function |
| (D) | An inverted S-shaped curve |

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| Q.4 | Which one of the following is an improvement type heuristic algorithm for <br> computerized layout design technique? |
| ---: | :--- |
| (A) | Systematic layout planning (SLP) |
| (B) | Computerized relative allocation of facilities technique (CRAFT) |
| (C) | Computerized relationship layout planning (CORELAP) |
| (D) | Plant layout analysis and evaluation technique (PLANET) |


| Q. 5 | Which one of the following is NOT a measure of forecast error? |
| ---: | :--- |
| (A) | Mean absolute deviation (MAD) |
| (B) | Mean squared error (MSE) |
| (C) | Mean absolute percent error (MAPE) |
| (D) | Mean sum product error (MSPE) |


| Q.6 | Pearlite microstructure in an eutectoid steel consists of alternating layers of <br> two phases, namely $\boldsymbol{\alpha}$ ferrite and |
| ---: | :--- |
| (A) | Martensite |
| (B) | Austenite |
| (C) | Cementite |
| (D) | Bainite |

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| Q. 7 | Which one of the following defects is NOT associated with welding <br> processes? |
| ---: | :--- |
| (A) | Angular distortion |
| (B) | Hot tear |
| (C) | Hydrogen embrittlement |
| (D) | Earring |


| Q. 8 | Match the component with the corresponding manufacturing process in the table below. |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Component | Manufacturing process |  |
|  | P | Aluminum alloy piston for IC engine | 1 | Blow molding |
|  | Q | Low carbon steel oil pan | 2 | Powder metallurgy |
|  | R | Tungsten carbide cutting tool insert | 3 | Sand casting |
|  | S | Plastic bottle | 4 | Deep drawing |
| (A) | P-3, Q-2, R-1, S-4 |  |  |  |
| (B) | P-3, Q-4, R-2, S-1 |  |  |  |
| (C) | P-2, Q-3, R-4, S-1 |  |  |  |
| (D) | P-1, Q-3, R-2, S-4 |  |  |  |

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| Q. 9 | In a turning operation, doubling the cutting speed $(\boldsymbol{V})$ reduces the tool life <br> $(\boldsymbol{T})$ to $\mathbf{1} / \mathbf{8}$ <br> equation, $\boldsymbol{V} \boldsymbol{T}^{\boldsymbol{n}}=\boldsymbol{C}$ the is |
| :--- | :--- |
| (A) | $\frac{1}{2}$ |
| (B) | $\frac{1}{3}$ |
| (C) | $\frac{1}{4}$ |
| (D) | $\frac{1}{8}$ |


| Q.10 | Which one among the following mechanisms is NOT used for transforming <br> rotation to translation in machine tools? |
| ---: | :--- |
| (A) | Screw-nut system |
| (B) | 4-bevel gear type differential mechanism |
| (C) | Cam and cam follower system |
| (D) | Whitworth mechanism |

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| Q. 11 | Match the measuring feature with the corresponding measuring instrument in the table below. |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Measuring feature |  | Measuring instrument |
|  | P | Flatness error of a surface plate | 1 | Auto collimator |
|  | Q | Profile of a cam | 2 | Tool maker's microscope |
|  | R | Alignment error of a machine tool slide way | 3 | Dividing head and dial gauge |
|  | S | Pitch and angle errors of screw thread | 4 | Optical interferometer |
| (A) | P-4, Q-1, R-2, S-3 |  |  |  |
| (B) | P-1, Q-3, R-4, S-2 |  |  |  |
| (C) | $\mathrm{P}-2, \mathrm{Q}-4, \mathrm{R}-3, \mathrm{~S}-1$ |  |  |  |
| (D) | P-4, Q-3, R-1, S-2 |  |  |  |


| Q.12 | The frequency of pulsing in a die-sinking electric discharge machine (EDM) <br> is 10 kHz . The pulse off-time is set at 40 micro-seconds. The duty factor at <br> this setting is |
| ---: | :--- |
| (A) | 0.40 |
| (B) | 0.60 |
| (C) | 0.67 |
| (D) | 2.50 |

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| Q. 13 | A cantilever beam of length 0.3 m is subjected to a uniformly distributed load $C=10 \mathrm{kN} / \mathrm{m}$, as shown in the figure. The bending (flexural) rigidity of the beam is $5000 \mathrm{Nm}^{2}$. Neglecting the self-weight of the beam, the magnitude of beam curvature in $\mathrm{m}^{-1}$ at the fixed end is |
| :---: | :---: |
| (A) | 1.10 |
| (B) | 0.02 |
| (C) | 0.09 |
| (D) | 0.05 |

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| Q. 14 | A circular rod of length $l=2 \mathrm{~m}$ is subjected to a compressive load $\boldsymbol{P}$, as shown <br> in the figure. The bending (flexural) rigidity of the rod is 2000 $\mathbf{N m}^{2}$. If both <br> ends are pinned, then the critical load $\boldsymbol{P}$ cr in $\mathbf{N}$ (rounded to the nearest <br> integer) at which the rod buckles elastically is |
| :--- | :--- |
| (A) | 493 |
| (B) | 2000 |
| (C) | 5167 |
| (D) | 1238 |

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| Q. 15 | Two cylindrical parts of equal length $l$, as shown in the figure, made of steel having Young's modulus $E=200 \mathrm{GPa}$ and Poisson's ratio $\nu=0.33$ are press fitted upon one another. If radial interference $\boldsymbol{\delta}=\mathbf{0 . 0 5} \mathbf{~ m m}$, and radii $\boldsymbol{R}=\mathbf{2 5}$ mm and $R_{0}=40 \mathrm{~mm}$, then the contact pressure $P$ in MPa at the interface upon press fit is |
| :---: | :---: |
| (A) | 10.7 |
| (B) | 60.9 |
| (C) | 121.9 |
| (D) | 1005.3 |


| Q.16 | The dimensionless number defined by the ratio of inertial force to viscous <br> force is called |
| ---: | :--- |
| (A) | Mach number |
| (B) | Froude number |
| (C) | Weber number |
| (D) | Reynolds number |

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| Q.17 | A small capillary tube of $\mathbf{3} \mathbf{~ m m}$ inner diameter is inserted into a fluid having <br> density $900 \mathrm{~kg} / \mathbf{m}^{\mathbf{3}}$, surface tension $\mathbf{0 . 1} \mathbf{N} / \mathbf{m}$, and contact angle $\mathbf{3 0} 0^{\circ}$. The rise <br> in the height of fluid in the capillary tube due to surface tension is |
| ---: | :--- |
| (A) | 111.4 mm |
| (B) | 128.3 mm |
| (C) | 89.1 mm |
| (D) | 154.1 mm |

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Q. 18 - Q. 25 Numerical Answer Type (NAT), carry ONE mark each (no negative marks).
Q. 18 A given steel has identical yield strength of 700 MPa in uni-axial tension and uni-axial compression. If the steel is subjected to pure shear stress such that the three principal stresses are $\sigma_{1}=\sigma, \sigma_{2}=0, \sigma_{3}=-\sigma$ with $\sigma_{1} \geq \sigma_{2} \geq \sigma_{3}$, then the stress $\sigma$ in MPa for the initiation of plastic yielding in the steel as per von Mises yield criterion is $\qquad$ . [round off to 2 decimal places]
Q. 19 A cylindrical mild steel tensile test specimen of gauge length 50 mm and diameter 10 mm is extended in two stages at a deformation speed of 4 $\mathrm{mm} / \mathrm{min}$. The specimen is extended from 50 mm to 55 mm in the first stage, and from 55 mm to 60 mm in the second stage. Neglecting elastic deformation, the total longitudinal true strain is $\qquad$ - [round off to 2 decimal places]

| Q. 20 | A M30 bolt needs to be subjected to pretension $F_{\mathrm{i}}=350 \mathrm{kN}$. If the torque <br> coefficient $K$ of the bolt is 0.2, then the torque in Nm needed to achieve this <br> pretension is |
| :--- | :--- |

Q. 21 A $\mathbf{1 5 0 ~ m m}$ wide polyamide flat belt is transmitting 15 kW power through a belt-pulley system. The driving pulley of 150 mm pitch diameter is rotating at 200 RPM. If $F_{1}$ is the belt tension on high tension side, and $F_{2}$ is the belt tension on low tension side, then the difference in belt tensions $\Delta F=F_{1}-F_{2}$ in N is $\qquad$ . [round off to one decimal place]

Heat is being removed from a refrigerator at a rate of $300 \mathrm{~kJ} / \mathbf{m i n}$ to maintain its inside temperature at $2^{\circ} \mathrm{C}$. If the input power to the refrigerator is $\mathbf{2} \mathbf{~ k W}$, the coefficient of performance of the refrigerator is $\qquad$ . [round off to one decimal place]

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| Q. 23 | In an ideal Otto cycle, $800 \mathrm{~kJ} / \mathrm{kg}$ is transferred to air during the constant <br> volume heat addition process and $381 \mathrm{~kJ} / \mathrm{kg}$ is removed during the constant <br> volume heat rejection process. The thermal efficiency in \% of the cycle is |
| :--- | :--- |
| [round off to one decimal place $]$ |  |

Q. 24 If $(3 i+1) x+(4 i+4) y+5=0$ with $x, y$ being real and $i=\sqrt{-1}$, then $x=$
$\qquad$ . [correct up to one decimal place]
Q. 25 The minimum value of function $f$ defined by

$$
f(x, y, z)=x^{2}+5 y^{2}+5 z^{2}-4 x+40 y-40 z+300
$$

is $\qquad$ . [in integer]

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Q. 26 - Q. 36 Multiple Choice Question (MCQ), carry TWO mark each (for each wrong answer: - 2/3).

| Q. 26 | For a given process control chart, there are four rules for determining out- <br> of-control state of the process which are being used simultaneously. The <br> probability of Type-I error for the four rules are 0.005, 0.02, 0.03, and 0.05. <br> Assuming independence of the rules, the probability of overall Type-I error <br> when all the four rules are used simultaneously is |
| :--- | :--- |
| (A) | 0.101 |
| (B) | 0.201 |
| (C) | 0.001 |
| (D) | 0.301 |


| Q.27 | An in-control process has an estimated standard deviation of $\mathbf{2} \mathbf{~ m m}$. The <br> specification limits of the component being processed are $120 \pm 8 \mathrm{~mm}$. When <br> the process mean shifts to 118 mm, the values of the process capability <br> indices, $\mathrm{C}_{\mathbf{p}}$ and $\mathrm{C}_{\mathbf{p k}}$, respectively are, |
| ---: | :--- |
| (A) | $1.000,1.667$ |
| (B) | $1.333,1.667$ |
| (C) | $1.333,1.000$ |
| (D) | $1.000,1.000$ |


| Q. 28 | There are a number of identical components in a parallel system. When the <br> system reliability is $\mathbf{0 . 9 7}$ and the reliability of each individual component is <br> $\mathbf{0 . 6 8 ,}$, the number of identical components in the system is (if actual value is <br> a fraction, it may be rounded up to the next higher integer). |
| ---: | :--- |
| (A) | 2 |
| (B) | 4 |
| (C) | 6 |
| (D) | 8 |

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| Q. 29 | A retail chain company has identified four sites A, B, C and D to open a new retail store. The company has selected four factors as the basis for evaluation of these sites. The factors, their weights, and the score for each site are given in the following table. |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Factor | Factor weight | Score for site (out of 100) |  |  |  |
|  |  |  | A | B | C | D |
|  | Average community income | 0.4 | 60 | 70 | 80 | 50 |
|  | Demand growth potential | 0.1 | 30 | 80 | 50 | 40 |
|  | Proximity to existing store | 0.3 | 50 | 10 | 40 | 60 |
|  | Availability of public transport | 0.2 | 40 | 30 | 40 | 20 |
|  | The site that should be selected to open the new retail store is |  |  |  |  |  |
| (A) | Site A |  |  |  |  |  |
| (B) | Site B |  |  |  |  |  |
| (C) | Site C |  |  |  |  |  |
| (D) | Site D |  |  |  |  |  |


| Q.30 | In the classical economic order quantity (EOQ) model, let $\boldsymbol{Q}$ and $\boldsymbol{C}$ denote <br> the optimal order quantity and the corresponding minimum total annual <br> cost (the sum of the inventory holding and ordering costs). If the order <br> quantity is estimated incorrectly as $\boldsymbol{Q}^{\prime}=\mathbf{2 Q}$, then the corresponding total <br> annual cost $\boldsymbol{C}^{\prime}$ is |
| :--- | :--- |
| (A) | $C^{\prime}=1.25 C$ |
| (B) | $C^{\prime}=1.5 C$ |
| (C) | $C^{\prime}=1.75 C$ |
| (D) | $C^{\prime}=2 C$ |

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| Q.31 | The eigenvalues of matrix $\mathbf{A}=\left[\begin{array}{rr}\mathbf{8} & \mathbf{3} \\ \mathbf{2} & \mathbf{7}\end{array}\right]$ are $\mathbf{5}$ and $\mathbf{1 0 .}$. For matrix $\mathbf{B}=\mathbf{A}+\boldsymbol{\alpha} \mathbf{I}$, <br> where $\boldsymbol{\alpha}$ is a constant and $\mathbf{I}$ is $\mathbf{2 \times 2}$ identity matrix, its eigenvalues are |
| ---: | :--- |
| (A) | 5,10 |
| (B) | $5+\alpha, 10+\alpha$ |
| (C) | $5-\alpha, 10-\alpha$ |
| (D) | $5 \alpha, 10 \alpha$ |


| Q. 32 | A company manufactures two products $P$ and $Q$ with unit profit of 4 and 5, respectively. The production requires manpower and two kinds of raw materials R1 and R2. The following table summarizes the requirement and availability of resources. |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Resource | Resou of | per unit ion | Amount of resource availabl |
|  |  | P | Q |  |
|  | manpower | 1 | 1 | 10 |
|  | R1 | 1 | 2 | 18 |
|  | R2 | 2 | 1 | 18 |
|  | The maximum profit the company can make is |  |  |  |
| (A) | 45 |  |  |  |
| (B) | 48 |  |  |  |
| (C) | 42 |  |  |  |
| (D) | 54 |  |  |  |

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| Q.33 | A tool of an NC machine has to move along a circular arc from (20,20) to <br> $\left(\begin{array}{ll\|l\|}\text { (10,10), while performing an operation. The center of the arc is at (20,10). } \\ \text { Which one of the following NC tool commands performs the above } \\ \text { mentioned operation? }\end{array}\right.$ <br> (A) N020 G03 X20 Y20 X10 Y10 R10 |
| ---: | :--- |
| (B) | N020 G02 X20 Y20 X10 Y10 R10 |
| (C) | N020 G02 X10 Y10 X20 Y20 R10 |
| (D) | N020 G01 X20 Y20 X10 Y10 R10 |


| Q.34 | In a shaft-hole assembly, the hole is specified as $\mathbf{3 0} 0.040$ <br> shaft has a clearance fit with minimum clearance of $\mathbf{0 . 0 1} \mathbf{~ m m}$. The tolerance <br> on the shaft is $\mathbf{0 . 0 3} \mathbf{~ m m}$. The maximum clearance in $\mathbf{~ m m}$ between the hole <br> and the shaft is |
| :--- | :--- |
| (A) | 0.04 |
| (B) | 0.05 |
| (C) | 0.08 |
| (D) | 0.10 |


| Q.35 | 'GO' and 'NO GO' snap gauges are to be designed for a shaft $\mathbf{3 6 . 0 0 0} \mathbf{+ 0 . 0 7 0}+\mathbf{0 . 0 1 0}$ <br> mm. Gauge tolerance can be taken as $\mathbf{5 \%}$ of the hole tolerance. Following <br> the ISO system of gauge design, the respective sizes of 'GO' and 'NO GO' <br> gauges are |
| ---: | :--- |
| (A) | 36.013 mm and 36.067 mm |
| (B) | 36.015 mm and 36.065 mm |
| (C) | 36.018 mm and 36.062 mm |
| (D) | 36.020 mm and 36.060 mm |

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| Q.36 | A circular tank of $4 \mathbf{m}$ diameter is filled up to a height of $\mathbf{3} \mathbf{~ m . ~ A s s u m i n g ~}$ <br> almost steady flow and neglecting losses, the time taken in seconds to empty <br> the tank through a $5 \mathbf{c m}$ diameter hole located at the center of the tank <br> bottom (take acceleration due to gravity $\boldsymbol{g}=\mathbf{9 . 8 1} \mathbf{m} / \mathbf{s}^{2}$ ) is [round off to the <br> nearest integer] |
| :--- | :--- |
| (A) | 5005 |
| (B) | 1807 |
| (C) | 8097 |
| (D) | 3154 |

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Q. 37 - Q. 55 Numerical Answer Type (NAT), carry TWO mark each (no negative marks).

| Q. 37 | The probability mass function $P(x)$ of a discrete random variable $X$ is given <br> by $P(x)=\frac{1}{2^{x}}$, <br>  <br> $[$ in integer $]$ |
| :--- | :--- |.

Q. 38 The time to pass through a security screening at an airport follows an exponential distribution. The mean time to pass through the security screening is 15 minutes. To catch the flight, a passenger must clear the security screening within 15 minutes. The probability that the passenger will miss the flight is $\qquad$ [round off to 3 decimal places]

| Q. 39 | A machine shop has received four jobs A, B, C and D for processing on a <br> single CNC machine. All jobs are available for processing on the first day of <br> the production schedule calendar, and processing times and due dates as <br> applicable on the first day are given below. Using earliest due date rule, the <br> average tardiness (in days) is <br> Job |  |
| :--- | :--- | :--- |
| $\qquad$Processing time <br> (in days) | Due date <br> (day) |  |
| A | 8 | 14 |
| B | 5 | 10 |
| C | 7 | 12 |
| D | 9 | 19 |

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Q. 40 A time study is carried out for a spot welding operation which is being performed by an operator. The time taken (in seconds) for five observations are recorded as $40,35,45,37$ and 43 , respectively. If the standard time and the allowance for this operation are 45 seconds and 9 seconds, respectively, then the performance rating (in percentage) of the operator is $\qquad$ . [in integer]
Q. 41

The initial cost of a machine is INR $10,00,000$ and its salvage value after 10 years of use is INR $\mathbf{5 0 , 0 0 0}$. Using the straight line depreciation method, the book value in INR of the machine at the end of $7^{\text {th }}$ year is $\qquad$ . [in integer]

| Q. 42 | A project consists of eight activities. The time required for each activit <br> its immediate predecessor(s) are given in the table below. |  |  |
| :---: | :---: | :---: | :---: |
| $\qquad$Activity Activity time (in days) Immediate predecessor(s) <br> A 2 - <br> B 3 - <br> C 2 A <br> D 4 A, B <br> E 4 C <br> F 3 C <br> G 2 D, E |  |  |  |

If the project completion time using critical path method (CPM) is 15 days, then the value of X (in days) is $\qquad$ . [in integer]

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Q. 43 A wire of 5 mm diameter is drawn into a wire of $4 \mathbf{~ m m}$ diameter through a conical die at a constant pulling speed of $5 \mathrm{~m} / \mathrm{s}$. Neglecting the coefficient of friction and redundant work, the drawing stress $\left(\sigma_{d}\right)$ in MPa for the above process is given by $\sigma_{d}=\bar{\sigma} \ln \left[\frac{1}{1-r}\right]$, where $\bar{\sigma}$ is the mean flow strength of wire material in MPa, and $r$ is the ratio of decrease in area of cross-section to initial area of cross-section of the wire. If the mean flow strength of wire material is 600 MPa , then the power required in $k W$ in the above wire drawing process is $\qquad$ .
[round off to 2 decimal places]
Q. 44 In an arc welding process, the DC power source characteristic is linear with an open circuit voltage of 60 V and short circuit current of 600 A . The heat required for melting a metal during the welding is $10 \mathrm{~J} / \mathrm{mm}^{3}$, and the heat transfer and melting efficiencies are $80 \%$ and $25 \%$, respectively. If the weld cross-sectional area of $\mathbf{2 0} \mathbf{~ m m}^{2}$ is made using the maximum arc power, then the required welding speed in $\mathrm{mm} / \mathrm{s}$ is $\qquad$ . [round off to one decimal place]
Q. 45 A company is producing a disc-shaped product of $\mathbf{5 0} \mathbf{~ m m}$ thickness and 1.0 m diameter using sand casting process. The solidification time of the above casting process is estimated by Chvorinov's equation $t=B\left[\frac{V}{A}\right]^{2}$, where $B$ is the mold constant, and $V$ and $A$ are the volume and surface area of the casting, respectively. It is decided to modify both the thickness and diameter of the disc to 25 mm and 0.5 m , respectively, maintaining the same casting condition. The percentage reduction in solidification time of the modified disc as compared to that of the bigger disc is $\qquad$ .[round off to one decimal place]

A single point cutting tool with $15^{\circ}$ orthogonal rake angle is used to machine a mild steel plate under orthogonal machining condition. The depth of cut (uncut thickness) is set at 0.9 mm . If the chip thickness is $\mathbf{1 . 8} \mathbf{~ m m}$, then the shear angle in degree is $\qquad$ . [round off to one decimal place]

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Q. 47 The top layer of a flat $750 \mathrm{~mm} \times \mathbf{3 0 0} \mathbf{~ m m}$ rectangular mild steel plate is to be machined with a single depth of cut using a shaping machine. The plate has been fixed by keeping $\mathbf{7 5 0} \mathbf{~ m m}$ side along the tool travel direction. If the approach and the over-travel are 25 mm each, average cutting speed is $\mathbf{1 0}$ $\mathrm{m} / \mathrm{min}$, feed rate is $0.4 \mathrm{~mm} / \mathrm{stroke}$, and the ratio of return time to cutting time of the tool is $1: 2$, the time (in minutes) required to complete the machining operation is $\qquad$ . [round off to one decimal place]
Q. 48 A 3 mm thick steel sheet, kept at room temperature of $30^{\circ} \mathrm{C}$, is cut by a fiber laser beam. The laser spot diameter on the top surface of the sheet is 0.2 mm . The laser absorptivity of the sheet is $\mathbf{5 0 \%}$. The properties of steel are density $=8000 \mathrm{~kg} / \mathrm{m}^{3}$, specific heat $=500 \mathrm{~J} / \mathrm{kg} .{ }^{\circ} \mathrm{C}$, melting temperature $=1530^{\circ} \mathrm{C}$, and latent heat of fusion $=3 \times 10^{5} \mathrm{~J} / \mathrm{kg}$. Assume that melting efficiency is $100 \%$ and that the kerf width is equal to the laser spot diameter. The maximum speed (in m/s) at which the sheet can be fully cut at 2 kW laser power is $\qquad$ -
[round off to 3 decimal places]

| Q.49 | In a point-to-point open-loop NC drive, a stepper motor with $1.8^{\circ}$ step angle <br> is coupled to a leadscrew through a gear reduction of 4:1 (4 rotations of the <br> motor enables 1 rotation of leadscrew). The single-start leadscrew has a <br> pitch of 4 mm . The worktable of the system is driven by the leadscrew. If the <br> table moves at a uniform speed of $10 \mathrm{~mm} / \mathrm{s}$, the pulse frequency (in Hz) <br> required to drive the stepper motor is__ [round off to one decimal <br> place] |
| :--- | :--- |
| generator |  |

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| Q. 50 | A 30 kg smooth, solid sphere rests on two frictionless inclines as shown in <br> the figure. The magnitude of contact force in N acting at the point A is (take <br> acceleration due to gravity $g=9.81 \mathrm{~m} / \mathbf{s}^{2}$ and consider both sphere and <br> inclines to be rigid) <br> [round off to 2 decimal places] |
| :--- | :--- |

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Q. 51 Consider the truss shown in the figure. The members AB, BC, and CA are all rigid and form an equilateral triangle. The contact between roller and ground at $C$ is frictionless. If the self-weight of members is neglected, the force in member $B C$ in $N$ is (negative sign should be used if the force is compressive and positive if the force in the member is tensile) $\qquad$ .
[round off to one decimal place]

Q. 52 A fluid with dynamic viscosity $\mu=1$ Pa.s is flowing through a circular pipe with diameter 1 cm . If the flow rate (discharge) in the pipe is 0.2 liter/s, the maximum velocity in $\mathrm{m} / \mathrm{s}$ of the fluid in the pipe is (assume fully developed flow and take fluid density $\rho=1000 \mathrm{~kg} / \mathrm{m}^{3}$ ) $\qquad$ . [round off to one decimal place]

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Q. 53 Values of function $y(x)$ at discrete values of $x$ for $0 \leq x \leq 10$ are given in table. Using trapezoidal rule, $\int_{0}^{10} y(x) d x=$ $\qquad$ .
[round off to one decimal place]

| $x$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $y(x)$ | 5 | 3 | 0 | -5 | -10 | -6 | 0 | 5 | 11 | 18 | 30 |

Q. 54 Temperature field inside a sphere of radius $R=1 \mathrm{~m}$ with origin at its center is $\quad T(x, y, z)=100-70 x+51 y-80 z-10 x^{2}-20 y^{2}-20 z^{2}$. If thermal conductivity of the sphere material is $K=50 \mathrm{~W} / \mathrm{m}$.K and Fourier law of heat conduction is valid, net heat leaving the sphere per unit time in $W$ is
$\qquad$ .
[round off to one decimal place]
Q. 55

A 3.5 mm thick sheet is rolled using a two high rolling mill to reduce the thickness under plane strain condition. Both rolls have a diameter of $\mathbf{5 0 0} \mathbf{~ m m}$ and are rotating at 200 RPM. The coefficient of friction at the sheet and roll interface is 0.08 , and the elastic deflection of the rolls is negligible. If the mean flow strength of the sheet material is 400 MPa , then the minimum possible thickness (in $\mathbf{m m}$ ) of sheet that can be produced in a single pass is
$\qquad$ .
[round off to 2 decimal places]

## END OF THE QUESTION PAPER

