Graduate Aptitude Test in Engineering 2021 Organising Institute - IIT Bombay

Metallurgical Engineering (MT)

## General Aptitude (GA)

Q. 1 - Q. 5 Multiple Choice Question (MCQ), carry ONE mark each (for each wrong answer: - 1/3).

| Q.1 | Five persons $P, Q, R, S$ and T are to be seated in a row, all facing the same <br> direction, but not necessarily in the same order. P and T cannot be seated at <br> either end of the row. P should not be seated adjacent to S. R is to be seated <br> at the second position from the left end of the row. The number of distinct <br> seating arrangements possible is: |
| :--- | :--- |
| (A) | 2 |
| (B) | 3 |
| (C) | 4 |
| (D) | 5 |


| Q. 2 | Consider the following sentences: <br> (i) <br> The number of candidates who appear for the GATE <br> examination is staggering. <br> Ais number of candidates from my class are appearing for the <br> GATE examination. <br> (The number of candidates who appear for the GATE <br> examination are staggering. <br> (iii) number of candidates from my class is appearing for the GATE <br> examination. <br> (iv) <br> Which of the above sentences are grammatically CORRECT? |
| :--- | :--- |
| (A) | (i) and (ii) |
| (B) | (i) and (iii) |
| (C) | (ii) and (iii) |
| (D) | (ii) and (iv) |

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| Q. 3 | A digital watch X beeps every $\mathbf{3 0}$ seconds while watch Y beeps every $\mathbf{3 2}$ <br> seconds. They beeped together at 10 AM. <br> The immediate next time that they will beep together is <br> (A) |
| ---: | :--- |
| (B) | 10.08 AM |
| (C) | 11.00 AM |
| (D) | 10.00 PM |


| Q. 4 | If $\oplus \div \odot=2 ; ~$ <br> Then, the value of $(\otimes-\oplus=3 ; \odot+\Delta=5 ; \Delta \times \otimes=10$, <br> , is: |
| :--- | :--- |
| (A) | 0 |
| (B) | 1 |
| (C) | 4 |
| (D) | 16 |


| Q.5 | The front door of Mr. X's house faces East. Mr. X leaves the house, walking <br> $\mathbf{5 0} \mathbf{m}$ straight from the back door that is situated directly opposite to the front <br> door. He then turns to his right, walks for another 50 $\mathbf{m}$ and stops. The <br> direction of the point Mr. X is now located at with respect to the starting point <br> is |
| ---: | :--- |
| (A) | South-East |
| (B) | North-East |
| (C) | West |
| (D) | North-West |

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Q. 6 - Q. 10 Multiple Choice Question (MCQ), carry TWO marks each (for each wrong answer: - 2/3).

| Q.6 | Given below are two statements 1 and 2, and two conclusions I and II. <br> Statement 1: All entrepreneurs are wealthy. <br> Statement 2: All wealthy are risk seekers. <br> Conclusion I: All risk seekers are wealthy. <br> Conclusion II: Only some entrepreneurs are risk seekers. <br> Based on the above statements and conclusions, which one of the following <br> options is CORRECT? |
| ---: | :--- |
| (A) | Only conclusion I is correct |
| (B) | Only conclusion II is correct |
| (C) | Neither conclusion I nor II is correct |
| (D) | Both conclusions I and II are correct |


| Q.7 | A box contains 15 blue balls and 45 black balls. If 2 balls are selected <br> randomly, without replacement, the probability of an outcome in which the <br> first selected is a blue ball and the second selected is a black ball, is |
| :--- | :--- |
| (A) | $\frac{3}{16}$ |
| (B) | $\frac{45}{236}$ |
| (C) | $\frac{1}{4}$ |
| (D) | $\frac{3}{4}$ |

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| Q. 8 |  |
| :--- | :--- |
| (A) | $\frac{1}{8}$ |
| (B) | $\frac{1}{6}$ |
| (C) | $\frac{1}{4}$ |
| (D) | $\frac{1}{2}$ |


| Q. 9 | Consider a square sheet of side 1 unit. The sheet is first folded along the main <br> diagonal. This is followed by a fold along its line of symmetry. The resulting <br> folded shape is again folded along its line of symmetry. The area of each face <br> of the final folded shape, in square units, equal to <br> (A) <br> $\frac{1}{4}$ <br> (B) |
| :--- | :--- |
| (C) | $\frac{1}{8}$ |
| (D) | $\frac{1}{32}$ |

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| Q.10 | The world is going through the worst pandemic in the past hundred years. <br> The air travel industry is facing a crisis, as the resulting quarantine <br> requirement for travelers led to weak demand. <br> In relation to the first sentence above, what does the second sentence do? |
| ---: | :--- |
| (A) | Restates an idea from the first sentence. |
| (B) | Second sentence entirely contradicts the first sentence. |
| (C) | The two statements are unrelated. |
| (D) | States an effect of the first sentence. |

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Q. 1 - Q. 13 Multiple Choice Question (MCQ), carry ONE mark each (for each wrong answer: - 1/3).

| Q.1 | For the matrix given below, the eigenvalues are: <br> $\left(\begin{array}{ccc}\mathbf{1} & \mathbf{0} & \mathbf{1} \\ \mathbf{0} & \mathbf{1} & \mathbf{0} \\ \mathbf{- 1} & \mathbf{0} & \mathbf{1}\end{array}\right)$ <br> (A) 0,2,2 |
| :--- | :--- |
| (B) | $1,1,2$ |
| (C) | $0,1,2$ |
| (D) | $0,1,3$ |


| Q. 2 | Which one of the following is a homogeneous function of degree three? |
| ---: | :--- |
| (A) | $x^{3}+2 x^{2} y^{2}$ |
| (B) | $y^{2} x+2 y x^{2}$ |
| (C) | $y^{3}+2 x^{2}$ |
| (D) | $x y^{2}+3 x y$ |

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| Q.3 | The divergence of a vector field $\overrightarrow{\boldsymbol{V}}(\boldsymbol{x}, \boldsymbol{y}, \boldsymbol{z})$, where its three components $\left(\boldsymbol{V}_{\boldsymbol{x}}\right.$, <br> $\left.\boldsymbol{V}_{\boldsymbol{y}}, \boldsymbol{V}_{\boldsymbol{z}}\right)$ are functions of $\boldsymbol{x}, \boldsymbol{y}, \boldsymbol{z}$, is: |
| :--- | :--- |
| (A) | $\frac{\partial V_{x}}{\partial x}+\frac{\partial V_{y}}{\partial y}+\frac{\partial V_{z}}{\partial z}$ |
| (B) | $\left(\frac{\partial V_{z}}{\partial y}-\frac{\partial V_{y}}{\partial z}\right) \boldsymbol{i}+\left(\frac{\partial V_{x}}{\partial z}-\frac{\partial V_{z}}{\partial x}\right) \boldsymbol{j}+\left(\frac{\partial V_{y}}{\partial x}-\frac{\partial V_{x}}{\partial y}\right) \boldsymbol{k}$ |
| (C) | $\frac{\partial V_{x}}{\partial x} \boldsymbol{i}+\frac{\partial V_{y}}{\partial y} \boldsymbol{j}+\frac{\partial V_{z}}{\partial z} \boldsymbol{k}$ |
| (D) | $\frac{\partial^{2} V_{x}}{\partial x^{2}}+\frac{\partial^{2} V_{y}}{\partial y^{2}}+\frac{\partial^{2} V_{z}}{\partial z^{2}}$ |

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Q. 4 Which one of the following is 'center split' defect in rolling operation?

| Q.5 | Single crystal turbine blades of nickel-based superalloys for aero-engines <br> are manufactured using: |
| ---: | :--- |
| (A) | Investment casting |
| (B) | Die casting |
| (C) | Squeeze casting |
| (D) | Directional solidification |

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| Q.6 | Elements A and B have the same crystal structure. For a dilute solution of <br> B in A, which one of the following is true? <br> (Given: $\boldsymbol{\Delta} \boldsymbol{H}_{\text {mix }}-$ Mixing enthalpy, $a_{B}-$ Activity of $\mathbf{B}$ and $X_{B}-$ Mole <br> fraction of B) |
| :--- | :--- |
| (A) | If $\Delta H_{m i x}=0$, then $a_{B}<X_{B}$ |
| (B) | If $\Delta H_{m i x}=0$, then $a_{B}>X_{B}$ |
| (C) | If $\Delta H_{m i x}>0$, then $a_{B}<X_{B}$ |
| (D) | If $\Delta H_{m i x}<0$, then $a_{B}<X_{B}$ |


| Q.7 | For uniaxial tensile stress-strain behaviour of polycrystalline aluminium, <br> which one of the following statements is FALSE? |
| ---: | :--- |
| (A) | True stress is always higher than the engineering stress. |
| (B) | At the ultimate tensile stress point on the true stress - strain curve, $\frac{d \sigma}{d \varepsilon}=0$ |
| (C) | Resilience is the area under the elastic region of the engineering stress - strain <br> curve. |
| (D) | Maximum true stress does not correspond to the maximum load. |


| Q.8 | Which one of the following is FALSE for creep deformation? |
| ---: | :--- |
| (A) | The minimum creep rate is obtained in the primary stage (stage I). |
| (B) | Creep resistance decreases with decrease in grain size. |
| (C) | Coble creep occurs via grain boundary diffusion. |
| (D) | Nabarro-Herring creep occurs via lattice diffusion. |

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| Q.9 | Which one of the following elements alloyed with iron is a ferrite <br> stabilizer? |
| ---: | :--- |
| (A) | Nickel |
| (B) | Manganese |
| (C) | Carbon |
| (D) | Silicon |


| Q.10 | Which one of the following is the correct decreasing sequence of Quenching <br> Power for quenchants used in heat treatment of steels? |
| ---: | :--- |
| (A) | Oil > Water > Brine > Air |
| (B) | Brine > Oil > Water > Air |
| (C) | Brine > Water > Oil > Air |
| (D) | Water > Brine > Oil > Air |


| Q.11 | For a zeroth order chemical reaction, which one of the following is <br> FALSE? |
| ---: | :--- |
| (A) | Concentration versus time plot is a straight line. |
| (B) | Increase in concentration of reacting species increases the rate of reaction. |
| (C) | Half-life depends on the initial concentration and zero-order rate constant. |
| (D) | Rate of reaction depends on temperature. |

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| Q.12 | Which one of the following elements oxidizes first in basic oxygen steel <br> making process? |
| ---: | :--- |
| (A) | Silicon |
| (B) | Carbon |
| (C) | Manganese |
| (D) | Phosphorus |


| Q.13 | Which one of the following is a hydrometallurgical operation? |
| ---: | :--- |
| (A) | Roasting |
| (B) | Leaching |
| (C) | Zone refining |
| (D) | Smelting |

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Q. 14 - Q. 25 Numerical Answer Type (NAT), carry ONE mark each (no negative marks).

$$
\text { Q. } 14 \text { The value of } \lim _{x \rightarrow 0} \frac{\sin ^{2} 5 x}{\sin ^{2} x} \text { is: ___ (round off to nearest integer). }
$$

Q. 15 The grain size ( $\mathbf{X}$ ) of annealed specimens follows a symmetric distribution with a mean $(\mu)$ of $5 \mu \mathrm{~m}$ and a standard deviation ( $\sigma$ ) of $0.5 \mu \mathrm{~m}$. The percentage of specimens with grain size in the range 5 to $6 \mu \mathrm{~m}$ is expected to be: $\qquad$ (round off to nearest integer).
Given: For the symmetric distribution: Probability $\mathbf{P}(\mathbf{X} \leq \mu+2 \sigma)=\mathbf{0 . 9 8}$
Q. 16 If $E_{N i^{2+} / N i}^{o}=-0.25 \mathrm{~V}$, the value of $\mu_{N i^{2+}}^{o}\left(\right.$ in $\left.\mathrm{J} \mathrm{mol}^{-1}\right)$ at 298 K is: $\qquad$ (round off to nearest integer).
Given: $\mathrm{F}=96500 \mathrm{C} \mathrm{mol}^{-1}$
Q. 17 Melting point of $\mathbf{C u}$ is $\mathbf{1 3 5 8} \mathbf{K}$ and its enthalpy of melting is $\mathbf{1 3 4 0 0} \mathrm{J} \mathrm{mol}^{-1}$. The value of free energy change (in $\mathrm{J} \mathrm{mol}^{-1}$ ) for liquid to solid transformation at 1058 K is: $\qquad$ (round off to nearest integer).
Assume: $\boldsymbol{C}_{P}^{\text {liquid }}=C_{P}^{\text {solid }}$
Q. 18 A body is subjected to a state of stress given by the following stress tensor: $\left(\begin{array}{ccc}50 & 0 & 0 \\ 0 & 200 & 0 \\ 0 & 0 & 100\end{array}\right)$ MPa.
If yielding is predicted by the Tresca Criterion, the uniaxial tensile yield stress (in MPa) of the body should be less than or equal to: $\qquad$ (round off to nearest integer).
Q. 19 Consider homogeneous nucleation of a spherical solid in liquid. For a given undercooling, if surface energy of a nucleus increases by $20 \%$, the corresponding increase (in percent) in the critical radius of the nucleus is: (round off to nearest integer).

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Q. 20 If saturation magnetization of iron at room temperature is $1700 \mathrm{kA} \mathrm{m}^{-1}$, the magnetic moment (in $\mathbf{A ~ m}^{2}$ ) per iron atom in the crystal is: $\qquad$ $\times 10^{-23}$ (round off to 1 decimal place).
(Given: Lattice parameter of iron at room temperature $\mathbf{=} \mathbf{0 . 2 8 7} \mathbf{~ n m}$ )
Q. 21 In the X-ray diffraction pattern of a FCC crystal, the first reflection occurs at a Bragg angle ( $\theta$ ) of $30^{\circ}$. The Bragg angle (in degree) for the second reflection will be: $\qquad$ (round off to 1 decimal place).
Q. 22 A $0.6 \mathrm{wt} . \% \mathrm{C}$ steel sample is slowly cooled from $900^{\circ} \mathrm{C}$ to room temperature. The fraction of proeutectoid ferrite in the microstructure is: (round off to 2 decimal places).
Given: Eutectoid composition: $0.8 \mathrm{wt} . \% \mathrm{C}$
Maximum solubility of carbon in $\alpha$-Fe: $0.025 \mathbf{w t} . \% \mathrm{C}$
Q. 23 If the degree of polymerization of polyethylene is 30000 , the average molecular weight (in $\mathrm{g} \mathrm{mol}^{-1}$ ) is: $\qquad$ (round off to nearest integer).
(Given: Atomic weights of carbon and hydrogen are 12 and 1, respectively)

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Q. 25 The vacancy concentration in a crystal doubles upon increasing the temperature from $27^{\circ} \mathrm{C}$ to $127^{\circ} \mathrm{C}$. The enthalpy (in $\mathrm{kJ} \mathrm{mol}^{-1}$ ) of vacancy formation is: $\qquad$ (round off to 2 decimal places).
Given: $\mathrm{R}=8.314 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$

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Q. 26 - Q. 36 Multiple Choice Question (MCQ), carry TWO mark each (for each wrong answer: - 2/3).

| Q.26 | The minimum value of $\boldsymbol{y}$ for the equation $\boldsymbol{y}=\boldsymbol{x}^{2}-\mathbf{2 x + 4}$ is |
| :--- | :--- |
| (A) | 3 |
| (B) | 1 |
| (C) | 4 |
| (D) | 6 |

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| Q. 27 | Match the forming process (in Column I) with its name (in Column II): <br> Column I <br> (P) <br> (R) <br> (S) <br> Column II <br> 1. Extrusion <br> 2. Rolling <br> 3. Deep Drawing <br> 3. Deep Drawing <br> 4. Open Die Forging |
| :---: | :---: |
| (A) | $\mathrm{P}-1, \mathrm{Q}-2, \mathrm{R}-3, \mathrm{~S}-4$ |
| (B) | $\mathrm{P}-3, \mathrm{Q}-1, \mathrm{R}-4, \mathrm{~S}-2$ |
| (C) | $\mathrm{P}-3, \mathrm{Q}-4, \mathrm{R}-1, \mathrm{~S}-2$ |
| (D) | $\mathrm{P}-1, \mathrm{Q}-4, \mathrm{R}-3, \mathrm{~S}-2$ |

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| Q.28 | Match the nondestructive technique (in Column I) with its underlying <br> phenomenon (in Column II): <br> Column I |
| :--- | :--- | :--- |
|  | (P) Dye penetrant test  <br> (Q) Radiography Column II <br>  (R) Eddy current test <br> (S) Ultrasonic inspection 1. X-ray absorption <br> (A) P-4, Q-3, R-2, S-1 <br> (B) P-2, Q-1, R-3, S-4 <br> (C) P-2, Q-1, R-4, S-3 <br> (D) P-3, Q-2, Electromagnetic waves reflection induction |


| Q.29 | Number of degrees of freedom for the following reacting system is: <br> $\mathbf{M}(\mathbf{s})+\mathbf{C O}_{2}(\mathbf{g})=\mathbf{M O}(\mathbf{s})+\mathbf{C O}(\mathbf{g})$ |
| ---: | :--- |
| (A) | 0 |
| (B) | 1 |
| (C) | 2 |
| (D) | 3 |

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| Q. 30 | The condition for getting the binary phase diagram of A-B (shown below) is: <br> Given: $\Delta H_{\text {mix }}^{\text {solid }}$ - Enthalpy of mixing of solid $\Delta H_{m i x}^{\text {liquid }} \text { - Enthalpy of mixing of liquid }$ |
| :---: | :---: |
| (A) | $\Delta H_{m i x}^{\text {solid }}=0$ and $\Delta H_{m i x}^{\text {liquid }}=0$ |
| (B) | $\Delta H_{m i x}^{\text {solid }} \ll 0$ and $\Delta H_{m i x}^{\text {liquid }}=0$ |
| (C) | $\Delta H_{m i x}^{\text {solid }}>0$ and $\Delta H_{m i x}^{\text {liquid }}=0$ |
| (D) | $\Delta H_{\text {mix }}^{\text {solid }}=0$ and $\Delta H_{\text {mix }}^{\text {liquid }} \ll 0$ |


| Q.31 | In the absence of any external stress, which one of the following statements <br> related to the interaction of point defect and a dislocation is FALSE: |
| ---: | :--- |
| (A) | An oversized solute atom would preferentially migrate below the slip plane of <br> an edge dislocation. |
| (B) | A spherically symmetric point defect can interact with both the hydrostatic and <br> shear stress fields of a dislocation. |
| (C) | A point defect can locally modify the elastic modulus and thereby can change <br> the interaction energy. |
| (D) | Vacancies are attracted towards the compressive region of dislocation. |

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| Q.32 | A single crystal aluminium sample is subjected to uniaxial tension along <br> [112] direction. If the applied tensile stress is 100 MPa and the critical <br> resolved shear stress (CRSS) is 25 MPa, which one of the following slip <br> systems will be activated? |
| ---: | :--- |
| (A) | $[\overline{1} 01](111)$ |
| (B) | $[\overline{1} 10](111)$ |
| (C) | $[101](11 \overline{1})$ |
| (D) | $[011](11 \overline{1})$ |


| Q.33 | One-dimensional steady-state temperature distribution in two adjacent <br> refractory blocks (with thermal conductivities, $\mathbf{k}_{1}$ and $\mathbf{k}_{2}$ of unit cross- <br> sectional area are shown below. The temperature $\mathbf{T 1}$ and thermal contact <br> resistance of the interface, respectively, are: |
| :--- | :--- | :--- |
| (A) | $200 \mathrm{~K}, 0.5 \mathrm{~K} \mathrm{~W}^{-1}$ |
| (B) | $400 \mathrm{~K}, 1.0 \mathrm{~K} \mathrm{~W}^{-1}$ |
| (C) | $200 \mathrm{~K}, 0.25 \mathrm{~K} \mathrm{~W}^{-1}$ |
| (D) | $500 \mathrm{~K}, 0.5 \mathrm{~K} \mathrm{~W}^{-1}$ |

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| Q. 34 | For a fully developed 1-D flow of a Newtonian fluid through a horizontal <br> pipe of radius $\mathbf{R}$ (see figure), the axial velocity $\left(\boldsymbol{v}_{\boldsymbol{z}}\right)$ is given by: <br> $\boldsymbol{v}_{\boldsymbol{Z}}=\left[\frac{\Delta \boldsymbol{P}}{\boldsymbol{L}}\right]\left(\frac{\boldsymbol{R}^{2}-\boldsymbol{r}^{2}}{4 \boldsymbol{\mu}}\right)$, <br> where, $\Delta \boldsymbol{P}$ is the pressure difference $(\boldsymbol{P} 1-\boldsymbol{P} 2), \boldsymbol{\mu}$ is the viscosity, $\boldsymbol{r}$ is the <br> radial distance from the axis and $L$ is the length of the tube. The shear <br> stress exerted by the fluid on the tube wall is: |
| :--- | :--- |
| (A) $\frac{\Delta P R}{2 L}$ |  |
| (B) $\frac{\Delta P R}{L}$ |  |
| (C) $\frac{3 \Delta P R}{2 L}$ |  |
| (D) $\frac{2 \Delta P R}{L}$ |  |

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| Q.35 | Match the terms (in Column I) with the unit process (in Column II) |  |
| :--- | :--- | :--- |
|  | Column I | Column II |
|  | (P) Submerged Entry Nozzle | 1. Ladle Furnace |
|  | (Q) Electric Heating 2. Continuous Casting <br> (R) Raceway Zone 3. LD Converter <br> (S) Oxygen Lancing 4. Blast Furnace |  |
| (A) | P-2, Q-1, R-4, S-3 |  |
| (B) | P-4, Q-1, R-2, S-3 |  |
| (C) | P-4, Q-3, R-1, S-2 |  |
| (D) | P-2, Q-3, R-4, S-1 |  |


| Q.36 | A blast furnace uses hematite ore with $\mathbf{8 0 \%} \mathrm{Fe}_{2} \mathrm{O}_{3}$ and $\mathbf{2 0 \%}$ gangue <br> materials. It uses $\mathbf{6 0 0} \mathrm{kg}$ coke per ton of hot metal. The coke contains $\mathbf{8 5 \%} \%$ <br> C and 15\% ash. The composition of hot metal is $\mathbf{9 5 . 5 \%} \mathbf{F e}$ and $\mathbf{4 . 5 \%} \mathbf{C}$. <br> The weight of iron ore used and slag produced per ton of hot metal <br> respectively, are: <br> Given: Atomic weight: $\mathbf{O}=\mathbf{1 6}, \mathbf{C}=\mathbf{1 2}, \mathbf{N}=\mathbf{1 4}, \mathbf{F e}=\mathbf{5 6}$ <br> All the compositions are in wt.\%. <br> $\mathbf{1}$ ton = 1000 kg |
| ---: | :--- |
| (A) | Assume that the gangue materials of the ore and ash content of coke form <br> slag while $\mathrm{Fe}_{2} \mathbf{O}_{\mathbf{3}}$ in the ore is consumed in making hot metal. |
| (B) | $2131 \mathrm{~kg}, 546 \mathrm{~kg}, 431 \mathrm{~kg}$ |
| (C) | $1705 \mathrm{~kg}, 331 \mathrm{~kg}$ |
| (D) | $1500 \mathrm{~kg}, 431 \mathrm{~kg}$ |

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Q. 37 - Q. 55 Numerical Answer Type (NAT), carry TWO mark each (no negative marks).

| Q. 37 | Consider the function $f(x)=x-\cos x$. Using Newton-Raphson method, <br> the estimated root of $f(x)$ after the first iteration is:___ (round off to 3 <br> decimal places). <br> Assume: Initial guess of the root $=0.5$ radians. |
| :--- | :--- |

Q. 38 The work done by a force $\vec{F}=2 x i+3 y j$ along a straight line from point $(0,0)$ to $(1,2)$ is: $\qquad$ (round off to nearest integer).

| Q. 39 | A coin is tossed three times. Given that there are more heads than tails, the |
| :--- | :--- | probability of getting exactly one tail is: $\qquad$ (round off to 2 decimal places).

Q. 40 A continuous fillet weld is made using a 3000 W welding machine. At a travel speed of $6 \mathrm{~mm} \mathrm{~s}^{-1}$, the cross-sectional area (in $\mathrm{mm}^{2}$ ) of the weld is:
$\qquad$ (round off to nearest integer).
Given: $\quad$ The unit energy required to melt the metal is $6 \mathrm{~J} \mathrm{~mm}^{-3}$.
Heat transfer factor $=0.6$
Melting factor $=0.5$
Q. 41 Liquid iron is cast into a spherical sand mold ( 6 cm radius) and a cubical sand mold ( $\mathbf{1 2} \mathbf{~ c m}$ edge length). If solidification time is $\mathbf{6 0}$ minutes in the spherical casting, the time (in minutes) required to solidify in the cubical casting is: $\qquad$ (round off to nearest integer).
Q. 42 True strain for $\mathbf{6 0 \%}$ height reduction of a sample subjected to hot forging is: $\qquad$ (round off to 2 decimal places).

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Q. 43 For the equilibrium reaction: $2 \mathrm{Cu}(s)+\mathrm{SO}_{2}(g)=\mathrm{Cu}_{2} S(s)+\mathrm{O}_{2}(g)$, the value of $\ln \left(\frac{P_{O_{2}}}{P_{S o_{2}}}\right)$ at 973 K is: $\qquad$ (round off to 2 decimal places).

Given:

$$
\begin{array}{ll}
2 C u(s)+0.5 S_{2}(g)=C u_{2} S(s) & \Delta G^{0} \text { at } 973 \mathrm{~K}=-100 \mathrm{~kJ} \\
S O_{2}(g)=0.5 S_{2}(g)+O_{2}(g) & \Delta G^{0} \text { at } 973 \mathrm{~K}=292 \mathrm{~kJ} \\
\mathrm{R}=8.314 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1} &
\end{array}
$$

Assume: Cu and $\mathrm{Cu}_{2} \mathrm{~S}$ are pure solids.
Q. 44 One mole of an ideal gas at 10 atm . and 300 K undergoes reversible adiabatic expansion to a pressure of one atm. The work done (in Joule) by the gas is: $\qquad$ (round off to nearest integer).
Given: $\mathrm{R}=8.314 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1} ; 1 \mathrm{~atm} .=101325 \mathrm{~Pa} ; \mathrm{Cp}=2.5 \mathrm{R}$
Q. 45 The figure shows the entropy versus temperature (S-T) plot of a reversible cycle of an engine. If $\mathbf{T}_{1}=200 \mathrm{~K}$ and $\mathrm{T}_{\mathbf{2}}=\mathbf{6 0 0} \mathrm{K}$, the efficiency of the engine (in percent) is: $\qquad$ (round off to 2 decimal places).


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Q. 46 Two dislocation lines parallel to $z$-axis lying in the $x$-z plane are shown in the figure. The glide force (in Newton) exerted by the edge dislocation on the screw dislocation is: $\qquad$ (round off to nearest integer).


For the edge, the shear stress component is given by:
$\tau_{\mathrm{xy}}=\frac{\mathrm{Gb}}{2 \pi(1-\mathrm{v})} \frac{\mathrm{x}\left(\mathrm{x}^{2}-\mathrm{y}^{2}\right)}{\left(\mathrm{x}^{2}+\mathrm{y}^{2}\right)^{2}}$
Given: Shear modulus, $\mathbf{G}=28 \mathbf{G P a}$
Poisson's ratio, $v=0.3$
Burgers vector, $b=0.29 \mathrm{~nm}$
Distance between the two dislocations $\mathbf{=} \mathbf{0 . 5} \mathbf{~ n m}$
Q. 47

In a material, a shear stress of 100 MPa is required to bow a dislocation line between precipitates with a spacing of $0.2 \mu \mathrm{~m}$. If the spacing between the precipitates is increased to $0.5 \mu \mathrm{~m}$, the shear stress (in MPa) to bow the dislocation would be: $\qquad$ (round off to nearest integer).
Q. 48 A metal plate is in a state of plane strain $\left(\varepsilon_{z z}=0\right)$ with $\sigma_{x x}=\sigma_{y y} \neq 0$ and $\tau_{x y}=\tau_{x z}=\tau_{y z}=0$. If the Poisson's ratio is 0.3 , the ratio, $\sigma_{z z} / \sigma_{x x}$ is (round off to 1 decimal place).

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Q. 49 An infinite metal plate has a central through-thickness crack of length $\frac{80}{\pi}$ mm . The maximum applied stress (in MPa) that the plate can sustain in mode $I$ is: $\qquad$ (round off to nearest integer).

Assume: Linear elastic fracture mechanics is valid
Given: Fracture toughness, $K_{I C}=\mathbf{2 0} \mathbf{~ M P a ~ m} \mathbf{m}^{1 / 2}$
Q. 50 A hypothetical binary eutectic phase diagram of A-B is shown below. An alloy with $5 \mathrm{wt} . \%$ B solidifies with no convection. Assuming steady state, the critical temperature gradient (in $\mathbf{K ~ m m}^{-1}$ ) required to maintain planar solidification front is: $\qquad$ (round off to nearest integer).


Given: $\quad$ Diffusivity of $B$ in liquid $=10^{-9} \mathrm{~m}^{2} \mathrm{~s}^{-1}$
Velocity of solidification front $=4 \mu \mathrm{~m} \mathrm{~s}^{-1}$

| Q. 51 | A thick steel plate containing $0.1 \mathrm{wt} . \% \mathrm{C}$ is carburized at $950{ }^{\circ} \mathrm{C}$. The plate's surface carbon concentration is maintained at $1.1 \mathrm{wt} . \%$ C. After 9 hours, the depth (in mm) below the surface at which the carbon concentration is $0.6 \mathrm{wt} . \% \mathrm{C}$ will be: $\qquad$ (round off to 2 decimal places). <br> Given: Diffusivity of carbon in $\gamma$-Fe at $950{ }^{\circ} \mathrm{C}=1.6 \times 10^{-11} \mathrm{~m}^{2} \mathrm{~s}^{-1}$ <br> Error function table: |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | z | 0.35 | 0.40 | 0.45 | 0.50 | 0.55 | 0.60 |
|  |  | 0.3794 | 0.4284 | 0.4755 | 0.5205 | 0.5633 | 0.6039 |

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## Q. 52 At $25^{\circ} \mathrm{C}$, iron corrodes in a deaerated acid of pH 3 with a corrosion

 current density of $4 \mu \mathrm{~A} \mathrm{~cm}^{-2}$. The corrosion potential (V) is: $\qquad$ (round off to 2 decimal places).Given: $\quad \beta_{c}=0.1 \mathrm{~V}$ per decade of current density
Exchange current density of hydrogen on iron surface $=10^{-9} \mathrm{~A} \mathrm{~cm}^{-2}$
$\mathrm{R}=8.314 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}, \mathrm{~F}=96500 \mathrm{C} \mathrm{mol}^{-1}$
All potentials are with reference to standard hydrogen electrode.

> | Q. 53 | $\begin{array}{l}\text { The radius of an interstitial atom which just fits (without distorting the } \\ \text { structure) inside an octahedral void of a bcc-iron crystal (in } \mathrm{nm} \text { ) is: } \\ \text { (round off to } 3 \text { decimal places). }\end{array}$ |
| :--- | :--- |
|  | Assume the radius of Fe atom to be 0.124 nm. |

Q. 54 Nickel undergoes isothermal oxidation at 800 K for a duration of 400 s resulting in a weight gain of $2 \mathrm{mg} \mathrm{cm}^{-2}$. The weight gain $\left(\mathrm{mg} \mathrm{cm}^{-2}\right)$ after a duration of 1600 s is: $\qquad$ (round off to nearest integer).

Assume: Weight gain is proportional to square root of time.

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END OF THE QUESTION PAPER

