Graduate Aptitude Test in Engineering 2021 Organising Institute - IIT Bombay

Mechanical Engineering (ME, Set-2)

## General Aptitude (GA)

Q. 1 - Q. 5 Multiple Choice Question (MCQ), carry ONE mark each (for each wrong answer: - 1/3).

| Q.1 | Five persons P, Q, R, S and T are to be seated in a row, all facing the same <br> direction, but not necessarily in the same order. P and T cannot be seated at <br> either end of the row. P should not be seated adjacent to S. R is to be seated <br> at the second position from the left end of the row. The number of distinct <br> seating arrangements possible is: |
| :--- | :--- |
| (A) | 2 |
| (B) | 3 |
| (C) | 4 |
| (D) | 5 |


| Q. 2 | Consider the following sentences: <br> (i) <br> The number of candidates who appear for the GATE <br> examination is staggering. <br> Ais number of candidates from my class are appearing for the <br> GATE examination. <br> The number of candidates who appear for the GATE <br> examination are staggering. <br> (iii) number of candidates from my class is appearing for the GATE <br> examination. <br> (iv) <br> Which of the above sentences are grammatically CORRECT? |
| :--- | :--- |
| (A) | (i) and (ii) |
| (B) | (i) and (iii) |
| (C) | (ii) and (iii) |
| (D) | (ii) and (iv) |

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Mechanical Engineering (ME, Set-2)

| Q. $\mathbf{3}$ | A digital watch X beeps every $\mathbf{3 0}$ seconds while watch Y beeps every 32 <br> seconds. They beeped together at 10 AM. <br> The immediate next time that they will beep together is <br> (A) |
| :--- | :--- |
| (B) | 10.08 AM |
| (C) | 11.00 AM |
| (D) | 10.00 PM |


| Q. 4 | If $\oplus \div \odot=2 ; ~$ <br> Then, the value of $(\otimes-\oplus=3 ; \odot+\Delta=5 ; \Delta \times \otimes=10$, <br> , is: |
| :--- | :--- |
| (A) | 0 |
| (B) | 1 |
| (C) | 4 |
| (D) | 16 |


| Q.5 | The front door of Mr. X's house faces East. Mr. X leaves the house, walking <br> $\mathbf{5 0} \mathbf{m}$ straight from the back door that is situated directly opposite to the front <br> door. He then turns to his right, walks for another 50 $\mathbf{m}$ and stops. The <br> direction of the point Mr. X is now located at with respect to the starting point <br> is |
| ---: | :--- |
| (A) | South-East |
| (B) | North-East |
| (C) | West |
| (D) | North-West |

Mechanical Engineering (ME, Set-2)
Q. 6 - Q. 10 Multiple Choice Question (MCQ), carry TWO marks each (for each wrong answer: - 2/3).

| Q.6 | Given below are two statements 1 and 2, and two conclusions I and II. <br> Statement 1: All entrepreneurs are wealthy. <br> Statement 2: All wealthy are risk seekers. <br> Conclusion I: All risk seekers are wealthy. <br> Conclusion II: Only some entrepreneurs are risk seekers. <br> Based on the above statements and conclusions, which one of the following <br> options is CORRECT? |
| ---: | :--- |
| (A) | Only conclusion I is correct |
| (B) | Only conclusion II is correct |
| (C) | Neither conclusion I nor II is correct |
| (D) | Both conclusions I and II are correct |


| Q. 7 | A box contains 15 blue balls and 45 black balls. If 2 balls are selected <br> randomly, without replacement, the probability of an outcome in which the <br> first selected is a blue ball and the second selected is a black ball, is |
| :--- | :--- |
| (A) | $\frac{3}{16}$ |
| (B) | $\frac{45}{236}$ |
| (C) | $\frac{1}{4}$ |
| (D) | $\frac{3}{4}$ |

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Mechanical Engineering (ME, Set-2)

| Q.8 |  |
| :--- | :--- |
| The ratio of the area of the inscribed circle to the area of the |  |
| circumscribed circle of an equilateral triangle is___ |  |
| (A) | $\frac{1}{8}$ |
| (B) | $\frac{1}{6}$ |
| (C) | $\frac{1}{4}$ |
| (D) | $\frac{1}{2}$ |


| Q.9 | Consider a square sheet of side 1 unit. The sheet is first folded along the <br> main diagonal. This is followed by a fold along its line of symmetry. The <br> resulting folded shape is again folded along its line of symmetry. The area <br> of each face of the final folded shape, in square units, equal to <br> (A) <br> $\frac{1}{4}$ <br> (B) <br> (C) <br> $\frac{1}{8}$ <br> (D) |
| :--- | :--- |

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Mechanical Engineering (ME, Set-2)

| Q.10 | The world is going through the worst pandemic in the past hundred years. <br> The air travel industry is facing a crisis, as the resulting quarantine <br> requirement for travelers led to weak demand. <br> In relation to the first sentence above, what does the second sentence do? |
| :--- | :--- |
| (A) | Restates an idea from the first sentence. |
| (B) | Second sentence entirely contradicts the first sentence. |
| (C) | The two statements are unrelated. |
| (D) | States an effect of the first sentence. |

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Mechanical Engineering (ME, Set-2)

## Mechanical Engineering (ME, Set-2)

Q. 1 - Q. 19 Multiple Choice Question (MCQ), carry ONE mark each (for each wrong answer: - 1/3).

| Q.1 | Consider an $n \times n$ matrix $A$ and a non-zero $n \times 1$ vector $p$. Their product <br> $A p=\alpha^{2} p$, where $\alpha \in \Re$ and $\alpha \notin\{-1,0,1\}$. Based on the given information, <br> the eigen value of $A^{2}$ is: |
| :--- | :--- |
| (A) | $\alpha$ |
| (B) | $\alpha^{2}$ |
| (C) | $\sqrt{ } \alpha$ |
| (D) | $\alpha^{4}$ |


| Q.2 | If the Laplace transform of a function $f(t)$ is given by $\frac{s+3}{(s+1)(s+2)}$ is |
| :--- | :--- |
| (A) | 0 |
| (B) | $\frac{1}{2}$ |
| (C) | 1 |
| (D) | $\frac{3}{2}$ |

Mechanical Engineering (ME, Set-2)

| Q.3 | The mean and variance, respectively, of a binomial distribution for $\boldsymbol{n}$ <br> independent trials with the probability of success as $\boldsymbol{p}$, are |
| :--- | :--- |
| (A) | $\sqrt{n p}, n p(1-2 p)$ |
| (B) | $\sqrt{n p}, \sqrt{n p(1-p)}$ |
| (C) | $n p, n p$ |
| (D) | $n p, n p(1-p)$ |


| Q.4 | The Cast Iron which possesses all the carbon in the combined form as <br> cementite is known as |
| :--- | :--- |
| (A) | Grey Cast Iron |
| (B) | Spheroidal Cast Iron |
| (C) | Malleable Cast Iron |
| (D) | White Cast Iron |


| Q.5 | The size distribution of the powder particles used in Powder Metallurgy <br> process can be determined by |
| :--- | :--- |
| (A) | Laser scattering |
| (B) | Laser reflection |
| (C) | Laser absorption |
| (D) | Laser penetration |

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Mechanical Engineering (ME, Set-2)

| Q.6 | In a CNC machine tool, the function of an interpolator is to generate |
| :--- | :--- |
| (A) | signal for the lubrication pump during machining |
| (B) | error signal for tool radius compensation during machining |
| (C) | NC code from the part drawing during post processing |
| (D) | reference signal prescribing the shape of the part to be machined |


| Q. 7 | The machining process that involves ablation is |
| :--- | :--- |
| (A) | Abrasive Jet Machining |
| (B) | Chemical Machining |
| (C) | Electrochemical Machining |
| (D) | Laser Beam Machining |


| Q. 8 | A PERT network has 9 activities on its critical path. The standard <br> deviation of each activity on the critical path is 3. The standard deviation of <br> the critical path is |
| :--- | :--- |
| (A) | 3 |
| (B) | 9 |
| (C) | 27 |
| (D) | 81 |

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Mechanical Engineering (ME, Set-2)

| Q.9 | The allowance provided in between a hole and a shaft is calculated from the <br> difference between |
| :--- | :--- |
| (A) | lower limit of the shaft and the upper limit of the hole |
| (B) | upper limit of the shaft and the upper limit of the hole |
| (C) | upper limit of the shaft and the lower limit of the hole |
| (D) | lower limit of the shaft and the lower limit of the hole |


| Q.10 | In forced convective heat transfer, Stanton number (St), Nusselt number <br> (Nu), Reynolds number (Re) and Prandtl number (Pr) are related as |
| ---: | :--- |
| (A) | $\mathrm{St}=\frac{\mathrm{Nu}}{\mathrm{Re} \mathrm{Pr}}$ |
| (B) | $\mathrm{St}=\frac{\mathrm{Nu} \mathrm{Pr}}{\mathrm{Re}}$ |
| (C) | $\mathrm{St}=\mathrm{Nu} \operatorname{Pr} \mathrm{Re}$ |
| (D) | $\mathrm{St}=\frac{\mathrm{Nu} \mathrm{Re}}{\mathrm{Pr}}$ |

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## Mechanical Engineering (ME, Set-2)

| Q.11 | For a two-dimensional, incompressible flow having velocity components $\boldsymbol{u}$ <br> and $\boldsymbol{v}$ in the $\boldsymbol{x}$ and $\boldsymbol{y}$ directions, respectively, the expression <br> can be simplified to <br> $\frac{\boldsymbol{\partial}\left(\boldsymbol{u}^{2}\right)}{\partial \boldsymbol{x}}+\frac{\boldsymbol{\partial ( \boldsymbol { u } \boldsymbol { v } )}}{\boldsymbol{\partial y}}$ |
| :--- | :--- |
| (A) | $u \frac{\partial u}{\partial x}+u \frac{\partial v}{\partial y}$ |
| (B) | $2 u \frac{\partial u}{\partial x}+u \frac{\partial v}{\partial y}$ |
| (C) | $2 u \frac{\partial u}{\partial x}+v \frac{\partial u}{\partial y}$ |
| (D) | $u \frac{\partial u}{\partial x}+v \frac{\partial u}{\partial y}$ |


| Q.12 | Which of the following is responsible for eddy viscosity (or turbulent <br> viscosity) in a turbulent boundary layer on a flat plate? |
| ---: | :--- |
| (A) | Nikuradse stresses |
| (B) | Reynolds stresses |
| (C) | Boussinesq stresses |
| (D) | Prandtl stresses |

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Mechanical Engineering (ME, Set-2)

| Q. 13 | A two dimensional flow has velocities in $\boldsymbol{x}$ and $\boldsymbol{y}$ directions given by $\boldsymbol{u}=$ <br> $\mathbf{2 x y t}$ and $\boldsymbol{v}=-\boldsymbol{y}^{2} \boldsymbol{t}$, where $\boldsymbol{t}$ denotes time. The equation for streamline <br> passing through $\boldsymbol{x}=\mathbf{1}, \boldsymbol{y}=\mathbf{1}$ is |
| :--- | :--- |
| (A) | $x^{2} y=1$ |
| (B) | $x y^{2}=1$ |
| (C) | $x^{2} y^{2}=1$ |
| (D) | $x / y^{2}=1$ |


| Q.14 | A plane truss $P Q R S\left(P Q=\boldsymbol{R S}\right.$, and $\left.\angle P Q R=\mathbf{9 0}^{\circ}\right)$ is shown in the figure. |
| :--- | :--- |
| (A) | $F \sqrt{2}$ (tensile) and $F$ (tensile) |
| (B) | $F \sqrt{2}$ (tensile) and $F$ (compressive) |
| (C) | $F$ (compressive) and $F \sqrt{2}$ (compressive) |
| (D) | $F$ (tensile) and $F \sqrt{2}$ (tensile) |

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Mechanical Engineering (ME, Set-2)

| Q.15 | Consider the mechanism shown in the figure. There is rolling contact <br> without slip between the disc and ground. <br> Select the correct statement about instantaneous centers in the mechanism. |
| :--- | :--- |
| (A) | Only points $P, Q$, and $S$ are instantaneous centers of mechanism |
| (B) | Only points $P, Q, S$ and $T$ are instantaneous centers of mechanism |
| (C) | Only points $P, Q, R, S$, and $U$ are instantaneous centers of mechanism |
| (D) | All points $P, Q, R, S, T$ and $U$ are instantaneous centers of mechanism |

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Mechanical Engineering (ME, Set-2)

| Q.16 | The controlling force curves $\mathrm{P}, \mathrm{Q}$ and R for a spring controlled governor are <br> shown in the figure, where $\boldsymbol{r}_{1}$ and $\boldsymbol{r}_{2}$ are any two radii of rotation. |
| :--- | :--- |
| (A) | P - Unstable; Q - Stable; R - Isochronous |
| (B) | P - Unstable; Q - Isochronous; R - Stable |
| (C) | $\mathrm{P}-$ Stable; Q - Isochronous; R - Unstable |
| (D) | P - Stable; Q - Unstable; R - Isochronous |


| Q.17 | The von Mises stress at a point in a body subjected to forces is proportional <br> to the square root of the |
| ---: | :--- |
| (A) | total strain energy per unit volume |
| (B) | plastic strain energy per unit volume |
| (C) | dilatational strain energy per unit volume |
| (D) | distortional strain energy per unit volume |

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Mechanical Engineering (ME, Set-2)

| Q.18 | Value of $\int_{\mathbf{4}}^{\mathbf{5 . 2}} \ln \boldsymbol{x} \boldsymbol{d} \boldsymbol{x}$ using Simpson's one-third rule with interval size $\mathbf{0 . 3}$ <br> is |
| :--- | :--- |
| (A) | 1.83 |
| (B) | 1.60 |
| (C) | 1.51 |
| (D) | 1.06 |


| Q. 19 | Value of $(\mathbf{1}+\boldsymbol{i})^{\mathbf{8}}$, where $\boldsymbol{i}=\sqrt{-\mathbf{1}}$, is equal to |
| :--- | :--- |
| (A) | 4 |
| (B) | 16 |
| (C) | $4 i$ |
| (D) | $16 i$ |

Graduate Aptitude Test in Engineering 2021

Mechanical Engineering (ME, Set-2)
Q. 20 - Q. 25 Numerical Answer Type (NAT), carry ONE mark each (no negative marks).

| Q. 20 | Consider adiabatic flow of air through a duct. At a given point in the duct, <br> velocity of air is $300 \mathrm{~m} / \mathrm{s}$, temperature is 330 K and pressure is 180 kPa |
| :--- | :--- |
| Assume that the air behaves as a perfect gas with constant |  |
| $c_{p}=1.005 \mathrm{~kJ} / \mathrm{kg} . \mathrm{K}$. The stagnation temperature at this point is __ |  |
| (round off to two decimal places). |  |

Q. 21 Consider an ideal vapour compression refrigeration cycle working on R -134a refrigerant. The COP of the cycle is $\mathbf{1 0}$ and the refrigeration capacity is $150 \mathrm{~kJ} / \mathrm{kg}$. The heat rejected by the refrigerant in the condenser is $\mathrm{kJ} / \mathrm{kg}$ (round off to the nearest integer).
Q. 22 A rigid tank of volume $50 \mathbf{m}^{\mathbf{3}}$ contains a pure substance as a saturated liquid vapour mixture at $\mathbf{4 0 0} \mathbf{~ k P a}$. Of the total mass of the mixture, $\mathbf{2 0 \%}$ mass is liquid and $80 \%$ mass is vapour. Properties at 400 kPa are: $T_{\text {sat }}=$ $143.61{ }^{\circ} \mathrm{C}, v_{f}=0.001084 \mathrm{~m}^{3} / \mathrm{kg}, v_{g}=0.46242 \mathrm{~m}^{3} / \mathrm{kg}$. The total mass of liquid vapour mixture in the tank is $\qquad$ kg (round off to the nearest integer).
Q. 23 An object is moving with a Mach number of 0.6 in an ideal gas environment, which is at a temperature of 350 K . The gas constant is $320 \mathrm{~J} / \mathrm{kg} . \mathrm{K}$ and ratio of specific heats is 1.3 . The speed of object is $\mathrm{m} / \mathrm{s}$ (round off to the nearest integer).
Q. 24 A column with one end fixed and one end free has a critical buckling load of 100 N . For the same column, if the free end is replaced with a pinned end then the critical buckling load will be $\qquad$ $\mathbf{N}$ (round off to the nearest integer).

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Mechanical Engineering (ME, Set-2)
Q. 25 A steel cubic block of side 200 mm is subjected to hydrostatic pressure of $250 \mathrm{~N} / \mathrm{mm}^{2}$. The elastic modulus is $2 \times 10^{5} \mathrm{~N} / \mathrm{mm}^{2}$ and Poisson ratio is 0.3 for steel. The side of the block is reduced by $\qquad$ mm (round off to two decimal places).

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Mechanical Engineering (ME, Set-2)
Q. 26 - Q. 34 Multiple Choice Question (MCQ), carry TWO mark each (for each wrong answer: - 2/3).

| Q.26 | The value of $\int_{0}^{\pi / 2} \int_{0}^{\cos \theta} r \sin \theta d r d \theta$ is |
| :--- | :--- |
| (A) | 0 |
| (B) | $\frac{1}{6}$ |
| (C) | $\frac{4}{3}$ |
| (D) | $\pi$ |


| Q.27 | Let the superscript $\boldsymbol{T}$ represent the transpose operation. Consider the function <br> $\boldsymbol{f}(\boldsymbol{x})=\frac{\mathbf{1}}{\mathbf{2}} \boldsymbol{\boldsymbol { x } ^ { \boldsymbol { T } } \boldsymbol { Q } \boldsymbol { x } - \boldsymbol { r } ^ { \boldsymbol { T } } \boldsymbol { x } \text { , where } \boldsymbol { x } \text { and } \boldsymbol { r } \text { are } \boldsymbol { n } \times \mathbf { 1 } \text { vectors and } \boldsymbol { Q } \text { is a }}$symmetric $\boldsymbol{n} \times \boldsymbol{n}$ matrix. The stationary point of $\boldsymbol{f}(\boldsymbol{x})$ is <br> (A)$Q^{T} r$ |
| :--- | :--- |
| (B) | $Q^{-1} r$ |
| (C) | $\frac{r}{r^{T} r}$ |
| (D) | $r$ |

Q. 28 Consider the following differential equation

$$
(1+y) \frac{d y}{d x}=y
$$

The solution of the equation that satisfies the condition $y(1)=1$ is
(A) $2 y e^{y}=e^{x}+e$
(B) $y^{2} e^{y}=e^{x}$
(C) $y e^{y}=e^{x}$
(D) $(1+y) e^{y}=2 e^{x}$

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Mechanical Engineering (ME, Set-2)

| Q. 29 | A factory produces $m(i=1,2, \ldots, m)$ products, each of which requires processing on $n(j=1,2, \ldots, n)$ workstations. Let $a_{i j}$ be the amount of processing time that one unit of the $i^{\text {th }}$ product requires on the $\boldsymbol{j}^{\boldsymbol{t h}}$ workstation. Let the revenue from selling one unit of the $i^{t h}$ product be $r_{i}$ and $h_{i}$ be the holding cost per unit per time period for the $i^{t h}$ product. The planning horizon consists of $T(t=1,2, \ldots, T)$ time periods. The minimum demand that must be satisfied in time period $t$ is $d_{i t}$, and the capacity of the $\boldsymbol{j}^{\boldsymbol{t h}}$ workstation in time period $t$ is $\boldsymbol{c}_{\boldsymbol{j} \boldsymbol{t}}$. Consider the aggregate planning formulation below, with decision variables $S_{i t}$ (amount of product $i$ sold in time period $t$ ), $X_{i t}$ (amount of product $i$ manufactured in time period $t$ ) and $I_{i t}$ (amount of product $i$ held in inventory at the end of time period $t$. $\begin{aligned} & \max \sum_{t=1}^{T} \sum_{i=1}^{m}\left(r_{i} S_{i t}-h_{i} I_{i t}\right) \\ & \text { subject to } \\ & S_{i t} \geq d_{i t} \forall i, t \\ & <\text { capacity constraint }> \\ & <\text { inventory balance constraint }> \\ & X_{i t}, S_{i t}, I_{i t} \geq 0 ; I_{i 0}=0 \end{aligned}$ <br> The capacity constraints and inventory balance constraints for this formulation are |
| :---: | :---: |
| (A) | $\sum_{i}^{m} a_{i j} X_{i t} \leq c_{j t} \forall j, t \quad$ and $\quad I_{i t}=I_{i, t-1}+X_{i t}-S_{i t} \quad \forall i, t$ |
| (B) | $\sum_{i}^{m} a_{i j} X_{i t} \leq c_{j t} \quad \forall i, t$ and $\quad I_{i t}=I_{i, t-1}+X_{i t}-d_{i t} \quad \forall i, t$ |
| (C) | $\sum_{i}^{m} a_{i j} X_{i t} \leq d_{i t} \quad \forall \quad i, t$ and $\quad I_{i t}=I_{i, t-1}+X_{i t}-S_{i t} \quad \forall i, t$ |
| (D) | $\sum_{i}^{m} a_{i j} X_{i t} \leq d_{i t} \quad \forall i, t \quad$ and $\quad I_{i t}=I_{i, t-1}+S_{i t}-X_{i t} \quad \forall i, t$ |

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Mechanical Engineering (ME, Set-2)

| Q. 30 | Ambient pressure, temperature, and relative humidity at a location are $101 \mathrm{kPa}, 300 \mathrm{~K}$, and $\mathbf{6 0 \%}$, respectively. The saturation pressure of water at 300 K is 3.6 kPa . The specific humidity of ambient air is $\qquad$ $\mathrm{g} / \mathrm{kg}$ of dry air. |
| :---: | :---: |
| (A) | 21.4 |
| (B) | 35.1 |
| (C) | 21.9 |
| (D) | 13.6 |


| Q. 31 | A plane frame $P Q R$ (fixed at $P$ and free at $R$ ) is shown in the figure. Both <br> members $(P Q$ and $Q R)$ have length, $L$, and flexural rigidity, $E$ I. Neglecting the <br> effect of axial stress and transverse shear, the horizontal deflection at free <br> end, $\boldsymbol{R}$, is |
| :--- | :--- |
| (A) | $\frac{5 F L^{3}}{3 E I}$ |
| (B) | $\frac{4 F L^{3}}{3 E I}$ |
| (C) | $\frac{2 F L^{3}}{3 E I}$ |
| (D) | $\frac{F L^{3}}{3 E I}$ |

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Mechanical Engineering (ME, Set-2)


Diameters of pulleys of belt drive and number of teeth $(T)$ on the gears 2 to 7 are indicated in the figure. The speed and direction of rotation of gear 7, respectively, are
(A) 255.68 rpm; clockwise
(B) 255.68 rpm ; anticlockwise
(C) 575.28 rpm ; clockwise
(D) 575.28 rpm ; anticlockwise

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Mechanical Engineering (ME, Set-2)

| Q. 33 | A machine of mass 100 kg is subjected to an external harmonic force with a frequency of $40 \mathrm{rad} / \mathrm{s}$. The designer decides to mount the machine on an isolator to reduce the force transmitted to the foundation. The isolator can be considered as a combination of stiffness $(K)$ and damper (damping factor, $\xi$ ) in parallel. The designer has the following four isolators: <br> 1) $K=640 \mathrm{kN} / \mathrm{m}, \xi=0.70$ <br> 2) $K=640 \mathrm{kN} / \mathrm{m}, \xi=0.07$ <br> 3) $K=22.5 \mathrm{kN} / \mathrm{m}, \xi=0.70$ <br> 4) $K=22.5 \mathrm{kN} / \mathrm{m}, \xi=0.07$ <br> Arrange the isolators in the ascending order of the force transmitted to the foundation. |
| :---: | :---: |
| (A) | 1-3-4-2 |
| (B) | 1-3-2-4 |
| (C) | 4-3-1-2 |
| (D) | 3-1-2-4 |

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Mechanical Engineering (ME, Set-2)

| Q.34 | Consider the system shown in the figure. A rope goes over a pulley. A mass, $\boldsymbol{m}$, <br> is hanging from the rope. A spring of stifness, $k$, is attached at one end of the <br> rope. Assume rope is inextensible, massless and there is no slip between pulley <br> and rope. |
| :--- | :--- |
| (A) | $\frac{k r^{2}}{J-m r^{2}}$ <br> is vibrating harmonically about its static equilibrium position. The natural <br> frequency of the system is |
| (B) | $\sqrt{\frac{k r^{2}}{J+m r^{2}}}$ |
| (C) | $\sqrt{k / m}$ |
| (D) | $\sqrt{\frac{k r^{2}}{J}}$ |

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Mechanical Engineering (ME, Set-2)
Q. 35 - Q. 55 Numerical Answer Type (NAT), carry TWO mark each (no negative marks).
Q. 35 Find the positive real root of $x^{3}-x-3=0$ using Newton-Raphson method. If the starting guess $\left(x_{0}\right)$ is 2 , the numerical value of the root after two iterations $\left(x_{2}\right)$ is $\qquad$ (round off to two decimal places).
Q. 36 Daily production capacity of a bearing manufacturing company is $\mathbf{3 0 0 0 0}$ bearings. The daily demand of the bearing is 15000 . The holding cost per year of keeping a bearing in the inventory is ₹ 20 . The setup cost for the production of a batch is ₹ $\mathbf{1 8 0 0}$. Assuming $\mathbf{3 0 0}$ working days in a year, the economic batch quantity in number of bearings is $\qquad$ (in integer).
Q. 37 A cast product of a particular material has dimensions $\mathbf{7 5} \mathbf{~ m m} \times \mathbf{1 2 5} \mathbf{~ m m} \times \mathbf{2 0}$ mm . The total solidification time for the cast product is found to be $\mathbf{2 . 0}$ minutes as calculated using Chvorinov's rule having the index, $\boldsymbol{n}=\mathbf{2}$. If under the identical casting conditions, the cast product shape is changed to a cylinder having diameter $=\mathbf{5 0} \mathbf{~ m m}$ and height $=\mathbf{5 0} \mathbf{~ m m}$, the total solidification time will be $\qquad$ minutes (round off to two decimal places).
Q. 38 A spot welding operation performed on two pieces of steel yielded a nugget with a diameter of 5 mm and a thickness of 1 mm . The welding time was 0.1 s . The melting energy for the steel is $20 \mathrm{~J} / \mathrm{mm}^{3}$. Assuming the heat conversion efficiency as $10 \%$, the power required for performing the spot welding operation is $\qquad$ kW (round off to two decimal places).

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Mechanical Engineering (ME, Set-2)
Q. 39 A surface grinding operation has been performed on a Cast Iron plate having dimensions 300 mm (length) $\times 10 \mathrm{~mm}$ (width) $\times 50 \mathrm{~mm}$ (height). The grinding was performed using an alumina wheel having a wheel diameter of 150 mm and wheel width of 12 mm . The grinding velocity used is $\mathbf{4 0} \mathrm{m} / \mathrm{s}$, table speed is 5 $\mathrm{m} / \mathrm{min}$, depth of cut per pass is $50 \mu \mathrm{~m}$ and the number of grinding passes is 20 . The average tangential and average normal force for each pass is found to be 40 N and 60 N respectively. The value of the specific grinding energy under the aforesaid grinding conditions is $\qquad$ $\mathrm{J} / \mathrm{mm}^{3}$ (round off to one decimal place).
Q. 40 In a pure orthogonal turning by a zero rake angle single point carbide cutting tool, the shear force has been computed to be 400 N . The cutting velocity, $V_{c}=100 \mathrm{~m} / \mathrm{min}$, depth of cut, $t=2.0 \mathrm{~mm}$, feed, $s_{0}=0.1 \mathrm{~mm} /$ revolution and chip velocity, $V_{f}=20 \mathrm{~m} / \mathrm{min}$, the shear strength, $\tau_{s}$ of the material will be MPa (round off to two decimal places).
Q. 41 The thickness, width and length of a metal slab are $50 \mathrm{~mm}, \mathbf{2 5 0} \mathbf{~ m m}$ and 3600 mm , respectively. A rolling operation on this slab reduces the thickness by $10 \%$ and increases the width by $3 \%$. The length of the rolled slab is mm (round off to one decimal place).
Q. 42 A 76.2 mm gauge block is used under one end of a 254 mm sine bar with roll diameter of $\mathbf{2 5 . 4} \mathbf{~ m m}$. The height of gauge blocks required at the other end of the sine bar to measure an angle of $30^{\circ}$ is $\qquad$ mm (round off to two decimal places).

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Q. 43 The demand and forecast of an item for five months are given in the table.

| Month | Demand | Forecast |
| :---: | :---: | :---: |
| April | 225 | 200 |
| May | 220 | 240 |
| June | 285 | 300 |
| July | 290 | 270 |
| August | 250 | 230 |

The Mean Absolute Percent Error (MAPE) in the forecast is $\qquad$ \% (round off to two decimal places)
Q. 44 A shell and tube heat exchanger is used as a steam condenser. Coolant water enters the tube at 300 K at a rate of $100 \mathrm{~kg} / \mathrm{s}$. The overall heat transfer coefficient is $1500 \mathrm{~W} / \mathrm{m}^{2} . \mathrm{K}$, and total heat transfer area is $400 \mathrm{~m}^{2}$. Steam condenses at a saturation temperature of 350 K . Assume that the specific heat of coolant water is $4000 \mathrm{~J} / \mathrm{kg} . \mathrm{K}$. The temperature of the coolant water coming out of the condenser is $\qquad$ K (round off to the nearest integer).
Q. 45 Ambient air flows over a heated slab having flat, top surface at $\boldsymbol{y}=0$. The local temperature (in Kelvin) profile within the thermal boundary layer is given by $T(y)=300+200 \exp (-5 y)$, where $y$ is the distance measured from the slab surface in meter. If the thermal conductivity of air is $1.0 \mathrm{~W} / \mathrm{m} . \mathrm{K}$ and that of the slab is $\mathbf{1 0 0} \mathbf{W} / \mathrm{m} . \mathrm{K}$, then the magnitude of temperature gradient $|d T / d y|$ within the slab at $y=0$ is $\qquad$ K/m (round off to the nearest integer).

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Q. 46 Water flows out from a large tank of cross-sectional area $A_{t}=1 \mathbf{m}^{2}$ through a small rounded orifice of cross-sectional area $A_{o}=1 \mathrm{~cm}^{2}$, located at $y=0$. Initially the water level, measured from $y=0$, is $H=1 \mathrm{~m}$. The acceleration due to gravity is $9.8 \mathrm{~m} / \mathrm{s}^{2}$.


Neglecting any losses, the time taken by water in the tank to reach a level of $y=H / 4$ is $\qquad$ seconds (round off to one decimal place).
Q. 47 Consider the open feed water heater (FWH) shown in the figure given below:


Specific enthalpy of steam at location 2 is $2624 \mathrm{~kJ} / \mathrm{kg}$, specific enthalpy of water at location 5 is $226.7 \mathrm{~kJ} / \mathrm{kg}$ and specific enthalpy of saturated water at location 6 is $708.6 \mathrm{~kJ} / \mathrm{kg}$. If the mass flow rate of water entering the open feed water heater (at location 5) is $100 \mathrm{~kg} / \mathrm{s}$ then the mass flow rate of steam at location 2 will be $\qquad$ $\mathrm{kg} / \mathrm{s}$ (round off to one decimal place).

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Mechanical Engineering (ME, Set-2)
Q. 48 A high velocity water jet of cross section area $=0.01 \mathrm{~m}^{2}$ and velocity $=\mathbf{3 5} \mathbf{~ m} / \mathrm{s}$ enters a pipe filled with stagnant water. The diameter of the pipe is 0.32 m . This high velocity water jet entrains additional water from the pipe and the total water leaves the pipe with a velocity $\mathbf{6 m} / \mathrm{s}$ as shown in the figure.


The flow rate of entrained water is $\qquad$ litres/s (round off to two decimal places).
Q. 49 A vertical shaft Francis turbine rotates at 300 rpm . The available head at the inlet to the turbine is $\mathbf{2 0 0} \mathbf{~ m}$. The tip speed of the rotor is $\mathbf{4 0} \mathbf{~ m} / \mathrm{s}$. Water leaves the runner of the turbine without whirl. Velocity at the exit of the draft tube is $3.5 \mathrm{~m} / \mathrm{s}$. The head losses in different components of the turbine are: (i) stator
 through the turbine is $20 \mathrm{~m}^{3} / \mathrm{s}$. Take $g=9.8 \mathrm{~m} / \mathrm{s}^{2}$. The hydraulic efficiency of the turbine is $\qquad$ \% (round off to one decimal place).

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Mechanical Engineering (ME, Set-2)
Q. 50 An adiabatic vortex tube, shown in the figure given below is supplied with $5 \mathrm{~kg} / \mathrm{s}$ of air (inlet 1) at 500 kPa and 300 K . Two separate streams of air are leaving the device from outlets 2 and 3. Hot air leaves the device at a rate of $3 \mathrm{~kg} / \mathrm{s}$ from outlet 2 at 100 kPa and 340 K , and $2 \mathrm{~kg} / \mathrm{s}$ of cold air stream is leaving the device from outlet 3 at 100 kPa and 240 K .


Assume constant specific heat of air is $1005 \mathrm{~J} / \mathrm{kg} . \mathrm{K}$ and gas constant is $287 \mathrm{~J} / \mathrm{kg} . \mathrm{K}$. There is no work transfer across the boundary of this device. The rate of entropy generation is $\qquad$ kW/K (round off to one decimal place).
Q. 51 A block of negligible mass rests on a surface that is inclined at $30^{\circ}$ to the horizontal plane as shown in the figure. When a vertical force of $\mathbf{9 0 0} \mathbf{N}$ and a horizontal force of $\mathbf{7 5 0} \mathbf{N}$ are applied, the block is just about to slide.


The coefficient of static friction between the block and surface is $\qquad$ (round off to two decimal places).

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Mechanical Engineering (ME, Set-2)
Q. 52 The wheels and axle system lying on a rough surface is shown in the figure.


Each wheel has diameter 0.8 m and mass 1 kg . Assume that the mass of the wheel is concentrated at rim and neglect the mass of the spokes. The diameter of axle is 0.2 m and its mass is 1.5 kg . Neglect the moment of inertia of the axle and assume $g=9.8 \mathrm{~m} / \mathrm{s}^{2}$. An effort of 10 N is applied on the axle in the horizontal direction shown at mid span of the axle. Assume that the wheels move on a horizontal surface without slip. The acceleration of the wheel axle system in horizontal direction is $\qquad$ $\mathrm{m} / \mathrm{s}^{2}$ (round off to one decimal place).
Q. 53 A cantilever beam with a uniform flexural rigidity $\left(E I=200 \times 10^{6} \mathrm{~N} . \mathrm{m}^{2}\right)$ is loaded with a concentrated force at its free end. The area of the bending moment diagram corresponding to the full length of the beam is $10000 \mathrm{~N} . \mathrm{m}^{2}$. The magnitude of the slope of the beam at its free end is $\qquad$ micro radian (round off to the nearest integer).
Q. 54 The torque provided by an engine is given by $T(\theta)=12000+2500 \sin (2 \theta)$ N.m, where $\theta$ is the angle turned by the crank from inner dead center. The mean speed of the engine is $\mathbf{2 0 0} \mathbf{~ r p m}$ and it drives a machine that provides a constant resisting torque. If variation of the speed from the mean speed is not to exceed $\pm 0.5 \%$, the minimum mass moment of inertia of the flywheel should be kg. $\mathrm{m}^{2}$ (round off to the nearest integer).

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Mechanical Engineering (ME, Set-2)
Q. 55 The figure shows the relationship between fatigue strength ( $S$ ) and fatigue life $(N)$ of a material. The fatigue strength of the material for a life of 1000 cycles is 450 MPa , while its fatigue strength for a life of $10^{6}$ cycles is 150 MPa .


The life of a cylindrical shaft made of this material subjected to an alternating stress of $\mathbf{2 0 0} \mathbf{~ M P a}$ will then be $\qquad$ cycles (round off to the nearest integer).

## END OF THE QUESTION PAPER

