# Graduate Aptitude Test in Engineering 2021 Organising Institute - IIT Bombay 

Electrical Engineering (EE)

## General Aptitude (GA)

Q. 1 - Q. 5 Multiple Choice Question (MCQ), carry ONE mark each (for each wrong answer: - 1/3).

| Q.1 | The people <br> of society. |
| ---: | :--- |
| (A) | whore at the demonstration were from all sections |
| (B) | which |
| (C) | who |
| (D) | whom |

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Q. 2

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| Q. 3 | For a regular polygon having 10 sides, the interior angle between the sides <br> of the polygon, in degrees, is: |
| :--- | :--- |
| (A) | 396 |
| (B) | 324 |
| (C) | 216 |
| (D) | 144 |


| Q. 4 | Which one of the following numbers is exactly divisible by $\left(11^{13}+1\right) ?$ |
| :--- | :--- |
| (A) | $11^{26}+1$ |
| (B) | $11^{33}+1$ |
| (C) | $11^{39}-1$ |
| (D) | $11^{52}-1$ |


| Q. 5 | Oasis is to sand as island is to <br> Which one of the following options maintains a similar logical relation in <br> the above sentence? |
| ---: | :--- |
| (A) | Stone |
| (B) | Land |
| (C) | Water |
| (D) | Mountain |

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Q. 6 - Q. 10 Multiple Choice Question (MCQ), carry TWO marks each (for each wrong answer: - 2/3).

| Q.6 | The importance of sleep is often overlooked by students when they are <br> preparing for exams. Research has consistently shown that sleep deprivation <br> greatly reduces the ability to recall the material learnt. Hence, cutting down <br> on sleep to study longer hours can be counterproductive. <br> Which one of the following statements is the CORRECT inference from the <br> above passage? |
| ---: | :--- |
| (A) | Sleeping well alone is enough to prepare for an exam. Studying has lesser <br> benefit. |
| (B) | Students are efficient and are not wrong in thinking that sleep is a waste of time. |
| (C) | If a student is extremely well prepared for an exam, he needs little or no sleep. |
| (D) | To do well in an exam, adequate sleep must be part of the preparation. |


| Q. 7 |  |
| :--- | :--- |
| (A) | 12.50 |
| (B) | 6.25 |
| In the figure shown above, each inside square is formed by joining the |  |
| square (shaded) as shown, in cm ${ }^{2}$ is: |  |
| (C) | 3.125 |
| (D) | 1.5625 |

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| Q.8 | Let $X$ be a continuous random variable denoting the temperature measured. <br> The range of temperature is $[\mathbf{0 , 1 0 0 ]}$ degree Celsius and let the probability <br> density function of $\boldsymbol{X}$ be $f(\boldsymbol{x})=\mathbf{0 . 0 1}$ for $\mathbf{0} \leq \boldsymbol{X} \leq \mathbf{1 0 0}$. <br> The mean of $X$ is |
| :--- | :--- |
| (A) | 2.5 |
| (B) | 5.0 |
| (C) | 25.0 |
| (D) | 50.0 |

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| Q. 9 |  <br> The number of students passing or failing in an exam for a particular subject are presented in the bar chart above. Students who pass the exam cannot appear for the exam again. Students who fail the exam in the first attempt must appear for the exam in the following year. Students always pass the exam in their second attempt. <br> The number of students who took the exam for the first time in the year 2 and the year 3 respectively, are $\qquad$ |
| :---: | :---: |
| A) | 65 and 53 |
| (B) | 60 and 50 |
| (C) | 55 and 53 |
| (D) | 55 and 48 |

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| Q.10 | Seven cars P, Q, R, S, T, U and V are parked in a row not necessarily in that <br> order. The cars T and U should be parked next to each other. The cars S and <br> V also should be parked next to each other, whereas P and Q cannot be <br> parked next to each other. Q and S must be parked next to each other. R is <br> parked to the immediate right of V. T is parked to the left of U. <br> Based on the above statements, the only INCORRECT option given below <br> is: |
| ---: | :--- |
| (A) | There are two cars parked in between Q and V. |
| (B) | Q and R are not parked together. |
| (C) | $V$ is the only car parked in between $S$ and $R$. |
| (D) | Car P is parked at the extreme end. |

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Q. 1 - Q. 12 Multiple Choice Question (MCQ), carry ONE mark each (for each wrong answer: - 1/3).

| Q.1 | Let $p$ and $q$ be real numbers such that $p^{2}+q^{2}=1$. The eigenvalues of |
| :--- | :--- |
| the matrix $\left[\begin{array}{cc}p & q \\ q & -p\end{array}\right]$ are |  |
| (A) | 1 and 1 |
| (B) | 1 and -1 |
| (C) | $j$ and $-j$ |
| (D) | $p q$ and $-p q$ |


| Q. 2 | Let $p(z)=z^{3}+(1+j) z^{2}+(2+j) z+3$, where $z$ is a complex number. <br> Which one of the following is true? |
| ---: | :--- |
| (A) | conjugate $\{p(z)\}=p($ conjugate $\{z\})$ for all $z$ |
| (B) | The sum of the roots of $p(z)=0$ is a real number |
| (C) | The complex roots of the equation $p(z)=0$ come in conjugate pairs |
| (D) | All the roots cannot be real |

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| Q. 3 | Let $f(x)$ be a real-valued function such that $f^{\prime}\left(x_{0}\right)=0$ for some |
| ---: | :--- |
| $x_{0} \in(0,1)$, and $f^{\prime \prime}(x)>0$ for all $x \in(0,1)$. Then $f(x)$ has |  |
| (A) | no local minimum in $(0,1)$ |
| (B) | one local maximum in $(0,1)$ |
| (C) | exactly one local minimum in $(0,1)$ |
| (D) | two distinct local minima in $(0,1)$ |


| Q. 4 | For the network shown, the equivalent Thevenin voltage and Thevenin <br> impedance as seen across terminals 'ab' is |
| :--- | :--- |
| (A) 10 V in series with $12 \Omega$ |  |
| (B) 65 V in series with $15 \Omega$ |  |
| (C) 50 V in series with $2 \Omega$ |  |
| (D) 35 V in series with $2 \Omega$ |  |


| Q. 5 | Which one of the following vector functions represents a magnetic field <br> $\overrightarrow{\mathbf{B}}$ ? ( $\hat{\mathrm{x}}, \hat{y}$, and $\hat{z}$ are unit vectors along $\mathbf{x}$-axis, $\mathbf{y}$-axis, and z-axis, <br> respectively) |
| :--- | :--- |
| (A) | $10 x \hat{\mathrm{x}}+20 y \hat{\mathrm{y}}-30 z \hat{\mathrm{z}}$ |
| (B) | $10 y \hat{\mathrm{x}}+20 x \hat{\mathrm{y}}-10 z \hat{\mathrm{z}}$ |
| (C) | $10 z \hat{\mathrm{x}}+20 y \hat{\mathrm{y}}-30 x \hat{\mathrm{z}}$ |
| (D) | $10 x \hat{\mathrm{x}}-30 z \hat{\mathrm{y}}+20 y \hat{z}$ |

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| Q.6 | If the input $x(t)$ and output $y(t)$ of a system are related as <br> $y(t)=\max (0, x(t))$, then the system is |
| :--- | :--- |
| (A) | linear and time-variant |
| (B) | linear and time-invariant |
| (C) | non-linear and time-variant |
| (D) | non-linear and time-invariant |


| Q. 7 | Two discrete-time linear time-invariant systems with impulse responses <br> $h_{1}[n]=\delta[n-1]+\delta[n+1]$ and $h_{2}[n]=\delta[n]+\delta[n-1]$ are connected in cascade, <br> where $\delta[n]$ is the Kronecker delta. The impulse response of the cascaded <br> system is |
| :--- | :--- |
| (A) | $\delta[n-2]+\delta[n+1]$ |
| (B) | $\delta[n-1] \delta[n]+\delta[n+1] \delta[n-1]$ |
| (C) | $\delta[n-2]+\delta[n-1]+\delta[n]+\delta[n+1]$ |
| (D) | $\delta[n] \delta[n-1]+\delta[n-2] \delta[n+1]$ |

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| Q. 8 | Consider the table given: |  |  |
| :---: | :---: | :---: | :---: |
|  | Constructional feature | Machine type | Mitigation |
|  | (P) Damper bars | (S) Induction motor | (X) Hunting |
|  | (Q) Skewed rotor slots | (T) Transformer | (Y) Magnetic locking |
|  | (R) Compensating winding | (U) Synchronous machine | (Z) Armature reaction |
|  |  | (V) DC machine |  |
|  | The correct combination that relates the constructional feature, machine type and mitigation is |  |  |
| (A) | P-V-X, Q-U-Z, R-T-Y |  |  |
| (B) | P-U-X, Q-S-Y, R-V-Z |  |  |
| (C) | P-T-Y, Q-V-Z, R-S-X |  |  |
| (D) | P-U-X, Q-V-Y, R-T-Z |  |  |


| Q. 9 | Consider a power system consisting of $\boldsymbol{N}$ number of buses. Buses in this <br> power system are categorized into slack bus, PV buses and PQ buses for load <br> flow study. The number of PQ buses is $N_{L}$. The balanced Newton-Raphson <br> method is used to carry out load flow study in polar form. $\boldsymbol{H}, \boldsymbol{S}, \boldsymbol{M}$, and $\boldsymbol{R}$ are <br> sub-matrices of the Jacobian matrix $\boldsymbol{J}$ as shown below: <br> $\left[\begin{array}{l}\Delta P \\ \Delta Q\end{array}\right]=J\left[\begin{array}{l}\Delta \delta \\ \Delta V\end{array}\right]$, where $J=\left[\begin{array}{ll}H & S \\ M & R\end{array}\right]$ <br> The dimension of the sub-matrix $\boldsymbol{M}$ is |
| :--- | :--- |
| (A) | $N_{L} \times(N-1)$ |
| (B) | $(N-1) \times\left(N-1-N_{L}\right)$ |
| (C) | $N_{L} \times\left(N-1+N_{L}\right)$ |
| (D) | $(N-1) \times\left(N-1+N_{L}\right)$ |

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| Q.10 | Two generators have cost functions $\boldsymbol{F}_{\mathbf{1}}$ and $\boldsymbol{F}_{2}$. Their incremental-cost <br> characteristics are <br> $\frac{d F_{1}}{d P_{1}}=40+0.2 P_{1}$ <br> $\frac{d F_{2}}{d P_{2}}=32+0.4 P_{2}$ <br> They need to deliver a combined load of 260 MW. Ignoring the network <br> losses, for economic operation, the generations $P_{1}$ and $P_{2}$ (in MW) are |
| :--- | :--- |
| (A) | $P_{1}=P_{2}=130$ |
| (B) | $P_{1}=160, P_{2}=100$ |
| (C) | $P_{1}=140, P_{2}=120$ |
| (D) | $P_{1}=120, P_{2}=140$ |



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| Q.12 | Inductance is measured by |
| ---: | :--- |
| (A) | Schering bridge |
| (B) | Maxwell bridge |
| (C) | Kelvin bridge |
| (D) | Wien bridge |

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Q. 13 - Q. 25 Numerical Answer Type (NAT), carry ONE mark each (no negative marks).
Q. 13 Suppose the circles $x^{2}+y^{2}=1$ and $(x-1)^{2}+(y-1)^{2}=r^{2}$ intersect each other orthogonally at the point $(u, v)$. Then $u+v=$ $\qquad$ .
Q. 14 In the given circuit, the value of capacitor $C$ that makes current $I=0$ is
$\qquad$ $\mu \mathrm{F}$.

Q. $15 \quad$ Two single-core power cables have total conductor resistances of $0.7 \Omega$ and $0.5 \Omega$, respectively, and their insulation resistances (between core and sheath) are $600 \mathrm{M} \Omega$ and $900 \mathrm{M} \Omega$, respectively. When the two cables are joined in series, the ratio of insulation resistance to conductor resistance is
$\qquad$ $\times 10^{6}$.
Q. 16 In the given circuit, for voltage $V_{y}$ to be zero, the value of $\boldsymbol{\beta}$ should be
$\qquad$ . (Round off to 2 decimal places).


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Q. 17 A $1 \mu$ Cpoint charge is held at the origin of a cartesian coordinate system. If a second point charge of $10 \mu \mathrm{C}$ is moved from $(0,10,0)$ to $(5,5,5)$ and subsequently to $(5,0,0)$, then the total work done is $\qquad$ mJ.
(Round off to 2 decimal places).
Take $\frac{1}{4 \pi \varepsilon_{o}}=9 \times 10^{9}$ in SI units. All coordinates are in meters.
Q. 18 The power input to a $500 \mathrm{~V}, 50 \mathrm{~Hz}$, 6-pole, 3-phase induction motor running at 975 RPM is 40 kW . The total stator losses are 1 kW . If the total friction and windage losses are 2.025 kW , then the efficiency is
$\qquad$ $\%$.
Q. 19

An alternator with internal voltage of $1 \angle \delta_{1} \mathbf{p}$.u and synchronous reactance of 0.4 p .u is connected by a transmission line of reactance 0.1 p.u to a synchronous motor having synchronous reactance $0.35 \mathrm{p} . \mathrm{u}$ and internal voltage of $0.85 \angle \delta_{2}$ p.u. If the real power supplied by the alternator is $\mathbf{0 . 8 6 6}$ p.u, then $\left(\delta_{1}-\delta_{2}\right)$ is $\qquad$ degrees. (Round off to $\mathbf{2}$ decimal places.)
(Machines are of non-salient type. Neglect resistances.)


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Q. 21 A signal generator having a source resistance of $50 \Omega$ is set to generate a 1 kHz sinewave. Open circuit terminal voltage is 10 V peak-to-peak.
Connecting a capacitor across the terminals reduces the voltage to 8 V peak-to-peak. The value of this capacitor is $\qquad$ $\mu \mathrm{F}$. (Round off to 2 decimal places.)

```
Q. 22 A 16-bit synchronous binary up-counter is clocked with a frequency \(f_{\text {CLK }}\).
The two most significant bits are OR-ed together to form an output Y.
Measurements show that \(Y\) is periodic, and the duration for which \(Y\) remains high in each period is
24 ms . The clock frequency \(f_{\text {CLK }}\) is
``` \(\qquad\)
``` MHz.
(Round off to 2 decimal places.)
```



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Q. 26 - Q. 37 Multiple Choice Question (MCQ), carry TWO mark each (for each wrong answer: - 2/3).

| Q.26 | In the open interval $(0,1)$, the polynomial $p(x)=x^{4}-4 x^{3}+2$ has |
| ---: | :--- |
| (A) | two real roots |
| (B) | one real root |
| (C) | three real roots |
| (D) | no real roots |


| Q.27 | Suppose the probability that a coin toss shows "head" is $p$, where <br> $0<p<1$. The coin is tossed repeatedly until the first "head" appears. <br> The expected number of tosses required is |
| ---: | :--- |
| (A) | $p /(1-p)$ |
| (B) | $(1-p) / p$ |
| (C) | $1 / p$ |
| (D) | $1 / p^{2}$ |


| Q. 28 | Let $(-1-j),(3-j),(3+j)$ and $(-1+j)$ be the vertices of a rectangle $C$ <br> in the complex plane. Assuming that $C$ is traversed in counter-clockwise <br> direction, the value of the contour integral $\oint_{C} \frac{d z}{z^{2}(z-4)}$ is |
| :--- | :--- |
| (A) | $j \pi / 2$ |
| (B) | 0 |
| (C) | $-j \pi / 8$ |
| (D) | $j \pi / 16$ |

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| Q.29 | In the circuit, switch ' $\mathbf{S}$ ' is in the closed position for a very long time. If the <br> switch is opened at time $\mathrm{t}=0$, then $\mathrm{i}_{\mathrm{L}}(\mathrm{t})$ in amperes, for $\mathrm{t} \geq 0$ is |
| :--- | :--- |
| (A) $8 e^{-10 \mathrm{t}}$ |  |
| (B) | 10 |
| (C) | $8+2 e^{-10 \mathrm{t}}$ |
| (D) | $10\left(1-e^{-2 \mathrm{t}}\right)$ |


| Q. 30 | The input impedance, $Z_{i n}(s)$, for the network shown is |
| :--- | :--- |
| (A) | $\frac{23 s^{2}+46 s+20}{4 s+5}$ |
| (B) | $6 s+4$ |
| (C) | $7 s+4$ |
| (D) | $\frac{25 s^{2}+46 s+20}{4 s+5}$ |

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| Q.31 | The causal signal with z-transform $z^{2}(z-a)^{-2}$ is <br> $(u[n]$ is the unit step signal) |
| :--- | :--- |
| (A) | $a^{2 n} u[n]$ |
| (B) | $(n+1) a^{n} u[n]$ |
| (C) | $n^{-1} a^{n} u[n]$ |
| (D) | $n^{2} a^{n} u[n]$ |


| Q.32 | Let $f(t)$ be an even function, i.e. $f(-t)=f(t)$ for all $t$. Let the Fourier |
| :--- | :--- |
| transform of $f(t)$ be defined as $F(\omega)=\int_{-\infty}^{\infty} f(t) e^{-j \omega t} d t$. Suppose |  |
|  | $\frac{d F(\omega)}{d \omega}=-\omega F(\omega)$ for all $\omega$, and $F(0)=1$. Then |
| (A) | $f(0)<1$ |
| (B) | $f(0)>1$ |
| (C) | $f(0)=1$ |
| (D) | $f(0)=0$ |


| Q.33 | In a single-phase transformer, the total iron loss is 2500 W at nominal <br> voltage of 440 V and frequency 50 Hz . The total iron loss is 850 W at $\mathbf{2 2 0} \mathbf{~ V}$ <br> and 25 Hz . Then, at nominal voltage and frequency, the hysteresis loss and <br> eddy current loss respectively are |
| :--- | :--- |
| (A) | 1600 W and 900 W |
| (B) | 900 W and 1600 W |
| (C) | 250 W and 600 W |
| (D) | 600 W and 250 W |

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| Q. 34 | In the figure shown, self-impedances of the two transmission lines are $\mathbf{1 . 5 j}$ p.u each, and $\mathbf{Z}_{\mathrm{m}}=0.5 \mathrm{j}$ p.u is the mutual impedance. Bus voltages shown in the figure are in p.u. Given that $\delta>0$, the maximum steady-state real power that can be transferred in p.u from Bus-1 to Bus-2 is |
| :---: | :---: |
| (A) | $\|\mathrm{E}\|\|\mathrm{V}\|$ |
| (B) | $\frac{\|\mathrm{E}\|\|\mathrm{V}\|}{2}$ |
| (C) | $2\|\mathrm{E}\|\|\mathrm{V}\|$ |
| (D) | $\frac{3\|\mathrm{E}\|\|\mathrm{V}\|}{2}$ |

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| Q. 35 | A 3-Bus network is shown. Consider generators as ideal voltage sources. If rows 1, 2 and 3 of the $Y_{\text {Bus }}$ matrix correspond to Bus 1, 2 and 3, respectively, then $Y_{\text {Bus }}$ of the network is |
| :---: | :---: |
| (A) | $\left[\begin{array}{ccc}-4 j & j & j \\ j & -4 j & j \\ j & j & -4 j\end{array}\right] \quad$ (B) $\left[\begin{array}{ccc}-4 j & 2 j & 2 j \\ 2 j & -4 j & 2 j \\ 2 j & 2 j & -4 j\end{array}\right]$ |
| (C) | $\left[\begin{array}{ccc}-\frac{3}{4} \mathrm{j} & \frac{1}{4} \mathrm{j} & \frac{1}{4} \mathrm{j} \\ \frac{1}{4} \mathrm{j} & -\frac{3}{4} \mathrm{j} & \frac{1}{4} \mathrm{j} \\ \frac{1}{4} \mathrm{j} & \frac{1}{4} \mathrm{j} & -\frac{3}{4} \mathrm{j}\end{array}\right] \quad$ (D) $\left[\begin{array}{ccc}-\frac{1}{2} \mathrm{j} & \frac{1}{4} \mathrm{j} & \frac{1}{4} \mathrm{j} \\ \frac{1}{4} \mathrm{j} & -\frac{1}{2} \mathrm{j} & \frac{1}{4} \mathrm{j} \\ \frac{1}{4} \mathrm{j} & \frac{1}{4} \mathrm{j} & -\frac{1}{2} \mathrm{j}\end{array}\right]$ |


| Q.36 | Suppose $I_{A}, I_{B}$ and $I_{C}$ are a set of unbalanced current phasors in a three- <br> phase system. The phase-B zero-sequence current $I_{B 0}=0.1 \angle 0^{\circ}$ p.u. If <br> phase-A current $I_{A}=1.1 \angle 0^{\circ}$ p.u and phase-C current $I_{C}=\left(1 \angle 120^{\circ}+0.1\right)$ p.u, <br> then $I_{B}$ in p.u is |
| :--- | :--- |
| (A) | $1 \angle 240^{\circ}-0.1 \angle 0^{\circ}$ |
| (B) | $1.1 \angle 240^{\circ}-0.1 \angle 0^{\circ}$ |
| (C) | $1.1 \angle-120^{\circ}+0.1 \angle 0^{\circ}$ |
| (D) | $1 \angle-120^{\circ}+0.1 \angle 0^{\circ}$ |

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| Q. 37 | A counter is constructed with three $\mathbf{D}$ flip-flops. The input-output pairs are named ( $D_{0}, \mathbf{Q}_{0}$ ), ( $\left.D_{1}, Q_{1}\right)$, and ( $D_{2}, \mathbf{Q}_{2}$ ), where the subscript 0 denotes the least significant bit. The output sequence is desired to be the Gray-code sequence $000,001,011,010,110,111,101$, and 100 , repeating periodically. Note that the bits are listed in the $\mathbf{Q}_{2} \mathbf{Q}_{1} \mathbf{Q}_{0}$ format. The combinational logic expression for $D_{1}$ is |
| :---: | :---: |
| (A) | $Q_{2} Q_{1} Q_{0}$ |
| (B) | $\mathrm{Q}_{2} \mathrm{Q}_{0}+\mathrm{Q}_{1} \overline{\mathrm{Q}}_{0}$ |
| (C) | $\bar{Q}_{2} \mathrm{Q}_{0}+\mathrm{Q}_{1} \overline{\mathrm{Q}}_{0}$ |
| (D) | $\mathrm{Q}_{2} \mathrm{Q}_{1}+\bar{Q}_{2} \bar{Q}_{1}$ |

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Q. 38 - Q. 55 Numerical Answer Type (NAT), carry TWO mark each (no negative marks).

## Q. 38

Let $\mathbf{A}$ be a $10 \times 10$ matrix such that $\mathbf{A}^{5}$ is a null matrix, and let $I$ be the $10 \times 10$ identity matrix. The determinant of $\mathbf{A}+\mathbf{I}$ is $\qquad$ -.

| Q. 39 | A three-phase balanced voltage is applied to the load shown. The phase <br> sequence is RYB . The ratio $\frac{\left\|\mathrm{I}_{\mathrm{B}}\right\|}{\left\|\mathrm{I}_{\mathrm{R}}\right\|}$ is__. |
| :--- | :--- |


| Q. 40 | In the given circuit, for maximum power to be delivered to $R_{L}$, its value <br> should be $\boldsymbol{\Omega} \mathbf{\Omega}$ <br> (Round off to 2 decimal places.) |
| :--- | :--- |

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| Q. 41 | One coulomb of point charge moving with a uniform velocity $10 \hat{\mathrm{x}} \mathrm{m} / \mathrm{s}$ <br> enters the region $x \geq 0$ having a magnetic flux density <br> $\vec{B}=(10 y \hat{\mathrm{x}}+10 x \hat{\mathrm{y}}+10 \hat{\mathrm{z}}) \mathrm{T}$. The magnitude of force on the charge at <br> $x=0^{+}$is $\quad \mathrm{N}$. <br> $(\hat{\mathrm{x}}, \hat{\mathrm{y}}$, and $\hat{\mathrm{z}}$ are unit vectors along x-axis, y-axis, and z-axis, <br> respectively. $)$ |
| :--- | :--- |


| Q.42 | Consider a large parallel plate capacitor. The gap $d$ between the two plates <br> is filled entirely with a dielectric slab of relative permittivity 5 . The plates <br> are initially charged to a potential difference of $V$ volts and then <br> disconnected from the source. If the dielectric slab is pulled out completely, <br> then the ratio of the new electric field $E_{2}$ in the gap to the original electric <br> field $E_{1}$ is |
| :--- | :--- |


| Q. 43 | Consider a continuous-time signal $x(t)$ defined by $x(t)=0$ for $\|t\|>1$, and $x(t)=1-\|t\|$ for $\|t\| \leq 1$. Let the Fourier transform of $x(t)$ be defined as $X(\omega)=\int_{-\infty}^{\infty} x(t) e^{-j \omega t} d t$. The maximum magnitude of $X(\omega)$ is |
| :---: | :---: |


| Q.44 | A belt-driven DC shunt generator running at 300 RPM delivers 100 kW to <br> a 200 V DC grid. It continues to run as a motor when the belt breaks, <br> taking 10 kW from the DC grid. The armature resistance is $0.025 \Omega$, field <br> resistance is $50 \Omega$, and brush drop is 2 V . Ignoring armature reaction, the <br> speed of the motor is <br> RPM. (Round off to 2 decimal places.) |
| :--- | :--- |

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Q. 45 An 8-pole, 50 Hz , three-phase, slip-ring induction motor has an effective rotor resistance of $0.08 \Omega$ per phase. Its speed at maximum torque is $\mathbf{6 5 0}$ RPM. The additional resistance per phase that must be inserted in the rotor to achieve maximum torque at start is $\qquad$ $\Omega$. (Round off to 2 decimal places.) Neglect magnetizing current and stator leakage impedance. Consider equivalent circuit parameters referred to stator.


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## Electrical Engineering (EE)

| Q. 47 | In the given figure, plant $G_{p}(s)=\frac{2.2}{(1+0.1 \mathrm{~s})(1+0.4 \mathrm{~s})(1+1.2 \mathrm{~s})}$ and compensator $G_{c}(s)=K\left(\frac{1+T_{1} s}{1+T_{2} s}\right)$. The external disturbance input is $\mathbf{D}(\mathrm{s})$. It is desired that when the disturbance is a unit step, the steady-state error should not exceed 0.1 unit. The minimum value of $K$ is $\qquad$ (Round off to 2 decimal places.) |
| :---: | :---: |
|  |  |


| Q. 48 | The waveform shown in solid line is obtained by clipping a full-wave rectified sinusoid (shown dashed). The ratio of the RMS value of the fullwave rectified waveform to the RMS value of the clipped waveform is $\qquad$ <br> (Round off to 2 decimal places.) |
| :---: | :---: |

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## Electrical Engineering (EE)

| Q. 49 | The state space representation of a first-order system is given as |
| :--- | :--- |
|  | $\dot{x}=-x+u$ |
| $y=x$ |  |
|  | where, $x$ is the state variable, $u$ is the control input and $y$ is the <br> controlled output. Let $u=-K x$ be the control law, where $K$ is the <br> controller gain. To place a closed-loop pole at -2, the value of $K$ is |
|  |  |


| Q.50 | An air-core radio-frequency transformer as shown has a primary winding <br> and a secondary winding. The mutual inductance M between the windings <br> of the transformer is <br> (Round off to 2 decimal places.) |
| :--- | :--- |


| Q.51 | A 100 Hz square wave, switching between 0 V and 5 V , is applied to a CR <br> high-pass filter circuit as shown. The output voltage waveform across the <br> resistor is 6.2 V peak-to-peak. If the resistance R is $820 \Omega$, then the value C <br> is $\mu \mathrm{F}$. <br> (Round off to 2 decimal places.) |
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## Electrical Engineering (EE)

| Q. 52 | A CMOS Schmitt-trigger inverter has a low output level of 0 V and a high <br> output level of 5 V . It has input thresholds of 1.6 V and 2.4 V . The input <br> capacitance and output resistance of the Schmitt-trigger are negligible. The <br> frequency of the oscillator shown is <br> (Round off to 2 decimal places.) |
| :--- | :--- |


| Q. 53 | Consider the boost converter shown. Switch Q is operating at 25 kHz with <br> a duty cycle of 0.6 . Assume the diode and switch to be ideal. Under steady- <br> state condition, the average resistance $\mathrm{R}_{\text {in }}$ as seen by the source is <br> $\frac{\Omega .}{\text { (Round off to } 2 \text { decimal places.) }}$ |
| :--- | :--- |

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## Electrical Engineering (EE)



END OF THE QUESTION PAPER

