## Graduate Aptitude Test in Engineering 2021 Organising Institute - IIT Bombay

Computer Science and Information Technology (CS, Set-2)

## General Aptitude (GA)

Q. 1 - Q. 5 Multiple Choice Question (MCQ), carry ONE mark each (for each wrong answer: - 1/3).

| Q.1 | Gauri said that she can play the keyboard___ her sister. |
| ---: | :--- |
|  | (A) |
| (B) | as well as |
| (C) | as better as nicest as |
| (D) | as worse as |

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| Q. 2 | A transparent square sheet shown above is folded along the dotted line. The folded sheet will look like $\qquad$ . |
| :---: | :---: |
| (A) |  |
| (B) |  |
| (C) |  |
| (D) |  |

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| Q. 3 | If $\theta$ is the angle, in degrees, between the longest diagonal of the cube and any <br> one of the edges of the cube, then, $\cos \theta=$ |
| :--- | :--- |
| (A) | $\frac{1}{2}$ |
| (B) $\frac{1}{\sqrt{3}}$ |  |
| (C) $\frac{1}{\sqrt{2}}$ |  |
| (D) $\frac{\sqrt{3}}{2}$ |  |


| Q. 4 | If $\left(x-\frac{1}{2}\right)^{2}-\left(x-\frac{3}{2}\right)^{2}=x+2$, then the value of $x$ is: |
| :--- | :--- |
| (A) | 2 |
| (B) | 4 |
| (C) | 6 |
| (D) | 8 |

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| Q.5 | Pen : Write :: Knife: __ |
| ---: | :--- |
| Which one of the following options maintains a similar logical relation in the |  |
| above? |  |$\quad$| (A) | Vegetables |
| ---: | :--- |
| (B) | Sharp |
| (C) | Cut |
| (D) | Blunt |

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## Computer Science and Information Technology (CS, Set-2)

Q. 6 - Q. 10 Multiple Choice Question (MCQ), carry TWO marks each (for each wrong answer: - 2/3).

| Q.6 | Listening to music during exercise improves exercise performance and reduces <br> discomfort. Scientists researched whether listening to music while studying can <br> help students learn better and the results were inconclusive. Students who needed <br> external stimulation for studying fared worse while students who did not need <br> any external stimulation benefited from music. <br> Which one of the following statements is the CORRECT inference of the above <br> passage? |
| ---: | :--- |
| (A) | Listening to music has no effect on learning and a positive effect on physical <br> exercise. |
| (B) | Listening to music has a clear positive effect both on physical exercise and on <br> learning. |
| (C) | Listening to music has a clear positive effect on physical exercise. Music has a <br> positive effect on learning only in some students. |
| (D) | Listening to music has a clear positive effect on learning in all students. Music <br> has a positive effect only in some students who exercise. |

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Computer Science and Information Technology (CS, Set-2)
Q. 7

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Computer Science and Information Technology (CS, Set-2)

| Q.8 | The number of students in three classes is in the ratio 3:13:6. If 18 students are <br> added to each class, the ratio changes to 15:35:21. <br> The total number of students in all the three classes in the beginning was: |
| ---: | :--- |
| (A) | 22 |
| (B) | 66 |
| (C) | 88 |
| (D) | 110 |

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\begin{tabular}{|c|c|}

\hline Q. 9 \& |  |
| :--- |
| The number of units of a product sold in three different years and the respective net profits are presented in the figure above. The cost/unit in Year 3 was ` 1 , which was half the cost/unit in Year 2. The cost/unit in Year 3 was one-third of the cost/unit in Year 1. Taxes were paid on the selling price at $10 \%, 13 \%$ and $15 \%$ respectively for the three years. Net profit is calculated as the difference between the selling price and the sum of cost and taxes paid in that year. |
| The ratio of the selling price in Year 2 to the selling price in Year 3 is $\qquad$ | <br>

\hline A) \& 4:3 <br>
\hline (B) \& 1:1 <br>
\hline (C) \& 3:4 <br>
\hline (D) \& 1:2 <br>
\hline
\end{tabular}

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Computer Science and Information Technology (CS, Set-2)

| Q.10 | Six students P, Q, R, S, T and U, with distinct heights, compare their heights <br> and make the following observations. <br> Observation I: S is taller than R. <br> Observation II: Q is the shortest of all. <br> Observation III: U is taller than only one student. <br> Observation IV: T is taller than S but is not the tallest. <br> The number of students that are taller than R is the same as the number of <br> students shorter than <br> (A) |
| :--- | :--- |
| (B) | R |
| (C) | S |
| (D) | P |

## Computer Science and Information Technology (CS, Set-2)

Q. 1 - Q. 10 Multiple Choice Question (MCQ), carry ONE mark each (for each wrong answer: - 1/3).

| Q. 1 | Let $G$ be a connected undirected weighted graph. Consider the following two statements. <br> $S_{1}$ : There exists a minimum weight edge in $G$ which is present in every minimum spanning tree of $G$. <br> $S_{2}$ : If every edge in $G$ has distinct weight, then $G$ has a unique minimum spanning tree. <br> Which one of the following options is correct? |
| :---: | :---: |
| (A) | Both $S_{1}$ and $S_{2}$ are true. |
| (B) | $S_{1}$ is true and $S_{2}$ is false. |
| (C) | $S_{1}$ is false and $S_{2}$ is true. |
| (D) | Both $S_{1}$ and $S_{2}$ are false. |


| Q. 2 | Let $H$ be a binary min-heap consisting of $n$ elements implemented as an array. What <br> is the worst case time complexity of an optimal algorithm to find the maximum <br> element in $H ?$ |
| ---: | :--- |
| (A) | $\Theta(1)$ |
| (B) | $\Theta(\log n)$ |
| (C) | $\Theta(n)$ |
| (D) | $\Theta(n \log n)$ |

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Computer Science and Information Technology (CS, Set-2)

| Q.3 | Consider the following ANSI C program: <br> int main() \{ <br> Integer x; <br> return 0; <br> Which one of the following phases in a seven-phase C compiler will throw an error? |
| ---: | :--- |
| (A) | Lexical analyzer <br> (B) |
| (C) | Semantax analyzer |
| (D) | Machine dependent optimizer |


| Q. 4 | The format of the single-precision floating-point representation of a real number as per the IEEE 754 standard is as follows: <br> Which one of the following choices is correct with respect to the smallest normalized positive number represented using the standard? |
| :---: | :---: |
| (A) | exponent $=00000000$ and mantissa $=00000000000000000000000$ |
| (B) | exponent $=00000000$ and mantissa $=0000000000000000000001$ |
| (C) | exponent $=00000001$ and mantissa $=00000000000000000000000$ |
| (D) | exponent $=00000001$ and mantissa $=0000000000000000000001$ |

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| Q. 5 | Which one of the following circuits implements the Boolean function given below? $f(x, y, z)=m_{0}+m_{1}+m_{3}+m_{4}+m_{5}+m_{6}$, where $m_{i}$ is the $i^{\text {th }}$ minterm. |
| :---: | :---: |
| (A) |  |
| (B) |  |
| (C) |  |
| (D) | $\begin{gathered} \begin{array}{cc} x^{\prime}-0 & \\ 1-1 & \\ x=1 \\ x-2 \times 1 \\ 1-3 & \text { Mux } \\ 1-3 & s_{1} \\ \vdots & s_{0} \\ \vdots & i \end{array} \end{gathered} \rightarrow f$ |

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| Q.6 | Consider the following statements S1 and S2 about the relational data model: <br> S1: A relation scheme can have at most one foreign key. <br> S2: A foreign key in a relation scheme R cannot be used to refer to tuples of R. <br> Which one of the following choices is correct? |
| ---: | :--- |
| (A) | Both S1 and S2 are true. |
| (B) | S1 is true and S2 is false. |
| (C) | S1 is false and S2 is true. |
| (D) | Both S1 and S2 are false. |


| Q.7 | Consider the three-way handshake mechanism followed during TCP connection es- <br> tablishment between hosts P and Q. Let X and Y be two random 32-bit starting <br> sequence numbers chosen by P and Q respectively. Suppose P sends a TCP connec- <br> tion request message to Q with a TCP segment having SYN bit $=1$, SEQ number <br> = X, and ACK bit $=0$. Suppose Q accepts the connection request. Which one of <br> the following choices represents the information present in the TCP segment header <br> that is sent by Q to P? |
| ---: | :--- |
| (A) | SYN bit $=1$, SEQ number $=\mathrm{X}+1$, ACK bit $=0$, ACK number $=\mathrm{Y}$, FIN bit $=0$ |
| (B) | SYN bit $=0$, SEQ number $=\mathrm{X}+1$, ACK bit $=0$, ACK number $=\mathrm{Y}$, FIN bit $=1$ |
| (C) | SYN bit $=1$, SEQ number $=\mathrm{Y}$, ACK bit $=1$, ACK number $=\mathrm{X}+1$, FIN bit $=0$ |
| (D) | SYN bit $=1$, SEQ number $=\mathrm{Y}, \mathrm{ACK}$ bit $=1$, ACK number $=\mathrm{X}$, FIN bit $=0$ |

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| Q.8 | What is the worst-case number of arithmetic operations performed by recursive <br> binary search on a sorted array of size $n ?$ |
| ---: | :--- |
| (A) | $\Theta(\sqrt{n})$ |
| (B) | $\Theta\left(\log _{2}(n)\right)$ |
| (C) | $\Theta\left(n^{2}\right)$ |
| (D) | $\Theta(n)$ |


| Q.9 | Let $L \subseteq\{0,1\}^{*}$ be an arbitrary regular language accepted by a minimal DFA with <br> $k$ states. Which one of the following languages must necessarily be accepted by a <br> minimal DFA with $k$ states? |
| :--- | :--- |
| (A) | $L-\{01\}$ |
| (B) | $L \cup\{01\}$ |
| (C) | $\{0,1\}^{*}-L$ |
| (D) | $L \cdot L$ |

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| Q. 10 | Consider the following ANSI C program. ```#include <stdio.h> int main(){ int arr [4] [5]; int i, j; for (i=0; i<4; i++){ for ( }\textrm{j}=0; j<5; j++){ arr[i][j] = 10*i + j; } } printf("%d", *(arr[1] + 9)); return 0; }``` <br> What is the output of the above program? |
| :---: | :---: |
| (A) | 14 |
| (B) | 20 |
| (C) | 24 |
| (D) | 30 |

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Computer Science and Information Technology (CS, Set-2)
Q. 11 - Q. 15 Multiple Select Question (MSQ), carry ONE mark each (no negative marks).

| Q.11 | Consider the following sets, where $n \geq 2:$ <br> $S_{1}:$ Set of all $n \times n$ matrices with entries from the set $\{a, b, c\}$ <br> $S_{2}:$ Set of all functions from the set $\left\{0,1,2, \ldots, n^{2}-1\right\}$ to the set $\{0,1,2\}$ <br> Which of the following choice(s) is/are correct? |
| ---: | :--- |
| (A) | There does not exist a bijection from $S_{1}$ to $S_{2}$. |$\quad$| (B) | There exists a surjection from $S_{1}$ to $S_{2}$. |
| ---: | :--- |$\quad$| (C) | There exists a bijection from $S_{1}$ to $S_{2}$. |
| ---: | :--- |
| (D) | There does not exist an injection from $S_{1}$ to $S_{2}$. |


| Q.12 | Let $L_{1}$ be a regular language and $L_{2}$ be a context-free language. Which of the <br> following languages is/are context-free? |
| :--- | :--- |
| (A) | $L_{1} \cap \overline{L_{2}}$ |
| (B) | $\overline{\overline{L_{1}} \cup \overline{L_{2}}}$ |
| (C) | $L_{1} \cup\left(L_{2} \cup \overline{L_{2}}\right)$ |
| (D) | $\left(L_{1} \cap L_{2}\right) \cup\left(\overline{L_{1}} \cap L_{2}\right)$ |

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| Q.13 | In the context of compilers, which of the following is/are NOT an intermediate <br> representation of the source program? |
| ---: | :--- |
| (A) | Three address code |
| (B) | Abstract Syntax Tree (AST) |
| (C) | Control Flow Graph (CFG) |
| (D) | Symbol table |


| Q.14 | Which of the following statement(s) is/are correct in the context of CPU scheduling? |
| ---: | :--- |
| (A) | Turnaround time includes waiting time. |
| (B) | The goal is to only maximize CPU utilization and minimize throughput. |
| (C) | Round-robin policy can be used even when the CPU time required by each of the <br> processes is not known apriori. |
| (D) | Implementing preemptive scheduling needs hardware support. |

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| Q.15 | Choose the correct choice(s) regarding the following propositional logic assertion <br> $S:$ <br>  <br> $S:((P \wedge Q) \rightarrow R) \rightarrow((P \wedge Q) \rightarrow(Q \rightarrow R))$ |
| :--- | :--- |
| (A) | $S$ is neither a tautology nor a contradiction. |
| (B) | $S$ is a tautology. |
| (C) | $S$ is a contradiction. |
| (D) | The antecedent of $S$ is logically equivalent to the consequent of $S$. |

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Computer Science and Information Technology (CS, Set-2)
Q. 16 - Q. 25 Numerical Answer Type (NAT), carry ONE mark each (no negative marks).

| Q. 16 | Consider a complete binary tree with 7 nodes. Let $A$ denote the set of first 3 <br> elements obtained by performing Breadth-First Search (BFS) starting from the <br> root. Let $B$ denote the set of first 3 elements obtained by performing Depth-First <br> Search (DFS) starting from the root. <br> The value of $\|A-B\|$ is |
| :--- | :--- |

Q. 17 Consider the following deterministic finite automaton (DFA).

| Q. 18 | If $x$ and $y$ are two decimal digits and $(0.1101)_{2}=(0.8 x y 5)_{10}$, the decimal value of <br> $x+y$ is |
| :--- | :--- |

Q. 19

Consider a set-associative cache of size $2 \mathrm{~KB}\left(1 \mathrm{~KB}=2^{10}\right.$ bytes) with cache block size of 64 bytes. Assume that the cache is byte-addressable and a 32-bit address is used for accessing the cache. If the width of the tag field is 22 bits, the associativity of the cache is $\qquad$

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Computer Science and Information Technology (CS, Set-2)
Q. 20 Consider a computer system with DMA support. The DMA module is transferring one 8-bit character in one CPU cycle from a device to memory through cycle stealing at regular intervals. Consider a 2 MHz processor. If $0.5 \%$ processor cycles are used for DMA, the data transfer rate of the device is $\qquad$ bits per second.

| Q.21 | A data file consisting of $1,50,000$ student-records is stored on a hard disk with block <br> size of 4096 bytes. The data file is sorted on the primary key RollNo. The size of <br> a record pointer for this disk is 7 bytes. Each student-record has a candidate key <br> attribute called ANum of size 12 bytes. Suppose an index file with records consisting <br> of two fields, ANum value and the record pointer to the corresponding student record, <br> is built and stored on the same disk. Assume that the records of data file and index <br> file are not split across disk blocks. The number of blocks in the index file is |
| :--- | :--- |


| Q.22 | For a given biased coin, the probability that the outcome of a toss is a head is 0.4. <br> This coin is tossed 1,000 times. Let X denote the random variable whose value <br> is the number of times that head appeared in these 1,000 tosses. The standard <br> deviation of X (rounded to 2 decimal places) is |
| :--- | :--- |


| Q. 23 | ```Consider the following ANSI C function: int SomeFunction(int x, int y) { if ((x == 1) \|| ( y == 1)) return 1; if (x == y) return x; if (x > y) return SomeFunction(x - y, y); if (y > x) return SomeFunction(x, y - x); }``` <br> The value returned by SomeFunction $(15,255)$ is |
| :---: | :---: |

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| Q.24 | Suppose that $P$ is a $4 \times 5$ matrix such that every solution of the equation $P \mathbf{x}=0$ <br> is a scalar multiple of $\left[\begin{array}{lllll}2 & 5 & 4 & 3 & 1\end{array}\right]^{T}$. The rank of $P$ is |
| :--- | :--- |


| Q.25 | Suppose that $f: \mathbb{R} \rightarrow \mathbb{R}$ is a continuous function on the interval $[-3,3]$ and <br> a differentiable function in the interval $(-3,3)$ such that for every $x$ in the <br> interval, $f^{\prime}(x) \leq 2$. If $f(-3)=7$, then $f(3)$ is at most |
| :--- | :--- |

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Computer Science and Information Technology (CS, Set-2)
Q. 26 - Q. 39 Multiple Choice Question (MCQ), carry TWO mark each (for each wrong answer: $-2 / 3$ ).

| Q.26 | Consider the string abbccddeee. Each letter in the string must be assigned a <br> binary code satisfying the following properties: <br> 1. For any two letters, the code assigned to one letter must not be a prefix of the <br> code assigned to the other letter. |
| :--- | :--- |
| 2. For any two letters of the same frequency, the letter which occurs earlier in the |  |
| dictionary order is assigned a code whose length is at most the length of the |  |
| code assigned to the other letter. |  |
| Among the set of all binary code assignments which satisfy the above two properties, |  |
| what is the minimum length of the encoded string? |  |$|$

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| Q.27 | Assume a two-level inclusive cache hierarchy, L1 and L2, where L2 is the larger of <br> the two. Consider the following statements. <br> $S_{1}: \quad$Read misses in a write through L1 cache do not result in writebacks <br> of dirty lines to the L2. <br> Write allocate policy must be used in conjunction with write <br> through caches and no-write allocate policy is used with writeback <br> caches. <br> Which of the following statements is correct? |
| :--- | :--- |
| (A) | $S_{1}$ is true and $S_{2}$ is false |
| (B) | $S_{1}$ is false and $S_{2}$ is true |
| (C) | $S_{1}$ is true and $S_{2}$ is true |
| (D) | $S_{1}$ is false and $S_{2}$ is false |

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Computer Science and Information Technology (CS, Set-2)

| Q.28 | Suppose we want to design a synchronous circuit that processes a string of 0's <br> and 1's. Given a string, it produces another string by replacing the first 1 in any <br> subsequence of consecutive 1's by a 0. Consider the following example. |
| :--- | :--- |
| Input sequence: $\quad 00100011000011100$ <br> Output sequence: 00000001000001100 |  |
| A Mealy Machine is a state machine where both the next state and the output are |  |
| functions of the present state and the current input. |  |
| The above mentioned circuit can be designed as a two-state Mealy machine. The |  |
| states in the Mealy machine can be represented using Boolean values 0 and 1 . We |  |
| denote the current state, the next state, the next incoming bit, and the output bit |  |
| of the Mealy machine by the variables $s, t, b$ and $y$ respectively. |  |
| Assume the initial state of the Mealy machine is 0. |  |
| What are the Boolean expressions corresponding to $t$ and $y$ in terms of $s$ and $b ?$ |  |$|$| (A) | $t=s+b$ <br> $y=s b$ |
| :--- | :--- |
| (B) | $t=b$ <br> $y=s b$ |
| (C) | $t=b$ <br> $y=s \bar{b}$ |
| (D) | $t=s+b$ <br> $y=s \bar{b}$ |

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| Q. 29 | In an examination, a student can choose the order in which two questions (QuesA and QuesB) must be attempted. <br> - If the first question is answered wrong, the student gets zero marks. <br> - If the first question is answered correctly and the second question is not answered correctly, the student gets the marks only for the first question. <br> - If both the questions are answered correctly, the student gets the sum of the marks of the two questions. <br> The following table shows the probability of correctly answering a question and the marks of the question respectively. <br> Assuming that the student always wants to maximize her expected marks in the examination, in which order should she attempt the questions and what is the expected marks for that order (assume that the questions are independent)? |
| :---: | :---: |
| (A) | First QuesA and then QuesB. Expected marks 14. |
| (B) | First QuesB and then QuesA. Expected marks 14. |
| (C) | First QuesB and then QuesA. Expected marks 22. |
| (D) | First QuesA and then QuesB. Expected marks 16. |

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Computer Science and Information Technology (CS, Set-2)

| Q. 30 | Consider the following ANSI C code segment: ```z = x + 3 + y->f1 + y->f2; for (i = 0; i < 200; i = i + 2){ if (z > i) { p = p + x + 3; q=q+y->f1; } else { p = p + y->f2; q=q + x + 3; } }``` <br> Assume that the variable y points to a struct (allocated on the heap) containing two fields $f 1$ and $f 2$, and the local variables $\mathrm{x}, \mathrm{y}, \mathrm{z}, \mathrm{p}, \mathrm{q}$, and i are allotted registers. Common sub-expression elimination (CSE) optimization is applied on the code. The number of addition and dereference operations (of the form $y->f 1$ or $y->f 2$ ) in the optimized code, respectively, are: |
| :---: | :---: |
| (A) | 403 and 102 |
| (B) | 203 and 2 |
| (C) | 303 and 102 |
| (D) | 303 and 2 |

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| Q.31 | The relation scheme given below is used to store information about the employees of <br> a company, where empId is the key and deptId indicates the department to which <br> the employee is assigned. Each employee is assigned to exactly one department. <br> emp(empId, name, gender, salary, deptId) |
| :--- | :--- |
| Consider the following SQL query: <br> select deptId, count (*) <br> from emp <br> where gender = "female" and salary > (select avg(salary) from emp) <br> group by deptId; <br> The above query gives, for each department in the company, the number of <br> female employees whose salary is greater than the average salary of |  |
| (A) | employees in the department. |
| (B) | employees in the company. |
| (C) | female employees in the department. |
| (D) | female employees in the company. |

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## Computer Science and Information Technology (CS, Set-2)

| Q.32 | Let S be the following schedule of operations of three transactions $T_{1}, T_{2}$ and $T_{3}$ <br> in a relational database system: <br> $R_{2}(Y), R_{1}(X), R_{3}(Z), R_{1}(Y), W_{1}(X), R_{2}(Z), W_{2}(Y), R_{3}(X), W_{3}(Z)$ <br> Consider the statements P and Q below: <br> P: S is conflict-serializable. <br> Q: If $T_{3}$ commits before $T_{1}$ finishes, then S is recoverable. <br> Which one of the following choices is correct? |
| ---: | :--- |
| (A) | Both P and Q are true. |
| (B) | P is true and Q is false. <br> (C)P is false and Q is true. <br> (D)Both P and Q are false. |


| Q.33 | A bag has $r$ red balls and $b$ black balls. All balls are identical except for their <br> colours. In a trial, a ball is randomly drawn from the bag, its colour is noted and <br> the ball is placed back into the bag along with another ball of the same colour. <br> Note that the number of balls in the bag will increase by one, after the trial. A <br> sequence of four such trials is conducted. Which one of the following choices gives <br> the probability of drawing a red ball in the fourth trial? |
| ---: | :--- |
| (A) | $\frac{r}{r+b}$ |
| (B) | $\frac{r}{r+b+3}$ |
| (C) | $\frac{r+3}{r+b+3}$ |
| (D) | $\left(\frac{r}{r+b}\right)\left(\frac{r+1}{r+b+1}\right)\left(\frac{r+2}{r+b+2}\right)\left(\frac{r+3}{r+b+3}\right)$ |

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| Q.34 | Consider the cyclic redundancy check (CRC) based error detecting scheme having <br> the generator polynomial $X^{3}+X+1$. Suppose the message $m_{4} m_{3} m_{2} m_{1} m_{0}=11000$ <br> is to be transmitted. Check bits $c_{2} c_{1} c_{0}$ are appended at the end of the message by <br> the transmitter using the above CRC scheme. The transmitted bit string is denoted <br> by $m_{4} m_{3} m_{2} m_{1} m_{0} c_{2} c_{1} c_{0}$. The value of the checkbit sequence $c_{2} c_{1} c_{0}$ is |
| :--- | :--- |
| (A) | 101 |
| (B) | 110 |
| (C) | 100 |
| (D) | 111 |

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| Q. 35 | Consider the following ANSI C program: ```#include <stdio.h> #include <stdlib.h> struct Node{ int value; struct Node *next;}; int main(){ struct Node *boxE, *head, *boxN; int index = 0; boxE = head = (struct Node *) malloc(sizeof(struct Node)); head->value = index; for (index = 1; index <= 3; index++){ boxN = (struct Node *) malloc(sizeof(struct Node)); boxE->next = boxN; boxN->value = index; boxE = boxN; } for (index = 0; index <= 3; index++) { printf("Value at index %d is %d\n", index, head->value); head = head->next; printf("Value at index %d is %d\n", index+1, head->value); } }``` <br> Which one of the statements below is correct about the program? |
| :---: | :---: |
| (A) | Upon execution, the program creates a linked-list of five nodes. |
| (B) | Upon execution, the program goes into an infinite loop. |
| (C) | It has a missing return which will be reported as an error by the compiler. |
| (D) | It dereferences an uninitialized pointer that may result in a run-time error. |

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| Q.36 | Consider the following two statements about regular languages: <br> $S_{1}:$ Every infinite regular language contains an undecidable language as a subset. <br> $S_{2}:$ Every finite language is regular. <br> Which one of the following choices is correct? |
| :--- | :--- |
| (A) | Only $S_{1}$ is true. |
| (B) | Only $S_{2}$ is true. |
| (C) | Both $S_{1}$ and $S_{2}$ are true. |
| (D) | Neither $S_{1}$ nor $S_{2}$ is true. |


| Q. 37 | For two $n$-dimensional real vectors $P$ and $Q$, the operation $s(P, Q)$ is defined as <br> follows: |
| ---: | :--- |
| $\qquad$Let $\mathcal{L}$ be a set of 10 -dimensional non-zero real vectors such that for every pair of <br> distinct vectors $P, Q \in \mathcal{L}, s(P, Q)=0$. What is the maximum cardinality possible <br> for the set $\mathcal{L}$ ? |  |
| (A) | 9 |
| (B) | 10 |
| (C) | 11 |
| (D) | 100 |

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| Q.38 | For a statement $S$ in a program, in the context of liveness analysis, the following <br> sets are defined: <br> $\operatorname{USE}(S) \quad: \quad$ the set of variables used in $S$ <br> $\operatorname{IN}(S) \quad: \quad$ the set of variables that are live at the entry of $S$ <br> $\operatorname{OUT}(S) \quad$ : the set of variables that are live at the exit of $S$ <br> Consider a basic block that consists of two statements, $S_{1}$ followed by $S_{2}$. <br> Which one of the following statements is correct? |
| :--- | :--- |
| (A) | $\operatorname{OUT}\left(S_{1}\right)=\operatorname{IN}\left(S_{2}\right)$ |
| (B) | $\operatorname{OUT}\left(S_{1}\right)=\operatorname{IN}\left(S_{1}\right) \cup \operatorname{USE}\left(S_{1}\right)$ |
| (C) | $\operatorname{OUT}\left(S_{1}\right)=\operatorname{IN}\left(S_{2}\right) \cup \operatorname{OUT}\left(S_{2}\right)$ |
| (D) | $\operatorname{OUT}\left(S_{1}\right)=\operatorname{USE}\left(S_{1}\right) \cup \operatorname{IN}\left(S_{2}\right)$ |


| Q. 39 | For constants $a \geq 1$ and $b>1$, consider the following recurrence defined on the non-negative integers: $T(n)=a \cdot T\left(\frac{n}{b}\right)+f(n)$ <br> Which one of the following options is correct about the recurrence $T(n)$ ? |
| :---: | :---: |
| (A) | If $f(n)$ is $n \log _{2}(n)$, then $T(n)$ is $\Theta\left(n \log _{2}(n)\right)$. |
| (B) | If $f(n)$ is $\frac{n}{\log _{2}(n)}$, then $T(n)$ is $\Theta\left(\log _{2}(n)\right)$. |
| (C) | If $f(n)$ is $O\left(n^{\log _{b}(a)-\epsilon}\right)$ for some $\epsilon>0$, then $T(n)$ is $\Theta\left(n^{\log _{b}(a)}\right)$. |
| (D) | If $f(n)$ is $\Theta\left(n^{\log _{b}(a)}\right)$, then $T(n)$ is $\Theta\left(n^{\log _{b}(a)}\right)$. |

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Computer Science and Information Technology (CS, Set-2)
Q. 40 - Q. 47 Multiple Select Question (MSQ), carry TWO mark each (no negative marks).

| Q.40 | Suppose the following functional dependencies hold on a relation U with attributes <br> $P, Q, R, S$, and $T:$ |
| :--- | :--- |
|  | $P \rightarrow Q R$ <br>  <br>  <br> Which of the following functional dependencies can be inferred from the above <br> functional dependencies? |
| (A) | $P S \rightarrow T$ |
| (B) | $R \rightarrow T$ |
| (C) | $P \rightarrow R$ |
| (D) | $P S \rightarrow Q$ |


| Q.41 | For a string $w$, we define $w^{R}$ to be the reverse of $w$. For example, if $w=01101$ <br> then $w^{R}=10110$. <br> Which of the following languages is/are context-free? |
| ---: | :--- |
| (A) | $\left\{w x w^{R} x^{R} \mid w, x \in\{0,1\}^{*}\right\}$ |
| (B) | $\left\{w w^{R} x x^{R} \mid w, x \in\{0,1\}^{*}\right\}$ |
| (C) | $\left\{w x w^{R} \mid w, x \in\{0,1\}^{*}\right\}$ |
| (D) | $\left\{w x x^{R} w^{R} \mid w, x \in\{0,1\}^{*}\right\}$ |

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| Q. 42 | Consider the following multi-threaded code segment (in a mix of C and pseudocode), invoked by two processes P1 and P2, and each of the processes spawns two threads T1 and T2: ```int x = 0; // global Lock L1; // global main() { create a thread to execute foo(); // Thread T1 create a thread to execute foo(); // Thread T2 wait for the two threads to finish execution; print (x);} foo() { int y = 0; Acquire L1; x = x + 1; y = y + 1; Release L1; print (y);}``` <br> Which of the following statement(s) is/are correct? |
| :---: | :---: |
| (A) | Both P1 and P2 will print the value of x as 2 . |
| (B) | At least one of P1 and P2 will print the value of x as 4 . |
| (C) | At least one of the threads will print the value of y as 2 . |
| (D) | Both T1 and T2, in both the processes, will print the value of y as 1. |

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Computer Science and Information Technology (CS, Set-2)
\(\left.$$
\begin{array}{|l|l|}\hline \text { Q.43 } & \begin{array}{c}\text { Consider a computer system with multiple shared resource types, with one instance } \\
\text { per resource type. Each instance can be owned by only one process at a time. } \\
\text { Owning and freeing of resources are done by holding a global lock (L). The following } \\
\text { scheme is used to own a resource instance : } \\
\text { function OwnREsource(Resource R) } \\
\text { Acquire lock L // a global lock } \\
\text { if R is available then } \\
\text { Acquire R } \\
\text { Release lock L } \\
\text { else } \\
\text { if R is owned by another process P then } \\
\text { Terminate P, after releasing all resources owned by P } \\
\text { Acquire R } \\
\text { Restart P } \\
\text { Release lock L }\end{array}
$$ <br>
end if <br>
end if <br>
end function <br>

Which of the following choice(s) about the above scheme is/are correct?\end{array}\right\}\)| (A) | The scheme ensures that deadlocks will not occur. |
| :--- | :--- |
| (B) | The scheme may lead to live-lock. |
| (C) | The scheme may lead to starvation. |
| (D) | The scheme violates the mutual exclusion property. |

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Computer Science and Information Technology (CS, Set-2)

| Q.44 | If the numerical value of a 2-byte unsigned integer on a little endian computer <br> is 255 more than that on a big endian computer, which of the following choices <br> represent(s) the unsigned integer on a little endian computer? |
| ---: | :--- |
| (A) | $0 \times 6665$ |
| (B) | $0 \times 0001$ |
| (C) | $0 \times 4243$ |
| (D) | $0 \times 0100$ |

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Computer Science and Information Technology (CS, Set-2)
$\left.\begin{array}{|l|l|}\hline \text { Q.45 } & \begin{array}{l}\text { Consider a computer network using the distance vector routing algorithm in its } \\ \text { network layer. The partial topology of the network is as shown below. }\end{array} \\ \text { The objective is to find the shortest-cost path from the router } R \text { to routers } P \text { and } Q \text {. } \\ \text { Assume that } R \text { does not initially know the shortest routes to } P \text { and } Q \text {. Assume that } \\ R \text { has three neighbouring routers denoted as } X, Y, \text { and } Z \text {. During one iteration, } \\ R \text { measures its distance to its neighbours } X, Y, \text { and } Z \text { as } 3,2 \text {, and } 5, \text { respectively. } \\ \text { Router } R \text { gets routing vectors from its neighbours that indicate that the distance } \\ \text { to router } P \text { from routers } X, Y, \text { and } Z \text { are } 7,6, \text { and } 5, \text { respectively. The routing } \\ \text { vector also indicates that the distance to router } Q \text { from routers } X, Y \text {, and } Z \text { are } \\ 4,6, \text { and } 8, \text { respectively. Which of the following statement(s) is/are correct with } \\ \text { respect to the new routing table of } R \text {, after updation during this iteration? }\end{array}\right\}$

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| (A) |
| :--- |
| The graph does not have a topological order. |
| (B) |
| A depth-first traversal starting at vertex S classifies three directed edges as back |
| edges. |
| (C) |
| The graph does not have a strongly connected component. |
| (D) |
| For each pair of vertices $u$ and $v$, there is a directed path from $u$ to $v$. |

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Computer Science and Information Technology (CS, Set-2)

| Q. 47 | Which of the following regular expressions represent(s) the set of all binary numbers <br> that are divisible by three? Assume that the string $\epsilon$ is divisible by three. |
| ---: | :--- |
| (A) | $\left(0+1\left(01^{*} 0\right)^{*} 1\right)^{*}$ |
| (B) | $\left(0+11+10(1+00)^{*} 01\right)^{*}$ |
| (C) | $\left(0^{*}\left(1\left(01^{*} 0\right)^{*} 1\right)^{*}\right)^{*}$ |
| (D) | $\left(0+11+11(1+00)^{*} 00\right)^{*}$ |

Graduate Aptitude Test in Engineering 2021 Organising Institute - IIT Bombay
Computer Science and Information Technology (CS, Set-2)
Q. 48 - Q. 55 Numerical Answer Type (NAT), carry TWO mark each (no negative marks).

| Q. 48 | Consider a three-level page table to translate a 39 -bit virtual address to a physical address as shown below. <br> The page size is $4 \mathrm{~KB}\left(1 \mathrm{~KB}=2^{10}\right.$ bytes $)$ and page table entry size at every level is 8 bytes. A process $P$ is currently using $2 \mathrm{~GB}\left(1 \mathrm{~GB}=2^{30}\right.$ bytes) virtual memory which is mapped to 2 GB of physical memory. The minimum amount of memory required for the page table of $P$ across all levels is $\qquad$ KB. |
| :---: | :---: |



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Computer Science and Information Technology (CS, Set-2)

| Q. 50 | Let $S$ be a set consisting of 10 elements. The number of tuples of the form $(A, B)$ <br> such that $A$ and $B$ are subsets of $S$, and $A \subseteq B$ is |
| :--- | :--- |


| Q. 51 | Consider the following augmented grammar with $\{\#, @,<,>, a, b, c\}$ as the set of terminals. $\begin{aligned} & \mathrm{S}^{\prime} \rightarrow \mathrm{S} \\ & \mathrm{~S} \rightarrow \mathrm{~S} \# c \mathrm{~S} \\ & \mathrm{~S} \rightarrow \mathrm{SS} \\ & \mathrm{~S} \rightarrow \mathrm{~S} @ \\ & \mathrm{~S} \rightarrow<\mathrm{S}> \\ & \mathrm{S} \rightarrow a \\ & \mathrm{~S} \rightarrow b \\ & \mathrm{~S} \rightarrow c \end{aligned}$ <br> Let $\mathrm{I}_{0}=\operatorname{CLOSURE}\left(\left\{\mathrm{S}^{\prime} \rightarrow \bullet \mathrm{S}\right\}\right)$. The number of items in the set $\operatorname{GOTO}\left(\operatorname{GOTO}\left(\mathrm{I}_{0},<\right),<\right)$ is $\qquad$ . |
| :---: | :---: |


| Q. 52 | Consider a Boolean function $f(w, x, y, z)$ such that |
| :--- | :--- |
| $f(w, 0,0, z)=1$ |  |
| $f(1, x, 1, z)=x+z$ |  |
| $f(w, 1, y, z)=w z+y$ |  |$\quad$|  |  |
| ---: | :--- |
|  | The number of literals in the minimal sum-of-products expression of $f$ is |

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## Computer Science and Information Technology (CS, Set-2)

\(\left.\left.$$
\begin{array}{|l|l|}\hline \text { Q.53 } & \begin{array}{l}\text { Consider a pipelined processor with 5 stages, Instruction Fetch (IF), Instruction } \\
\text { Decode (ID), Execute (EX), Memory Access (MEM), and Write Back (WB). Each stage } \\
\text { of the pipeline, except the EX stage, takes one cycle. Assume that the ID stage } \\
\text { merely decodes the instruction and the register read is performed in the EX stage. } \\
\text { The EX stage takes one cycle for ADD instruction and two cycles for MUL instruction. } \\
\text { Ignore pipeline register latencies. } \\
\text { Consider the following sequence of } 8 \text { instructions: }\end{array} \\
\text { ADD, MUL, ADD, MUL, ADD, MUL, ADD, MUL }\end{array}
$$\right\} \begin{array}{l}Assume that every MUL instruction is data-dependent on the ADD instruction just <br>
before it and every ADD instruction (except the first ADD) is data-dependent on the <br>
MUL instruction just before it. The Speedup is defined as follows: <br>
Speedup = Execution time without operand forwarding <br>

Execution time with operand forwarding\end{array}\right\}\) The Speedup achieved in executing the given instruction sequence on the pipelined | processor (rounded to 2 decimal places) is |
| :--- |

Q. 54 Consider a network using the pure ALOHA medium access control protocol, where each frame is of length 1,000 bits. The channel transmission rate is $1 \mathrm{Mbps}\left(=10^{6}\right.$ bits per second). The aggregate number of transmissions across all the nodes (including new frame transmissions and retransmitted frames due to collisions) is modelled as a Poisson process with a rate of 1,000 frames per second. Throughput is defined as the average number of frames successfully transmitted per second. The throughput of the network (rounded to the nearest integer) is $\qquad$

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END OF QUESTION PAPER

